

2012 CA

Test Paper Code: CA

Time: 3 Hours

Max. Marks: 300

**INSTRUCTIONS****A. General:**

1. This Booklet is your Question Paper. It contains **20** pages and has 100 questions.
2. The Question Booklet **Code** is printed on the right-hand top corner of this page.
3. The Question Booklet contains blank spaces for your rough work. No additional sheets will be provided for rough work.
4. **Clip board, log tables, slide rule, calculator, cellular phone or any other electronic gadget in any form are NOT allowed.**
5. Write your **Name** and **Registration Number** in the space provided at the bottom.
6. All answers are to be marked only on the machine gradable Objective Response Sheet (**ORS**) provided along with this booklet, as per the instructions therein.
7. The Question Booklet along with the Objective Response Sheet (**ORS**) must be handed over to the Invigilator before leaving the examination hall.
8. Refer to **Special Instruction/Useful Data** on reverse of this sheet.

**B. Filling-in the ORS:**

9. Write your Registration Number in the boxes provided on the upper left-hand-side of the **ORS** and darken the appropriate bubble under each digit of your Registration Number using a **HB pencil**.
10. Ensure that the **code** on the **Question Booklet** and the **code** on the **ORS** are the same. If the codes do not match, report to the Invigilator immediately.
11. On the lower-left-hand-side of the **ORS**, write your Name, Registration Number, and Name of the Test Centre and put your signature in the appropriate box with ball-point pen. Do not write these anywhere else.

**C. Marking of Answers on the ORS:**

12. Each question has **4 choices** for its answer: (A), (B), (C) and (D). Only **ONE** of them is the correct answer.
13. On the right-hand-side of **ORS**, for each question number, darken with a **HB Pencil ONLY** one bubble corresponding to what you consider to be the most appropriate answer, from among the four choices.
14. There will be **negative marking** for wrong answers.

**MARKING SCHEME:**

- (a) For each correct answer, you will be awarded **3 (Three)** marks.
- (b) For each wrong answer, you will be awarded **-1 (Negative one)** mark.
- (c) Multiple answers to a question will be treated as a wrong answer.
- (d) For each un-attempted question, you will be awarded **0 (Zero)** mark.

<b>Name</b>							
<b>Registration Number</b>							

**Special Instructions/ Useful Data**

$\mathbb{N}$  denotes the set of natural numbers  $\{1, 2, 3, \dots\}$

$\mathbb{Z}$  denotes the set of integers

$\mathbb{Q}$  denotes the set of rational numbers

$\mathbb{R}$  denotes the set of real numbers

$\mathbb{C}$  denotes the set of complex numbers

$A \setminus B = \{x \in A \mid x \notin B\}$  for two sets  $A$  and  $B$

LPP denotes Linear Programming Problem

Max  $f$  denotes the maximum of  $f$

Min  $f$  denotes the minimum of  $f$

$x'$  denotes the complement of a Boolean variable  $x$

$f'$  denotes the first derivative of a function  $f$

$f_x$  denotes the partial derivative of  $\frac{\partial f}{\partial x}$  of  $f$

$f_y$  denotes the partial derivative of  $\frac{\partial f}{\partial y}$  of  $f$

$\nabla f$  denotes the gradient of a function  $f$

For all C programs, assume that all standard library functions are accessible.

Q.1 Who created the first free email service on the Internet?

- (A) B. W. Kernighan (B) Bill Gates  
 (C) N. Karmakar (D) Sabeer Bhatia

Q.2 Let  $S = \{x \in \mathbb{Q} \mid x^2 \in \{1, 20, 21\}\}$ . Then the number of elements in the set  $S$  is

- (A) 1 (B) 2 (C) 4 (D) 6

Q.3 The rank of the matrix  $\begin{bmatrix} 1 & 2 & 4 & 1 & -2 \\ 2 & 3 & 7 & 1 & -2 \\ 1 & 0 & 2 & -1 & 2 \\ 1 & -1 & 1 & -2 & 4 \end{bmatrix}$  is

- (A) 1 (B) 2 (C) 3 (D) 4

Q.4 Mega FLOPS stands for

- (A)  $10^9$  floating point operations per second  
 (B)  $10^5$  fixed point operations per second  
 (C)  $10^6$  floating point operations per second  
 (D)  $10^{12}$  fixed point operations per second

Q.5 The set  $S = \{(x, y) \in \mathbb{R}^2 \mid x \notin \mathbb{Q} \text{ or } y \notin \mathbb{Z}\}$  is

- (A)  $(\mathbb{R} \setminus \mathbb{Q}) \times (\mathbb{R} \setminus \mathbb{Z})$  (B)  $(\mathbb{R} \times \mathbb{R}) \times (\mathbb{Q} \setminus \mathbb{Z})$  (C)  $(\mathbb{R} \setminus \mathbb{Q}) \times \mathbb{R}$  (D)  $\mathbb{R} \times (\mathbb{R} \setminus \mathbb{Z})$

Q.6 The number  $20^6 - 13^6$  is divisible by

- (A) 11 (B) 5 (C) 13 (D) 6

Q.7 The inverse of the matrix  $\begin{bmatrix} 1 & 1 & 1 \\ 2 & 3 & 2 \\ 3 & 8 & 2 \end{bmatrix}$  is

- (A)  $\begin{bmatrix} 10 & -6 & 1 \\ -2 & -1 & 0 \\ -7 & -5 & -1 \end{bmatrix}$  (B)  $\begin{bmatrix} 10 & -6 & 1 \\ -2 & -1 & 0 \\ -7 & -5 & 1 \end{bmatrix}$   
 (C)  $\begin{bmatrix} 10 & -6 & -1 \\ -2 & 1 & 0 \\ -7 & 5 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} 10 & -6 & 1 \\ -2 & 1 & 0 \\ -7 & 5 & -1 \end{bmatrix}$

Q.8 Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be defined by  $f(x) = x^2 + 4x + 5$ . Then which of the following statements is TRUE?

- (A)  $f$  is one-one. (B)  $f$  is on-to.  
 (C)  $f$  is one-one and on-to. (D)  $f$  is neither one-one nor on-to.

Q.9 The number of distinct 3 digit numbers greater than 100 where no digit repeats itself is

- (A) 504 (B) 648 (C) 326 (D) 210

Q.10 The digit at the unit place of the number  $19^{25}$  is

- (A) 1 (B) 3 (C) 5 (D) 9

Q.11 The differential equation

$$\frac{dy}{dx} + (\tan x)y = \cos x, \quad x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$$

has the solution

- (A)  $y = (x + c)\cos x$  (B)  $y = (x + c)\sec x$   
 (C)  $y = (x + c)\sin x$  (D)  $y = (x + c)\operatorname{cosec} x$

Q.12 Consider the function  $f(x) = -x^4 + 2x^3 - 1$ . What is the absolute truncation error for evaluation of  $f'(x)$  at  $x = 0.5$  by the first order forward difference scheme using a step size,  $h = 0.5$ ?

- (A)  $\frac{5}{8}$  (B)  $\frac{1}{2}$  (C)  $\frac{1}{3}$  (D)  $\frac{8}{5}$

Q.13 Consider the following LPP

$$\text{Max } f = 5x + 12y$$

subject to

$$\begin{aligned} x + 5y &\leq 50, \\ 6x + 3y &\leq 36, \\ x &\leq 5, x \geq 0, y \geq 0 \end{aligned}$$

The number of extreme points of the feasible region are

- (A) 4 (B) 5 (C) 6 (D) 7

Q.14 Solution of the initial value problem

$$(2 \cos y + 3x)dx - x \sin y dy = 0, \quad y(1) = 0$$

is

- (A)  $x^2 \cos y + y^3 = 1$  (B)  $x^2 \sin y + y^3 = 0$   
 (C)  $x^2 \cos y + x^3 = 2$  (D)  $y^2 \sin x + y^3 = 0$

Q.15 Let  $\alpha$  be a real number and  $G = \{z \in \mathbb{C} \setminus \{0\} \mid |z| = \alpha\}$ . Then  $G$  is a group under multiplication of complex numbers if

- (A)  $\alpha = 0$                       (B)  $\alpha < 1$                       (C)  $\alpha > 1$                       (D)  $\alpha = 1$

Q.16 Order the following processors in the increasing order of speed.

M1: 486,                      M2: 8085,                      M3: Dual core,                      M4: Pentium III

- (A) M1 M2 M3 M4      (B) M2 M1 M4 M3      (C) M1 M2 M4 M3      (D) M1 M3 M4 M2

Q.17 Which of the following statements is TRUE?

- (A) There exists a field with 1000 elements.  
 (B) There exists a field with 100 elements.  
 (C) There exists a field with 500 elements.  
 (D) There exists a field with 9 elements

Q.18 A particular solution of the differential equation

$$\frac{d^5 y}{dx^5} - 3 \frac{d^4 y}{dx^4} + 3 \frac{d^3 y}{dx^3} - \frac{d^2 y}{dx^2} = 2e^x$$

is

- (A)  $\frac{1}{3}x^3 e^x$                       (B)  $\frac{1}{2}x^3 e^x$                       (C)  $\frac{1}{6}x^3 e^x$                       (D)  $\frac{2}{3}x^3 e^x$

Q.19 For an LPP, if the constraints are

$$\begin{aligned} x + y &\leq 3, \\ -x + 3y &\leq 5, \\ y &\geq 0, x \geq 0 \end{aligned}$$

then which one of the following point is NOT a feasible point?

- (A) (3,0)                      (B) (1,2)                      (C) (2,4)                      (D)  $\left(0, \frac{5}{3}\right)$

Q.20 The volume of the tetrahedron bounded by the planes  $z = 0, x = 0, y = 0$  and  $y + z - x = 1$  is

- (A) 1/6                      (B) 6                      (C) 1                      (D) 1/3

Q.21 Aadhar Unique Identification (UID) number is of

- (A) 10 digits                      (B) 12 digits                      (C) 14 digits                      (D) 16 digits

Q.22 The general solution of the nonhomogeneous differential equation

$$\frac{d^2y}{dx^2} + \frac{dy}{dx} - 12y = 150 \cos 3x$$

is

- (A)  $c_1e^{-3x} + c_2e^{4x} - 7 \cos 3x - \sin 3x$
- (B)  $c_1e^{3x} + c_2e^{-4x} - 7 \cos 3x + \sin 3x$
- (C)  $c_1e^{3x} + c_2e^{-4x} + 7 \cos 3x + \sin 3x$
- (D)  $c_1e^{3x} + c_2e^{-4x} - 7 \cos 3x - \sin 3x$

Q.23 Which of the following is/are main memory of a computer?

P: RAM,      Q: Hard disk,      R: CDROM,      S: Pen drive

- (A) P and Q only      (B) Q only      (C) P only      (D) P, R, and S only

Q.24 The boundary value problem

$$\frac{d^2y}{dx^2} + \pi^2y = 0, \quad y(0) = 0, \quad y(1) = 0$$

has

- (A) two solutions      (B) no solution
- (C) unique solution      (D) infinitely many solutions

Q.25 Suppose  $\vec{a} = \hat{i} - 2\hat{j} + 3\hat{k}$ ,  $\vec{b} = \hat{i} + \hat{k}$  and  $\vec{c} = \hat{i} - \hat{j} + 3\hat{k}$ . Then  $\vec{a} \times (\vec{b} \times \vec{c})$  is

- (A)  $8\hat{i} + 4\hat{j}$       (B)  $8\hat{i} - 4\hat{j}$       (C)  $8\hat{i} + 8\hat{j}$       (D)  $8\hat{i} - 8\hat{j}$

Q.26 The Newton-Raphson method is used to find a real root of  $f(x) = x^3 - x + 1 = 0$  with initial approximation  $x_0 = 1$ . Then the second approximation  $x_2$  is

- (A)  $\frac{1}{2}$       (B)  $\frac{5}{8}$       (C) 2      (D) 3

Q.27 SMS stands for

- (A) Short Message Service      (B) Secured Message Service
- (C) Short Mail Service      (D) Secured mail Service

Q.28 What is the probability of getting an even number or a number less than 5, in tossing a fair die?

- (A)  $\frac{2}{3}$       (B)  $\frac{1}{3}$       (C)  $\frac{5}{6}$       (D)  $\frac{1}{6}$

Q.29 Rabindranath Tagore won the Nobel prize in Literature for his book entitled

- (A) War and Peace (B) Malgudi Days  
(C) Gitanjali (D) Durgeshnandini

Q.30 Which company is the leader in computer networking?

- (A) Wipro (B) Cisco (C) Oracle (D) TCS

Q.31 For the table

$x$	0	1	2	3
$f(x)$	1	2	9	28

the divided difference  $f[1,2,3]$  is

- (A) 6 (B) 13 (C) 3 (D) 1

Q.32 Which one of the following is equivalent to 8 Giga bytes?

- (A)  $2^{23}$  bytes (B)  $2^{33}$  bytes (C)  $2^{43}$  bytes (D)  $2^{53}$  bytes

Q.33 The decimal value of  $(327)_8 \times (25)_8$  is

- (A) 5625 (B) 8175 (C) 3267 (D) 4515

Q.34 The value of the integral  $\int_0^2 (1+5x-100x^2)dx$  by Simpson's  $\frac{1}{3}$ rd rule is

- (A) -288 (B)  $-\frac{764}{3}$  (C) 288 (D) 289

Q.35 Which one of the following stands for LAN?

- (A) Local Area Network (B) Logical Area Network  
(C) Large Area Network (D) Least Area Network

Q.36 The Boolean expression  $(x + y) (x + y')$  is equivalent to

- (A)  $x + y$  (B)  $y$  (C)  $xy$  (D)  $x$

Q.37 ISP stands for

- (A) Internet Security Protocol (B) Intelligent Service Package  
(C) Internet Service Provider (D) Intelligent Service Provider

- Q.38 Let  $f(x, y) = \cos(xy) + x \cos y$ . Then the value of  $f_x(2, \pi/2) + f_y(2, \pi/2)$  is  
 (A) 0 (B) -2 (C) 2 (D) 4
- Q.39 If  $\vec{a} = 2\hat{i} - \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} - 2\hat{j} + 2\hat{k}$  and  $\vec{c} = 4\hat{i} - 3\hat{j} + 2\hat{k}$ , then the projection of  $\vec{a} + \vec{b}$  on the vector  $\vec{b}$  is  
 (A)  $\frac{20}{3}$  (B) 20 (C)  $\frac{20}{9}$  (D)  $\frac{8}{3}$
- Q.40 For what value of  $\alpha$ , the vectors  $2\hat{i} + \hat{j} + \hat{k}$ ,  $\alpha\hat{i} + 2\hat{j} + 2\hat{k}$  and  $\hat{i} + \hat{j} - \hat{k}$  are coplanar?  
 (A) 1 (B) 2 (C) 4 (D) 8
- Q.41 The next term in the sequence of ternary number 10, 20, 100, 110, ... is  
 (A) 120 (B) 111 (C) 112 (D) 101
- Q.42 The 9's complement of 123456789 is  
 (A) 876543211 (B) 876543210 (C) 987654321 (D) 012345678
- Q.43 What is the largest unsigned integer that can be expressed with  $n$  bits?  
 (A)  $2^{n-1}$  (B)  $2^n - 1$  (C)  $2^n + 1$  (D)  $2^{n+1}$
- Q.44 Suppose  $f(x) = x^3 + 2x^2 + x + 1$ . Then the polynomial that interpolates the value of  $f$  at  $x = -1, 0, 1$  is  
 (A)  $4x^2 + 4x + 1$  (B)  $x^2 + x + 1$   
 (C)  $2x^2 + 2x + 1$  (D)  $3x^2 + 3x + 1$
- Q.45 A search engine is  
 (A) a machine (B) a web site  
 (C) a movie (D) a map used for driving



Q.46 The Lagrange form of the interpolating polynomial that fits the data

$x$	0	1	2
$f(x)$	1	2	5

is

- (A)  $\frac{1}{2}(x-1)(x-2) - 2x(x+2) + \frac{5}{2}x(x-1)$
- (B)  $\frac{1}{2}(x-1)(x-2) + 2x(x+2) + \frac{5}{2}x(x-1)$
- (C)  $2(x-1)(x-2) + \frac{1}{2}x(x+2) + \frac{2}{5}x(x-1)$
- (D)  $2(x-1)(x-2) - \frac{1}{2}x(x+2) + \frac{2}{5}x(x-1)$

Q.47 The function  $f(x, y) = xy$  defined on  $x^2 + y^2 \leq 1$  has

- (A) both maximum and minimum values
- (B) only maximum value
- (C) only minimum value
- (D) neither maximum nor minimum value

Q.48 The area of the region enclosed by the parabola  $x^2 = 4ay$  and the line  $x = 2a$  with  $x$ -axis is

- (A)  $\frac{4}{3}a^2$
- (B)  $\frac{3}{2}a^2$
- (C)  $\frac{3}{4}a^2$
- (D)  $\frac{2}{3}a^2$

Q.49 Consider the system of linear equations

$$\begin{aligned} x - 2y + z &= 3 \\ 2x + \alpha z &= -2 \\ -2x + 2y + \alpha z &= 1 \end{aligned}$$

In order to have unique solution to this linear system of equations the value of  $\alpha$  should not be equal to

- (A)  $-\frac{2}{3}$
- (B)  $\frac{2}{3}$
- (C)  $\frac{4}{3}$
- (D)  $-\frac{4}{3}$

Q.50 The quadratic approximation of  $f(x, y) = \cos x \cos y$  about the point  $(0, 0)$  is

- |                                  |                                  |
|----------------------------------|----------------------------------|
| (A) $1 + \frac{1}{2}(x^2 - y^2)$ | (B) $1 + \frac{1}{2}(x^2 + y^2)$ |
| (C) $1 - \frac{1}{2}(x^2 - y^2)$ | (D) $1 - \frac{1}{2}(x^2 + y^2)$ |

Q.51 Consider the following two lists:

- | List I       | List II            |
|--------------|--------------------|
| 1: Mouse     | P: Input device    |
| 2: Modem     | Q: External memory |
| 3: Pen drive | R: Web browser     |
| 4: Opera     | S: Network device  |

The correct match is

- |  |  |
|--|--|
| (A) $1 \rightarrow R, 2 \rightarrow S, 3 \rightarrow P, 4 \rightarrow Q$ | (B) $1 \rightarrow P, 2 \rightarrow S, 3 \rightarrow Q, 4 \rightarrow R$ |
| (C) $1 \rightarrow S, 2 \rightarrow R, 3 \rightarrow Q, 4 \rightarrow P$ | (D) $1 \rightarrow P, 2 \rightarrow Q, 3 \rightarrow S, 4 \rightarrow R$ |

Q.52 The matrix  $\begin{bmatrix} -1 & 2 & 2 \\ 2 & 2 & -1 \\ 2 & -1 & 2 \end{bmatrix}$  has

- (A) all positive eigenvalues  
 (B) all negative eigenvalues  
 (C) some positive eigenvalues and some negative eigenvalues  
 (D) one zero eigenvalue

Q.53 An integrating factor of the differential equation  
 $2 \sinh x \cos y \, dx - \cosh x \sin y \, dy = 0$   
 is

- |               |               |              |              |
|---------------|---------------|--------------|--------------|
| (A) $\cosh x$ | (B) $\sinh x$ | (C) $\sin x$ | (D) $\cos x$ |
|---------------|---------------|--------------|--------------|

Q.54 The random variable  $X$  follows the Poisson distribution with variance 4. The mean of this Poisson distribution is

- |       |       |        |       |
|-------|-------|--------|-------|
| (A) 2 | (B) 4 | (C) 16 | (D) 8 |
|-------|-------|--------|-------|

Q.55 Two balls are drawn in succession from a box containing 30 red, 20 white, 10 blue and 15 orange balls; replacement being made after each draw. The probability that neither is orange is

- |                     |                    |                    |                     |
|---------------------|--------------------|--------------------|---------------------|
| (A) $\frac{16}{25}$ | (B) $\frac{9}{25}$ | (C) $\frac{1}{25}$ | (D) $\frac{24}{25}$ |
|---------------------|--------------------|--------------------|---------------------|

Q.56 Let the function  $f$  has the values  $f_0, f_1, f_2$  at equidistant nodal points  $x_0, x_1, x_2$  where  $x_i = x_0 + ih, i = 1, 2$ . Then, the divided difference  $f[x_0, x_1, x_2]$  is equal to

- (A)  $\frac{\nabla f_2}{2h}$                       (B)  $\frac{\Delta f_0}{2h}$                       (C)  $\frac{\Delta^2 f_0}{2h^2}$                       (D)  $\frac{\nabla f_1}{2h}$

Q.57 Let  $\sigma = (1, 3, 5, 7, 9, 10)(2, 4, 6, 8)$  be a permutation in  $S_{10}$ . Then the smallest positive integer  $m$  such that  $\sigma^m = Id$ , the identity permutation, is

- (A) 24                      (B) 6                      (C) 4                      (D) 12

Q.58 Consider the following two lists:

**List I**

- 1: TFT
- 2: RAM
- 3: ROM
- 4: CRT

**List II**

- P: Visual display unit
- Q: Volatile memory
- R: Non-volatile memory
- S: Non-writable memory

The correct match is

- (A)  $1 \rightarrow P, 2 \rightarrow Q, 3 \rightarrow S, 4 \rightarrow R$                       (B)  $1 \rightarrow P, 2 \rightarrow R, 3 \rightarrow Q, 4 \rightarrow S$   
 (C)  $1 \rightarrow S, 2 \rightarrow Q, 3 \rightarrow S, 4 \rightarrow P$                       (D)  $1 \rightarrow P, 2 \rightarrow Q, 3 \rightarrow S, 4 \rightarrow P$

Q.59 A base 12 number system is called duodecimal. It uses the symbols 0, 1, 2, ..., 9, A, and B, where A and B are the symbols used to represent 10 and 11 respectively. What is the duodecimal equivalent of the decimal number 1594?

- (A) A09                      (B) A0A                      (C) B0A                      (D) B0B

Q.60 A particular solution of the differential equation

$$\frac{d^2 y}{dx^2} - \frac{dy}{dx} = x e^x$$

is

- (A)  $-\frac{x^2}{2}e^x + (x-1)e^x$                       (B)  $-\frac{x^2}{2}e^{-x} + (x-1)e^{-x}$   
 (C)  $\frac{x^2}{2}e^x - (x-1)e^x$                       (D)  $\frac{x^2}{2}e^{-x} - (x-1)e^{-x}$

Q.61 The equation for the tangent plane to the surface  $2x^3y - xz^2 = -3$  at the point  $(1, -1, 1)$  is

- (A)  $7x - 2y + 2z = 11$                       (B)  $2x - 7y + 2z = 11$   
 (C)  $2x + 7y - 2z = 11$                       (D)  $7x + 2y - 2z = 11$

Q.62 The minimum distance from the origin to the plane  $x + 3y - z = 11$  in  $\mathbb{R}^3$  is  
 (A) 10 (B) 1 (C)  $\sqrt{11}$  (D) 11

Q.63 Let  $\sigma$  be a 6-cycle in  $S_{12}$ . Then  $\sigma^i$  is also 6-cycle if the value of  $i$  is  
 (A) 2 (B) 3 (C) 5 (D) 12

Q.64 The book entitled, 'The Discovery of India' was written by  
 (A) Abul Kalam Azad (B) Jawaharlal Nehru  
 (C) Rajendra Prasad (D) Sarvepalli Radhakrishnan

Q.65 Consider the following two lists:

- | List I                         | List II       |
|--------------------------------|---------------|
| 1: Functional programming      | P: C language |
| 2: Logical programming         | Q: Prolog     |
| 3: Procedural programming      | R: C++        |
| 4: Object oriented programming | S: Lisp       |

Which one of the following is correct match?

- (A)  $1 \rightarrow P, 2 \rightarrow Q, 3 \rightarrow S, 4 \rightarrow R$  (B)  $1 \rightarrow P, 2 \rightarrow Q, 3 \rightarrow R, 4 \rightarrow S$   
 (C)  $1 \rightarrow P, 2 \rightarrow R, 3 \rightarrow S, 4 \rightarrow Q$  (D)  $1 \rightarrow S, 2 \rightarrow Q, 3 \rightarrow P, 4 \rightarrow R$

Q.66 What is the octal equivalent of the hexadecimal number ABC?  
 (A) 5674 (B) 5314 (C) 5275 (D) 5274

Q.67 The fourth order linear differential equation having  $e^{-x}, xe^{-x}, \cos 2x, \sin 2x$  as solutions is

- (A)  $\frac{d^4 y}{dx^4} + 2\frac{d^3 y}{dx^3} + 5\frac{d^2 y}{dx^2} + 8\frac{dy}{dx} + 4y = 0$   
 (B)  $\frac{d^4 y}{dx^4} + 2\frac{d^3 y}{dx^3} + 8\frac{d^2 y}{dx^2} + 5\frac{dy}{dx} + 4y = 0$   
 (C)  $\frac{d^4 y}{dx^4} + 2\frac{d^3 y}{dx^3} + 3\frac{d^2 y}{dx^2} + 4\frac{dy}{dx} + 2y = 0$   
 (D)  $\frac{d^4 y}{dx^4} + 2\frac{d^3 y}{dx^3} + 4\frac{d^2 y}{dx^2} + 3\frac{dy}{dx} + 2y = 0$

Q.68 The probability of getting a total of 9 at least once in two tosses of a pair of fair dice is  
 (A)  $\frac{600}{729}$  (B)  $\frac{128}{729}$  (C)  $\frac{601}{729}$  (D)  $\frac{64}{81}$

- Q.69 If the matrix  $\begin{bmatrix} a & b \\ b & 2 \end{bmatrix}$  has eigenvalues 1 and 3, then the value of  $(a, b)$  is
- (A) (1,2)                      (B) (2,1)                      (C) (-1,2)                      (D) (-2,1)

- Q.70 The value of the integral  $\int_0^9 \frac{dy}{\sqrt{y}\sqrt{1+\sqrt{y}}}$  is
- (A) 4                      (B)  $4(\sqrt{10}-1)$                       (C) 8                      (D) 12

- Q.71 The truth table of a binary operator  $\odot$  is given below:

$x$	$y$	$x \odot y$
0	0	0
0	1	0
1	0	1
1	1	0

Which one of the following is equivalent to  $x \odot y$ ?

- (A)  $x'y'$                       (B)  $xy$                       (C)  $x'y$                       (D)  $xy'$
- Q.72 Suppose  $\vec{a} + \vec{b} = 2\hat{i} + 2\hat{j} + 3\hat{k}$ ,  $\vec{a} - \vec{b} = \hat{i} - 2\hat{j} + 3\hat{k}$  represent diagonals of a parallelogram whose sides are  $\vec{a}$  and  $\vec{b}$ . Then the area of the triangle formed by the sides  $\vec{a}, \vec{b}$  and  $\vec{a} + \vec{b}$  is

- (A)  $\frac{1}{4}\sqrt{189}$                       (B)  $\frac{1}{4}\sqrt{198}$                       (C)  $\frac{1}{4}\sqrt{179}$                       (D)  $\frac{1}{4}\sqrt{197}$

- Q.73 What is the characteristic equation of the T flip-flop, if Q and Q<sup>+</sup> denote the output during the current and next clock cycle?

- (A)  $Q^+ = T + Q$                       (B)  $Q^+ = T'Q' + TQ$   
 (C)  $Q^+ = TQ' + T'Q$                       (D)  $Q^+ = T' + Q'$

- Q.74 The integral  $\int_{-1}^1 f(x)dx$  where  $f$  is continuous on  $[-1,1]$ , is approximated by the formula

$$\int_{-1}^1 f(x)dx \approx \alpha f\left(-\frac{1}{\sqrt{2}}\right) + \beta f\left(\frac{1}{\sqrt{2}}\right).$$

Suppose the approximation is exact for all polynomials of degree  $\leq 1$ . Then the value of  $\alpha$  is

- (A) -1                      (B) 1                      (C)  $\frac{1}{\sqrt{2}}$                       (D)  $-\frac{1}{\sqrt{2}}$

Q.75 Let  $g(x) = \frac{1}{1-x+x^2}$  and  $a_0 + a_1x + a_2x^2 + a_3x^3 + \dots$  be the Taylor series of the function  $g$  around 0. Then the value of  $a_3$  is

- (A) 0                                      (B) 1                                      (C) -1                                      (D) 3

Q.76 Which of the following is/are forbidden input(s) for SR flip-flop?

P: S = 1, R = 1                                      Q: S = 0, R = 0

- (A) P only                                      (B) Q only                                      (C) both P and Q                                      (D) neither P nor Q

Q.77 The iteration formula

$$x_{n+1} = x_n - (\cos x_n)(\sin x_n) + R \cos x_n$$

where  $R$  is a positive constant, is used to find a real root of some function  $f(x)$ . What is  $f(x)$ , assuming the iteration method is convergent with an initial approximation  $x_0$ ?

- (A)  $\tan x - R$                                       (B)  $\cot x - R$                                       (C)  $\sin x - R$                                       (D)  $\cos x - R$

Q.78 The area of the surface generated by rotating the hypocycloid

$$x = a \cos^3 \theta, \quad y = a \sin^3 \theta, \quad 0 \leq \theta \leq \pi$$

about  $y$ -axis is

- (A)  $\frac{12}{5} \pi a^2$                                       (B)  $\frac{5}{12} \pi a^2$                                       (C)  $\frac{6}{5} \pi a^2$                                       (D)  $\frac{5}{6} \pi a^2$

Q.79 What is the output of a JK flip-flop during next clock cycle, when  $J = 1, K = 1$ ? Assume,  $Q$  is the output during the current clock cycle.

- (A) 1                                      (B) 0                                      (C)  $Q$                                       (D)  $Q'$

Q.80 What are the values of the variables  $i, j,$  and  $k$  after execution of the following program segment?

```
int i=1, j=2, k=3;
i += j += k;
```

- (A)  $i=3, j=5, k=6$                                       (B)  $i=3, j=6, k=5$   
 (C)  $i=6, j=3, k=5$                                       (D)  $i=6, j=5, k=3$

Q.81 What is the content of the array after execution of the following program segment?

```
int a[] = {1, 2, 3, 4}, i;
for (i=1; i<4; ++i) a[i] = a[i] + a[i-1];
```

- (A) {0, 1, 2, 3}                                      (B) {1, 2, 3, 4}  
 (C) {1, 3, 6, 10}                                      (D) {4, 3, 2, 1}

Q.82

The eigenvectors of the matrix  $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$  are

(A)  $\begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$

(B)  $\begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$

(C)  $\begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$

(D)  $\begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$

Q.83 Consider the following C function:

```
void fun2(int n) {
    while (n > 0) {
        printf("%d", n%10);
        n = n/10;
    }
}
```

What is the output of fun2 ( 475 )?

(A) 475

(B) 543

(C) 754

(D) 574

Q.84 Consider the following algorithm:

```
(1) for i = 1 to p do
(2)     for j = 1 to q do
(3)         for k = 1 to r do
(4)             c[i,j] = c[i,j] + a[i,k] * b[k,j];
```

How many times line (4) is executed?

(A) 3

(B) p + q + r

(C) pqr

(D) ijk

Q.85 Consider the following C function:

```
int fun1(int n) {
    int x=0;
    while (n > 1) {
        n = n/2;
        ++x;
    }
    return (x);
}
```

What is the return value of fun1(31)?

- (A) 3                      (B) 4                      (C) 5                      (D) 6

Q.86 Let  $A$  be a  $3 \times 3$  matrix whose sum of the diagonal elements is  $\frac{1}{2}$  and the determinant is  $-\frac{1}{2}$ .

If 1 is an eigenvalue of  $A$ , then the eigenvalues of  $(A^{-1})^2$  are

- (A) 1,1,4                      (B)  $\frac{1}{4}, 1, 1$                       (C) 1,1,2                      (D)  $\frac{1}{2}, 1, 1$

Q.87 Let  $S_1 = \{(x, y, z) \in \mathbb{R}^3 \mid x + y + z = 0\}$  and  $S_2 = \{(x, y, z) \in \mathbb{R}^3 \mid x^2 + y^2 - z^2 \leq 1\}$ . Then the set  $S_1 \cap S_2$  is

- (A) convex but not bounded.  
 (B) bounded but not convex.  
 (C) bounded and convex.  
 (D) neither bounded nor convex.

Q.88 The number of different Boolean functions with 3 inputs and 4 outputs is

- (A) 64                      (B) 127                      (C) 128                      (D) 144

Q.89 What is the output of the following program fragment?

```
int x = 123, y= -123, z=0;
if (x) { if (z) printf("aaa\n"); }
        else if (y) printf("bbb\n");
        else printf("ccc\n");
```

- (A) aaa                      (B) bbb                      (C) ccc                      (D) outputs nothing



Q.90 The solution of the following LPP

$$\begin{aligned} \text{Max } f &= x + 5y \\ \text{subject to} \\ 2x + y &\geq 10, \\ 4x + 3y &\leq 24, \\ y &\leq 2x, y \geq 0 \end{aligned}$$

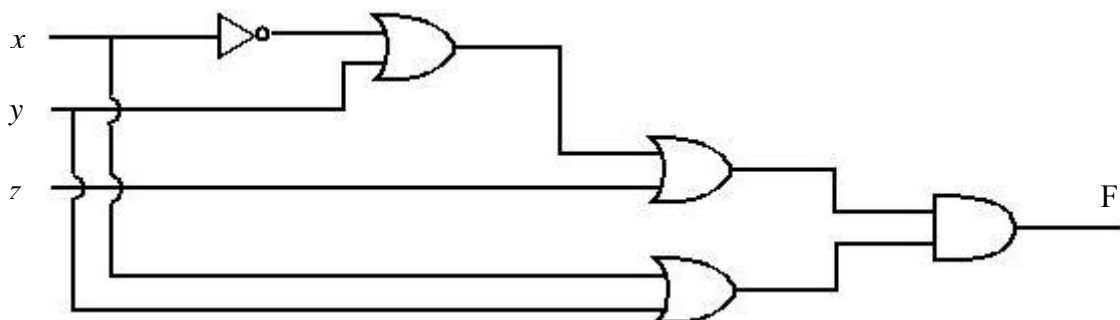
is

- (A) 27.5                      (B) 26.4                      (C) 23                      (D) 6

Q.91 Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be the function defined by  $f(x) = \begin{cases} x^2 & \text{if } x \in \mathbb{Q} \\ x & \text{if } x \notin \mathbb{Q} \end{cases}$ . Then the function  $f$  is

- (A) differentiable on  $\mathbb{R}$ .  
 (B) differentiable only at 0.  
 (C) differentiable only at 1.  
 (D) is continuous at 0 but NOT differentiable at 0.

Q.92 Consider the following logic circuit:



What is the output F?

- (A)  $x + yz$                       (B)  $y + xz$                       (C)  $z + xy$                       (D)  $x + y + z$

Q.93 Suppose  $\phi_1$  and  $\phi_2$  are two linearly independent solutions of the differential equation

$$\frac{d^2 y}{dx^2} + a_1 \frac{dy}{dx} + a_2 y = 0$$

where  $a_1$  and  $a_2$  are constants. Then  $\phi_1$  and  $\phi_2$  have

- (A) odd number of common zeros  
 (B) exactly one common zero  
 (C) no common zeros  
 (D) at most two common zeros

- Q.94 Which one is equivalent to  $xyz + xyz' + xy'z + xy'z'$ ?
- (A)  $x$                       (B)  $x'$                       (C)  $y + z$                       (D)  $yz$

Q.95 In the following segment of C program

```
int x;
scanf("%d",&x);
if(x&1)printf("%s",STAMENT);
```

**STAMENT** represents a missing string. Which one of the following is an appropriate string?

- (A) "x is a prime number"                      (B) "x is an even number"  
 (C) "x is an odd number"                      (D) "the value of x is 1"

Q.96 Let  $W_1 = \{(x, y, z, w) \in \mathbb{R}^4 \mid x + y + z = 0 \text{ and } 6x + 7y + 8z = 0\}$  and  $W_2 = \{(x, y, z, w) \in \mathbb{R}^4 \mid x + 2y + 3z = 0 \text{ and } 2x + 3y + 4z = 0\}$ . Then the dimension of the subspace  $W_1 + W_2$  is

- (A) 1                      (B) 2                      (C) 4                      (D) 3

Q.97 The composite Trapezoidal rule is used to compute  $\int_0^1 e^{-x} dx$  with an error of at most  $\frac{1}{12} \times 10^{-2}$ . How many points should be used?

- (A) 11                      (B) 9                      (C) 8                      (D) 7

Q.98 Consider the following C function:

```
float f(float x)
{ float sum=1.0,term=1.;
  int n=1;
  while(n<50)
  { term=x*term/n;
    sum+=term;
    n++;
  }
  return sum;
}
```

The return value of the function  $f(1.0)$  is the approximate value of

- (A) 0.0                      (B)  $\sin(1.0)$                       (C)  $\cos(1.0)$                       (D)  $e$

Q.99 The length of the one arc of the cycloid

$$x = a(t - \sin t), \quad y = a(1 - \cos t)$$

is

(A)  $8a$

(B)  $4a$

(C)  $4\sqrt{2} a$

(D)  $2\sqrt{2} a$

Q.100 Consider the following C function:

```
void f(int x,int y)
{ int d;
  if(x>0)
  { d=x%y;
    f(x/y,y);
    printf("%d",d);
  }
  else return;
}
```

The output for  $f(100,16)$  is

(A) 11

(B) 64

(C) 82

(D) 110

**End of the paper**



**SPACE FOR ROUGH WORK**



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