## PAPER : JNU 2018 <br> PHYSICS-PH

## OBJECTIVE QUESTIONS

1. Given the points $\mathrm{P}(0,0,0), \mathrm{Q}(1,1,1), \mathrm{R}(1,1,0)$ and $\mathrm{S}(0,1,1)$ in three-dimensional space, what is the shortest distance between lines PQ and RS?
(a) 1
(b) $\frac{1}{\sqrt{3}}$
(c) $\frac{1}{\sqrt{5}}$
(d) $\frac{1}{\sqrt{6}}$
2. The exponential function $e^{i \theta A}$ of matrix $A=\left(\begin{array}{ll}0 & 1 \\ 1 & 0\end{array}\right)$ is given by which one of the following matrices? Here $\theta$ is an arbitrary real number.
(a) $\left(\begin{array}{cc}0 & e^{i \theta} \\ e^{i \theta} & 0\end{array}\right)$
(b) $\left(\begin{array}{cc}1 & e^{i \theta} \\ e^{-i \theta} & 1\end{array}\right)$
(c) $\left(\begin{array}{cc}\cos \theta & i \sin \theta \\ -i \sin \theta & \cos \theta\end{array}\right)$
(d) $\left(\begin{array}{cc}\cos \theta & -i \sin \theta \\ i \sin \theta & \cos \theta\end{array}\right)$
3. What is the solution of the differential equation $y^{\prime \prime}+y^{\prime}=b x$, with the boundary conditions $y(0)=1$ and $y^{\prime}(0)=0$ ? Here $b$ is a constant, $y^{\prime}=\frac{d y}{d x}$ and $y^{\prime \prime}=d^{2} y / d x^{2}$ ?
(a) $y(x)=(1-b)+\frac{b}{2} x(x+2)+b e^{-x}$
(b) $y(x)=(1-b)-\frac{b}{2} x(x-2)+b e^{-x}$
(c) $y(x)=(1+b)-\frac{b}{2} x(x+2)-b e^{-x}$
(d) $y(x)=(1+b)+\frac{b}{2} x(x-2)-b e^{-x}$
4. What is the value of the following complex integral?

$$
\int^{2} e^{2} A T A E E R E N D E A V O U R
$$

Here $C$ denotes the unit circle $|z|=1$ traversed counter-clockwise
(a) $2 \pi i$
(b) $\pi i$
(c) $2 \pi i / 5$
(d) $\pi i / 3$
5. A point particle of mass $m$ is placed on the inner surface of a frictionless bowl which has the shape of a paraboloid of revolution given by the equation $z=a\left(x^{2}+y^{2}\right)$. The gravity $g$ is acting vertically downwards (along the negative z-direction). At what angular speed should be the bowl be rotated about the vertical axis so that the particle remains stationary?
(a) $\sqrt{2 a g}$
(b) $\sqrt{a g}$
(c) $\sqrt{2 g / a}$
(d) $1 / \sqrt{2 a g}$
6. The stiffness $k_{C}$ of a spring when compressed from its equilibrium length is given to be different from its stiffness $k_{s}$ when stretched. The potential energy $V(x)$, stored in this spring for an arbitrary compression or stretching $x$, is given by $V(x)=k_{C} x^{2} / 2$ for $x<0$ and $V(x)=k_{S} x^{2} / 2$ for $x \geq 0$. A particle of mass $m$ is attached to the one end of this spring, while the other end is fixed. The mass of the spring is negligible. Starting at time $t=0$, with the compressed spring and the particle at rest at $x(0)=-1$, this system undergoes an oscillatory motion. What is the angular frequency of its oscillation?
(a) $\sqrt{\frac{k_{C}+k_{S}}{2 m}}$
(b) $\frac{2}{\sqrt{m}} \frac{\sqrt{k_{C} k_{S}}}{\sqrt{k_{C}}+\sqrt{k_{S}}}$
(c) $\frac{1}{2}\left[\sqrt{\frac{k_{C}}{m}}+\sqrt{\frac{k_{S}}{m}}\right]$
(d) $\sqrt{\frac{2 k_{C} k_{S}}{m\left(k_{C}+k_{S}\right)}}$
7. A uniform string of length 2 m and mass 10 g is under a tension of 8 N , with both ends fixed. If the string is plucked transversely and then touched at a point 80 cm away from one end, the vibrational modes of what frequencies will persist?
(a) All integer multiples of 10 Hz
(b) All integer multiples of 20 Hz
(c) All integers multiples of 25 Hz
(d) All integer multiples of 50 Hz
8. A concave-convex lens of negligible thickness has refractive inded of 1.5 , and its radii of curvature are 10 cm (for the convex surface) and 20 cm (for the concave surface). The lens is placed horizontally with concave surface facing upwards which is filled with an oil of refractive index 1.6. What is the focal length of this lens filled with oil?
(a) 18.18 cm
(b) 40.12 cm
(c) 20.5 cm
(d) 6.3 cm
9. Consider the fringes produced with monochromatic light of wavelength $5880 \AA$ in a Young's doubleslit experiment. When a thin glass plate of refractive index 1.5 is placed normally in front of one of the slits, the central bright fringe is shifted to a position where the third bright fringe from the centre was before the plate was placed. What is the thickness of this glass plate?
(a) $1.176 \mu \mathrm{~m}$
(b) $1.764 \mu \mathrm{~m}$
(c) $2.941 \mu \mathrm{~m}$
(d) $3.528 \mu \mathrm{~m}$
10. Consider a solid cube with a uniform charge density. Let the electrostatic potential be $\mathrm{V}_{1}$ at its centre, and $\mathrm{V}_{2}$ at any corner of the cube. The potential is zero at infinity. What is the $\mathrm{V}_{1} / \mathrm{V}_{2}$ ?
(a) 2
(b) $\frac{2}{\sqrt{3}}$
(c) $\frac{1}{2}$
(d) 8
11. A metallic disc of radius 0.1 m rotates about its vertical axis with a rotational speed of 10 revolutions per second in a uniform magnetic field $(\mathrm{B})$ of 0.1 tesla. If a $1 \Omega$ resistor is connected between the axle and the outer edge of the disc, then the current flowing through the resistor is

(a) 5 mA
(b) 31.4 mA
(c) 15.7 mA
(d) 10 mA
12. The photoelectric effect can be demonstrated by shining light on a metallic surface in an evacuated chamber which results in a current of photoelectrons. To stop the photoelectric current $\left(i_{p}\right)$, a negative voltage is applied between cathode and anode using a variable voltage source (V), and the corresponding stopping potential $\left(\mathrm{V}_{\mathrm{s}}\right)$ is determined. In a typical experiment, the photoelectric current is measured by varying V with fixed intensity $(\mathrm{I})$ and frequency $(v)$ of the incident light. Based on the resultant findings sketched in graphs $[(\mathrm{A}),(\mathrm{B}),(\mathrm{C})]$ below, which of the following conclusions are correct?
(i) The work function of tugnsten (W) is more than that of potassium (K)
(ii) The saturation current is independent of the frequency of light for a fixed $I$.
(iii) The $\mathrm{V}_{\mathrm{s}}$ depends on the intensity of light
(iv) The Planck constant can be estimated from graph [C]
(v) The graph [C] is explainable by classical electrodynamics
(vi) In graph [B], $v_{1}>v_{2}$

(A)

(B)

(C)
(a) (i), (ii) and (iv) are the correct conclusions
(b) (i), (iv) and (v) are the correct conclusions
(c) (ii), (iii), (v) and (vi) are the correct conclusions
(d) (i), (ii), (iv) and (vi) are the correct conclusions
13. A particle in one dimension is given to be in the quantum state $\psi(x)=e^{(a+i b) x-\frac{1}{2} x^{2}}$, where $a$ and $b$ are real-valued constants. What are the position and momentum expectation values, $\langle x\rangle$ and $\langle p\rangle$ respectively, of the particle in this state?
(a) $\langle x\rangle=a$ and $\langle p\rangle=\frac{\hbar}{2 a}$
(b) $\langle x\rangle=a$ and $\langle p\rangle=\hbar b$
(c) $\langle x\rangle=a e^{a^{2}} \sqrt{\pi}$ and $\langle p\rangle=\hbar b e^{-b^{2}} \sqrt{\pi}$
(d) $\langle x\rangle=a e^{a^{2}} \sqrt{\pi}$ and $\langle p\rangle=\hbar b e^{a^{2}} \sqrt{\pi}$
14. The unstable oxygen nuclei ${ }_{8}^{14} O$ and ${ }_{8}^{19} O$ undergo beta decay. Which of the following do you expect to happen?
(a) ${ }_{8}^{14} \mathrm{O}$ undergoes positive beta decay and ${ }_{8}^{19} \mathrm{O}$ undergoes positive beta decay.
(b) ${ }_{8}^{14} \mathrm{O}$ undergoes negative beta decay and ${ }_{8}^{19} \mathrm{O}$ undergo positive beta decay
(c) Both ${ }_{8}^{14} \mathrm{O}$ and ${ }_{8}^{19} \mathrm{O}$ undergo positive beta decay
(d) Both ${ }_{8}^{14} O$ and ${ }_{8}^{19} O$ undergo negative beta decay.
15. An X-ray tube operates at an applied voltage of 15000 V . What is the shortest wavelength of the Xray emitted by this tube?
(a) $0.83 \AA$
(b) $0.66 \AA$
(c) $1.2 \AA$
(d) $2.1 \AA$
16. The work (in mega electron volts) that must be done to increase the speed of an electron from 0.4 c to 0.8 c (where $c$ is the speed of light) is approximately.
(a) 0.1 MeV
(b) 0.3 MeV
(c) 0.5 MeV
(d) 0.7 MeV
17. Consider a three-level atom with energy levels, $0, \varepsilon_{1}$ and $\varepsilon_{2}$. What is the probability of finding the atom in the energy level $\varepsilon_{2}$ at temperature $T\left(\right.$ with $\left.\beta=\frac{1}{k_{B} T}\right)$ ?
(a) 0
(b) $e^{-\beta \varepsilon_{2}}$
(c) $e^{-\beta \varepsilon_{1}} /\left(1+e^{-\beta \varepsilon_{1}}+e^{-\beta \varepsilon_{2}}\right)$
(d) $e^{-\beta \varepsilon_{2}} /\left(1+e^{-\beta \varepsilon_{1}}+e^{-\beta \varepsilon_{2}}\right)$
18. For a gas at fixed temperature, pressure and particle number $(T, P, N)$, the natural thermodynamic potential is $\mathrm{G}=\mathrm{U}-\mathrm{TS}+\mathrm{PV}$, where U is the internal energy, V is volume and S is entropy. Which of the following is the corresponding potential for a gas at fixed $(T, V, \mu)$ ? Here $\mu$ is the chemical potential.
(a) $G+T S$
(b) $G-P V$
(c) $G-P V+\mu N$
(d) $G-P V-\mu N$
19. Two moles of an ideal gas is kept at a temperature of 300 K in a container of $1 \mathrm{~m}^{3}$ volume. At this temperature, particle number and volume, what is the rate of change of its entropy with pressure in SI units?
(a) 300
(b) -600
(c) $-1 / 300$
(d) $1 / 600$
20. What is the number of lattice points contained in a primitive unit cell of the f.c.c. (face centred cubic) lattice?
(a) 1
(b) 2
(c) 3
(d) 4
21. Which one of the following is not true for the specific heat $\left(C_{V}\right)$ of solids?
(a) The $C_{V}$ decreases as temperature ( T ) decreases
(b) According to Debye model, $C_{V} \propto T^{3}$ at low temperature
(c) The Einstein model accounts for the contribution to $C_{V}$ from the acoustic modes of lattice vibrations.
(d) The Debye model accounts for the contribution to $C_{V}$ from the acoustic modes of lattice vibrations.
22. What is the concentration of electrons and holes at a temperature of 300 K in an intrinsic semiconductor with the band gap 1.1 eV ? In this semiconductor, the effective mass of electrons is given to be $0.7 m_{e}$ and the effective mass of holes is $m_{e}$. Here $m_{e}$ denotes the rest mass of a free electron.
(a) $2.1 \times 10^{17} \mathrm{~m}^{-3}$
(b) $8.5 \times 10^{16} \mathrm{~m}^{-3}$
(c) $1.1 \times 10^{16} \mathrm{~m}^{-3}$
(d) $1.1 \times 10^{15} \mathrm{~m}^{-3}$
23. Consider the circuit drawn below of a resistor ( R ), capacitor ( C ) and inductor (L) with an applied time-dependent voltage $\mathrm{V}(\mathrm{t})$. Let $\mathrm{V}_{1}$ be the resultant voltage at any time $t$ across the inductor. Which one of the following differential equations correctly applies to this circuit? Here $V_{1}=d V_{1} / d t$ and $V_{1}=d^{2} V_{1} / d t^{2}$

(a) $R C \ddot{V}_{1}+\dot{V}_{1}+(R / L) V_{1}=\dot{V}(t)$
(b) $R C \ddot{V}_{1}+\dot{V}_{1}-(R / L) V_{1}=\dot{V}(t)$
(c) $R C \ddot{V}_{1}+\dot{V}_{1}+(R / L) \dot{V}_{1}+V_{1}=V(t)$
(d) $R C \ddot{V}_{1}-\dot{V}_{1}+(R / L) \dot{V}_{1}+V_{1}=V(t)$
24. The Boolean expression $B \cdot(A+B)+A \cdot(\bar{B}+A)$ can be realized using a minimum number of
(a) 1 NAND gate
(b) 2 AND gates
(c) 1 OR gate
(d) 1 NOR gate
25. For an input voltage $V_{i}=1 \mathrm{mV}$, what is the output voltage $\mathrm{V}_{\mathrm{O}}$ in the following circuit of an ideal OPAMP (Operational Amplifier)?

(a) -10 mV
(b) 62 mV
(c) 31 mV
(d) 11 mV

