

BRILLIANT'S MOCK TEST 4 FOR STUDENTS OF OUR ONE/TWO-YEAR POSTAL COURSE TOWARDS BITSAT, 2008

Time: 3 Hours

Maximum Marks: 450

BITSAT 2008 MTP 4/QNS

Test Booklet Code

Read the following instructions carefully:

- 1. Immediately fill in the particulars on the Answer Book with Blue/Black Ball Point Pen.
- 2. The Answer Sheet is kept inside this Test Booklet. When you are directed to open the Test Booklet, take out the Answer Sheet and fill in the particulars carefully.
- 3. The candidate should write their Enrolment No. only in the space provided on the Test Booklet/Answer Sheet.
- **4.** For each correct response, the candidate will get 3 marks. For each incorrect response, one mark will be deducted from the total score. No deduction from the total score, however, will be made if no response is indicated for an item in the Answer Sheet.
- 5. The test is of 3 hours duration.
- 6. The test consists of 150 questions.
- 7. The maximum marks are 450.
- 8. Use Blue/Black Ball Point Pen only for writing particulars/marking responses on Side 1 and Side 2 of the Answer Sheet.
- 9. Rough work is to be done on the space provided for this purpose in the Test Booklet only.
- 10. Do not fold or make any stray marks on the Answer Sheet.
- 11. Use of Electronic/Manual Calculator is prohibited .

Name of the Candidate (in Capitals):

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PART I: MATHEMATICS

- 1. If $\vec{a} = \hat{i} + \hat{j} + \hat{k}$, $\vec{b} = 4\hat{i} + 3\hat{j} + 4\hat{k}$ and $\vec{c} = \hat{i} + \alpha\hat{j} + \beta\hat{k}$ are linearly dependent vectors and $|\vec{c}| = \sqrt{3}$, then
 - (1) $\alpha = 1, \beta = -1$
 - (2) $\alpha = 1, \beta = \pm 1$
 - (3) $\alpha = -1, \beta = \pm 1$
 - (4) $\alpha = \pm 1, \beta = 1$
- 2. Let $h(x) = f(x) (f(x))^2 + (f(x))^3$ for every real number x. Then
 - (1) h is increasing whenever f is increasing
 - (2) h is increasing whenever f is decreasing
 - (3) h is decreasing whenever f is increasing
 - (4) nothing can be said in general

- 3. Let n be an odd integer. If sin $n\theta = \sum_{r=0}^{n} b_{r} \sin^{r}\theta$, for every value of θ , then (1) $b_{0} = 1$, $b_{1} = 3$ (2) $b_{0} = 0$, $b_{1} = n$ (3) $b_{0} = -1$, $b_{1} = n$ (4) $b_{0} = 0$, $b_{1} = n^{2} - 3n + 3$ 4. Number of divisors of the form $4n + 2(n \ge 0)$ of the integer 240 is
 - **(1)** 4 **(2)** 8 **(3)** 10 **(4)** 3
- 5. Let $h(x) = min \{x, x^2\}$, for every real number of x. Then
 - (1) h is not continuous
 - (2) h is differentiable for all x
 - (3) h'(x) = 0 for all x > 1
 - (4) h is not differentiable at two values of x

SPACE FOR ROUGH WORK

- 6. If in a triangle PQR, sin P, sin Q, sin R are in A.P., then
 - (1) the altitudes are in A.P.
 - (1) the altitudes are in H.P.
 - (3) the medians are in G.P.
 - (4) the medians are in A.P.

7. If
$$f(x) = \frac{x^2 - 1}{x^2 + 1}$$
, for every real number x,

then the minimum value of f

- (1) does not exist because f is unbounded
- (2) is not attained even though f is bounded
- (3) is equal to 1
- (4) is equal to 1
- 8. Seven white balls and three black balls are randomly placed in a row. The probability that no two black balls are placed adjacently equals

(1)
$$\frac{1}{2}$$
 (2) $\frac{7}{15}$ (3) $\frac{2}{15}$ (4) $\frac{1}{3}$

9. If
$$a_n = \sum_{r=0}^{n} \frac{1}{r_{C_r}}$$
, then $\sum_{r=0}^{n} \frac{r}{r_{C_r}}$ equals
(1) $(n-1) a_n$
(2) na_n
(3) $\frac{1}{2} n a_n$
(4) None of the above
10. The number of common tangents to the circles $x^2 + y^2 = 4$ and $x^2 + y^2 - 6x - 8y = 24$ is
(1) 0 (2) 1 (3) 3 (4) 4
11. If ω is an imaginary cube root of unity, then $(1 + \omega - \omega^2)^7$ equals
(1) 128ω (2) $- 128 \omega$
(3) $128 \omega^2$ (4) $- 128 \omega^2$
12. If $\int_{0}^{x} f(t) dt = x + \int_{0}^{1} t f(t) dt$, then the

(1) $\frac{1}{2}$ (2) 0 (3) 1 (4) $-\frac{1}{2}$

SPACE FOR ROUGH WORK

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13. If P(1, 2), Q(4, 6), R(5, 7) and S(a, b) are the vertices of a parallelogram PQRS, then

(1) a = 2, b = 4
(2) a = 3, b = 4
(3) a = 2, b = 3
(4) a = 3, b = 0

14. For three vectors \vec{u} , \vec{v} , \vec{w} which of the following expressions is not equal to any of the remaining three?

(1)
$$\vec{u} \cdot (\vec{v} \times \vec{w})$$
 (2) $(\vec{v} \times \vec{w}) \cdot \vec{u}$
(3) $\vec{v} \cdot (\vec{u} \times \vec{w})$ (4) $(\vec{u} \times \vec{v}) \cdot \vec{w}$

- **15.** If f(x) = 3x 5, then $f^{-1}(x)$
 - (1) is given by $\frac{1}{3x-5}$
 - (2) is given by $\frac{x+5}{3}$
 - (3) does not exist because f is not oneone
 - (4) does not exist because f is not onto
- 16. If from each of the three boxes containing 3 white and 1 black, 2 white and 2 black, 1 white and 3 black balls, one ball is drawn at random, then the

probability that 2 white and 1 black ball will be drawn is

(1)
$$\frac{13}{32}$$
 (2) $\frac{1}{4}$ (3) $\frac{1}{32}$ (4) $\frac{3}{16}$

17. Let T_r be the rth term of an A.P., for r = 1, 2, 3, . . . If for some positive integers m, n, we have $T_m = \frac{1}{n}$, $T_n = \frac{1}{m}$, then T_{mn} equals

(1)
$$\frac{1}{mn}$$
 (2) $\frac{1}{m} + \frac{1}{m}$

(4) 0

- **18.** If g (f(x)) = | sin x | and f(g(x)) = $(sin \sqrt{x})^2$, then
 - (1) $f(x) = \sin^2 x, g(x) = \sqrt{x}$
 - (2) $f(x) = \sin x, g(x) = |x|$
 - (3) $f(x) = x^2$, $g(x) = \sin \sqrt{x}$
 - (4) f and g cannot be determined

19. If $\begin{vmatrix} 6i & -3i & 1 \\ 4 & 3i & -1 \\ 20 & 3 & i \end{vmatrix} = x + iy$, ther (1) x = 3, y = 1 (2) x = 1, y = 3 **(3)** x = 0, y = 3 **(4)** x = 0, y = 0

20. An n-digit number is a positive number with exactly n digits. Nine hundred distinct n-digit numbers are to be formed using only the three digits 2, 5 and 7. The smallest value of n for which this is possible is

- **21.** If \overline{E} and \overline{F} are the complementary events of events E and F respectively and if 0 < P(F) < 1, then
 - (1) $P(E | F) + P(\overline{E} | F) = 1$
 - (2) $P(E | F) + P(E | \overline{F}) = 1$
 - (3) $P(\overline{E} | F) + P(E | \overline{F}) = 1$
 - (4) $P(E | F) + P(\overline{E} | \overline{F}) = 1$

22. Let f(x) = x - (x), for every real number x, where (x) is the integral part of x. Then 1

$$\int_{-1}^{1} f(x) dx is$$

(1) 1

(2) 2 (3) 0 (4) $\frac{1}{2}$

- 23. It the circle $x^2 + y^2 = a^2$ intersects the hyperbola $xy = c^2$ in four points P(x₁, y₁), Q(x₂, y₂), R(x₃, y₃), S(x₄, y₄), then which of the following is not true?

(1)
$$x_1 + x_2 + x_3 + x_4 = 0$$

(2)
$$y_1 + y_2 + y_3 + y_4 = 1$$

(3)
$$x_1 x_2 x_3 x_4 = c^4$$

(4)
$$y_1 y_2 y_3 y_4 = c^4$$

-

24. There are four machines and it is known that exactly two of them are faulty. They are tested, one by one, in a random order till both the faulty machines are identified. Then the probability that only two tests are needed is

(1)
$$\frac{1}{3}$$
 (2) $\frac{1}{6}$ (3) $\frac{1}{2}$ (4) $\frac{1}{4}$

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SPACE FOR ROUGH WORK

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25. The value of the sum $\sum_{n=1}^{13} (i^n + i^{n+1})$, where $i = \sqrt{-1}$ equals

(1) i (2) i – 1 (3) – i (4) O

26. Which of the following expressions are meaningful?

(1)
$$\vec{u} \cdot (\vec{v} \times \vec{w})$$
 (2) $(\vec{u} \times \vec{v}) \cdot \vec{w}$
(3) $(\vec{u} \cdot \vec{v}) \times \vec{w}$ (4) $\vec{u} \times (\vec{v} \cdot \vec{w})$

- **27.** If E and F are events with $P(E) \le P(F)$ and $P(E \cap F) > 0$, then
 - (1) occurrence of $E \Rightarrow$ occurrence of F
 - (2) occurrence of $F \Rightarrow$ occurrence of E
 - (3) non-occurrence of E \Rightarrow non-occurrence of F
 - (4) none of the above implications holds
- 28. A fair coin is tossed repeatedly. If tail appears on first four tosses, then the probability of head appearing on fifth toss equals

(1)
$$\frac{1}{2}$$
 (2) $\frac{1}{32}$ (3) $\frac{31}{32}$ (4) $\frac{1}{5}$

29. The number of values of c such that the straight line y = 4x + c touches the curve $\frac{x^2}{4} + y^2 = 1$ is

(1) 0 (2) 1 (3) 2 (4) infinite

30. The order of the differential equation whose general solution is given by $y = (C_1 + C_2) \cos (x + C_3) + C_4 e^{(x + C_5)}$ where C_1, C_2, C_3, C_4, C_5 are arbitrary constants, is

(1) 5 **(2)** 4 **(3)** 3 **(4)** 2

- **31.** The diagonals of a parallelogram PQRS are along the lines x + 3y = 4 and 6x 2y = 7. Then PQRS will be a
 - (1) rectangle
 - (2) square
 - (3) cyclic quadrilateral
 - (4) rhombus
- **32.** In a college of 300 students, every students reads 5 news papers and every news paper is read by 60 students. Then the number of news papers is

- (1) at least 30
- (2) at most 20
- (3) exactly 25
- (4) none of the above
- 33. Let A₀ A₁ A₂ A₃ A₄ A₅ be a regular hexagon inscribed in a circle of unit radius. Then the product of the line segments A₀ A₁, A₀ A₂ and A₀ A₄ is

(1)
$$\frac{3}{4}$$
 (2) $3\sqrt{3}$ (3) 3 (4) $\frac{3\sqrt{3}}{2}$

34. If P = (x, y), $F_1 = (3, 0)$, $F_2 = (-3, 0)$ and $16x^2 + 25y^2 = 400$, then $PF_1 + PF_2$ equals

(1) 8 **(2)** 6 **(3)** 10 **(4)** 12

35. The number of values of x where the function $f(x) = \cos x + \cos (\sqrt{2}x)$ attains its maximum is

(1) 0 (2) 1 (3) 2 (4) infinite

- **36.** $\lim_{x \to 1} \frac{\sqrt{1 \cos 2(x 1)}}{x 1}$
 - (1) exists and it equals $\sqrt{2}$
 - (2) exists and it equals $-\sqrt{2}$

- (3) does not exist because $x 1 \rightarrow 0$
- (4) does not exist because left hand limit is not equal to right hand limit.

37. If
$$x > 1$$
, $y > 1$, $z > 1$ are in G.P., then

$$\frac{1}{1 + \ln x}, \frac{1}{1 + \ln y}, \frac{1}{1 + \ln z}$$
 are in

- (1) A.P.
- (2) H.P.
- (3) G.P.
- (4) None of the above
- **38.** The number of values of x in the interval I 0, 5π I satisfying the equation $3\sin^2 x 7\sin x + 2 = 0$ is
 - **(1)** 0 **(2)** 5 **(3)** 6 **(4)** 10
- **39.** If the vertices P, Q, R of a triangle PQR are rational points, which of the following point of the triangle PQR may not be a rational point?

(1) Centroid (2) Incentre

(3) Circumcentre (4) Orthocentre

(A rational point is a point both of whose co-ordinates are rational numbers.)

SPACE FOR ROUGH WORK

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- **40.** Which of the following number (s) is/are rational?
- rational? (1) sin 15° (2) cos 15°

(3) sin 15° cos 15° (4) sin 15° cos 75°

- **41.** $\int_{0}^{\pi^{2}} \sin \sqrt{x} \, dx =$ **(1)** π **(2)** 2π **(3)** $2\pi^{2}$ **(4)** π^{2}
- 42. For the ellipse $3x^2 + 4y^2 = 5$, if y + 3x = 0 is one diameter, the conjugate diameter is (Note: Two diameters of an ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ are said to be conjugate

when each bisects all chords parallel to the other).

4x = 0

(1) 4y - x = 0 (2) 4y + x = 0

(3)
$$y - 4x = 0$$
 (4) $y +$

43. A solution of the differential equation $p^2y + p(x - y) - x = 0$ is

(1) $x^2 - y^2 = c$ (2) $y^2 = 2x + c$

- **(3)** y = x + c **(4)** $x^2 + y^2 = c^2$
- **44.** In the binomial expansion $(a b)^n$, $n \ge 5$, the sum of the 5th and 6th terms is zero. Then $\frac{nb - 5a}{b} =$

(1) 14 **(2)** 7 **(3)** 4 **(4)** 1

45. Equation of the plane containing the line $\frac{x-3}{2} = \frac{y-4}{3} = \frac{z-\xi}{4}$ is (1) 4x + 4y - 5z = 3(2) 2x + 3y - 4z + 5 = 0(3) 4x + 6y + 8z + 13 = 0(4) x + 2y + z = 0

SPACE FOR ROUGH WORK

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PART II: PHYSICS

- **46.** For a short wave radio link between two stations via the ionosphere, the ratio of the maximum usable frequency to the critical frequency
 - (1) is always less than 1
 - (2) is always greater than 1
 - (3) may be $\frac{<}{>}$ 1 depending on the distance between the two stations
 - (4) does not depend on the distance between the two stations
- **47.** A plane electromagnetic wave travelling along the + z-direction, has its electric field given by

 $E_x = 2 \cos(\omega t)$ and

 $E_v = 2 \cos(\omega t + 90^\circ)$

The wave is

- (1) linearly polarised
- (2) right circularly polarised
- (3) left circularly polarised
- (4) elliptically polarised

- **48.** It is proposed to increase the Q of a coil. This can be done best by
 - (1) operating at low frequency.
 - (2) increasing the diameter of wire.
 - (3) increasing the diameter of coil.
 - (4) adding a core of magnetic material in compressed powder form.
- 49. In Compton effect, photons of wavelength λ and frequency υ scatter at angle φ with modified wavelength λ' and frequency υ' which of the following is true?
 - (1) $\lambda' \lambda$ varies with ϕ and also with the scatter
 - (2) $\upsilon-\upsilon'$ is independent of the scattering material
 - (3) $\lambda' \lambda$ varies with ϕ in proportion to $(1 + \cos \phi)$
 - (4) $\lambda' \lambda$ is independent of the scatterer but varies with ϕ



(2) ⊺≜

50. In a laser source the emission from various

53. In the circuit shown, X, Y are inputs and Z is the output. The values of inputs for which the output Z = 0 are



- **(1)** X = 0, Y = 0
- **(2)** X = 0, Y = 1
- (3) X = 1, Y = 1
- (4) X = 1, Y = 0
- **54.** The frequency f_v of the Lissajous figure is



(1)
$$f_y = 1.5 f_x$$
 (2) $f_y = 2f_x$
(3) $f_y = f_x$ (4) $f_t = 3f_x$

- **55.** A satellite in a stable orbit contains two closed vessels; one of these is filled with hot steam and the other with water.
 - (i) The water exerts very little pressure on its container.
 - (ii) The steam exerts almost the same pressure as it would on Earth.
 - (iii) The water exerts the same pressure as it would on Earth.
 - (iv) The steam exerts very little pressure on its container.
 - (1) (i) and (ii) are correct
 - (2) (iii) and (iv) are correct
 - (3) only (ii) is correct
 - (4) All but (i) are correct
- **56.** If the impedances of the series and parallel combination of the coil with its internal resistance are equal then

R_s L_s

SPACE FOR ROUGH WORK



57. A solid right-circular cylinder is placed on a rough plane of inclination α to the horizontal. The least coefficient of friction between the cylinder and the plane so that the cylinder rolls down (without sliding) is

(1)
$$\tan \alpha$$
 (2) $\sin \alpha$
(3) $\frac{1}{3} \tan \alpha$ (4) $\frac{3}{2} \tan \alpha$

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- **58.** A capacitor remains connected to a battery and a dielectric slab is slipped between the plates. The energy will increase due to
 - (1) increase of potential difference
 - (2) increase of electric field strength
 - (3) increase of capacitance
 - (4) none of the above
- **59.** When an electron in a hydrogen atom moves from an orbit to another orbit of longer radius, which of the following decreases?
 - (1) potential energy
 - (2) total energy
 - (3) angular momentum
 - (4) rotational speed
- **60.** Newton's law of cooling can be deduced from
 - (1) Wien's displacement law
 - (2) Stefan-Boltzmann law
 - (3) The law of equipartition of energy

(4) Joule-Thomson effect

- **61.** The probability of electrons being captured by the nucleus is maximum for
 - (1) K shell electrons
 - (2) L shell electrons
 - (3) M shell electrons
 - (4) same for all shells
- 62. In a plane transmission grating



a = b, then

- (1) the second order spectrum will be absent
- (2) first order spectrum will be absent
- (3) spectra up to third order can be obtained
- (4) no spectrum will be obtained

- 63. In the de Broglie hypothesis, waves are
 - (1) associated with particle at rest
 - (2) associated with a particle in motion
 - (3) associated with a medium
 - (4) not at all involved
- 64. In Rutherford's scattering formula, the scattering cross section for angle θ is proportional to

(1)
$$\sin^4\left(\frac{\theta}{2}\right)$$

(2) $\sin^{-4}\left(\frac{\theta}{2}\right)$
(3) $\sin^2\left(\frac{\theta}{2}\right)\cos^2\left(\frac{\theta}{2}\right)$
(4) $\cot^4\left(\frac{\theta}{2}\right)$

65. A p-type silicon sample has conductivity compared to an n-type sample having the same dopant concentration

(1) higher	(2) zero
(3) infinite	(4) less

SPACE FOR ROUGH WORK

- **66.** Silicon is not suitable for fabrication of light emitting diodes because it is
 - (1) an indirect band gap semiconductor
 - (2) a direct band gap semiconductor
 - (3) a wide band gap semicoductor
 - (4) a narrow band gap semiconductor
- **67.** Match the waveforms and the form factors (FFs).



Codes

	А	В	С	D
(1)	1	2	3	4
(2)	3	4	2	1
(3)	3	4	1	2
(4)	4	3	2	1

- **68.** Consider the following statements on negative feedback.
 - (i) It reduces the gain
 - (ii) It enhances noise and distortion
 - (iii) It decreases the input impedance
 - (iv) It increases the bandwidth

Choose the correct statements from above:

- (1) (i), (iii) and (iv) (2) (i) and (iv)
- (3) (ii) and (iii) (4) only (iv)
- **69.** In a transofrmer if the transfer of energy occurs at the same voltage, then the transformer is
 - (1) current transformer
 - (2) potential transformer
 - (3) isolating transformer
 - (4) step-up transformer

SPACE FOR ROUGH WORK

70. In post office box, the graph of galvanometer deflection versus resistance R (pulled out of resistance box) for the ratio 100 : 1 is given as shown (due to unsuitable values of R, galvanometer shows deflection). The two consecutive values of R are shown in the **Figure**:



The value of unknown resistance would be

- **(1)** 3.2 Ω **(2)** 3.24 Ω
- (3) 3.206 Ω (4) 3.2375 Ω
- 71. Given two statements for resonance tube method:
 - S1: Lower frequency tuning fork will require large tube to obtain two successive resonance positions.
 - S2: Higher frequency fork gives resonance positions for relatively small length of air column.

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- (1) S_1 only true (2) S_2 only true
- (3) Both S_1 , S_2 are true
- (4) Neither S_1 nor S_2 is true
- **72.** A 100 MHz carrier wave is frequency modulated by a 10 kHz signal. The peak frequency deviation is 60 kHz

	Column I		Column II
(a)	Maximum carrier frequency (MHz)	(i)	99.94
(b)	Minimum carrier frequency (MHz)	(ii)	6
(C)	Frequency swing (kHz)	(iii)	120
(d)	Modulation index (rad)	(iv)	100.06
Then	match them		
(1) (a-iv) (b-i) (c-iii) (d-ii)		
(2) (a-i) (b-ii) (c-iii) (d-iv)		
(3) (a-ii) (b-iii) (c-iv) (d-i)		
(4) (a-iii) (b-iv) (c-ii) (d-i)		

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- 73. In the measurement of three quantities A, B, C it is stated as A = 2 ± 0.005, B = 1 ± 0.001, C = 4 ± 0.01. Then, the percentage error in P = $\frac{A}{B}$ is
 - (1) ± 0.35 (2) ± 0.6
 - **(3)** ± 1.05 **(4)** ± 0.7
- **74.** Given two statements about a faulty physical balance:
 - **S**₁: If the masses of the left and right pans are m₁ and m₂ and if M₁ and M₂ are measured masses of a block placed successively in left and right pan then actual mass is $M = \sqrt{M_1 M_2}$.
 - **S**₂: If ℓ_1 and ℓ_2 are lengths of left and right arm of the balance, then

$$M = \frac{M_1 + M_2}{2}$$

- (1) only S_1 is correct
- (2) only S_2 is correct

- (3) both $\rm S_1$ and $\rm S_2$ are correct
- (4) neither S_1 nor S_2 is correct
- **75.** Which of the following has 3 significant figures?
 - **(1)** 15.7 **(2)** 1040
 - (3) 1.57 (4) all of above
- **76.** Which of the following relations correctly represent the work done under the indicator diagram shown?



(1)
$$W_P > W_Q > W_R > W_S$$

(2)
$$W_Q > W_R > W_P > W_S$$

(3) $W_{P} < W_{Q} > W_{R} > W_{S}$

(4)
$$W_{\Omega} > W_{R} > W_{P} < W_{S}$$

- 77. Induction furnace is based on the heating effect of
 - (1) magnetic field
 - (2) eddy current
 - (3) electric field
 - (4) electrostatic field
- 78. Match the following.

Column I Column II (a) The current (i) The collector gain of a BJT doping will be concentration increased if is increased (ii) The base width (b) The current gain of a BJT is reduced gain of a BJT will be reduced if (iii) The emitter (c) The breakdown doping concentration to voltage of a BJT will be base doping reduced if concentration ratio is reduced

- (iv) The base doping concentration is increased keeping the ratio of the emitter doping concentration to base doping concentration constant
- (1) (a-i) (b-iii) (c-i)
- (2) (a-ii) (b-iii) (c-i)
- (3) (a-iii) (b-i) (c-ii)
- (4) (a-ii) (b-ii) (c-iii)
- **79.** During a negative β -decay
 - (1) an electron which is already present within the nucleus is ejected
 - (2) a neutron in the nucleus decays emitting an electron
 - (3) a part of the binding energy of the nucleus is converted into an electron
 - (4) an atomic electron is ejected

80. An audio signal given by 15 sin 2π (2000 t) amplitude modulates a sinusoidal carrier wave 60 sin 2π (100,000) t. The modulation index is

(1) 1 **(2)** 0.25 **(3)** 0.5 **(4)** 0.33

81. A force of $\vec{F} = 3\hat{i} + c\hat{j} + 2\hat{k}$ acting on a particle causes a displacement of $\vec{s} = -4\hat{i} + 2\hat{j} + 3\hat{k}$ in its own direction. If the work done is $6\hat{j}$, then the value of c is

(1) 0 **(2)** 1 **(3)** 6 **(4)** 12

82. Two rods each of mass m and length l are joined at centre to form a cross. The moment of inertia of this cross about an axis passing through the common centre of the rods and perpendicular to the plane formed by them, is

(1)
$$\frac{m\ell^2}{12}$$
 (2) $\frac{m\ell^2}{6}$
(3) $\frac{m\ell^2}{3}$ (4) $\frac{m\ell^2}{2}$

83. A uniform cube is subjected to volume compression. If each side is increased by 0.01%, then bulk strain is

(1) 0.01 **(2)** 0.06 **(3)** 0.02 **(4)** 0.03

84. Shown are 3 lens systems



All curved surfaces have same radii of curvature. The equivalent focal lengths are in ratio $f_a : f_b : f_c$ as

(1) 1 : 2 : 3	(2) 3 : 2 : 1
(3) 1 : 1 : 1	(4) 2 : 1 : 1

- 85. A silver voltmeter of resistance 2 Ω and a 3 Ω resistor are connected in series across a cell. If a resistance of 2 Ω is connected in parallel with the silver voltmeter, then the rate of deposition of silver will
 - (1) decrease by 37.5%
 - (2) decrease by 73%
 - (3) increase by 50%
 - (4) decrease by 50%

PART III: CHEMISTRY

- **86.** Which of the following statement is wrong?
 - (1) Two p-orbitals always overlap laterally.
 - (2) A sigma bond has no free rotation around its axis.
 - (3) There can be more than one sigma bond between two atoms.
 - (4) All of these.
- **87.** The compound having a tetrahedral geometry is

(1)
$$\left[Ni(CN)_{4} \right]^{-2}$$
 (2) $\left[Pd(CN)_{4} \right]^{-2}$
(3) $\left[PdCl_{4} \right]^{-2}$ (4) $\left[NiCl_{4} \right]^{-2}$

- **88.** At its boiling point, a liquid is in equilibrium with its vapours. On an average, the molecules in the two phases have equal
 - (1) kinetic energies
 - (2) potential energies

- (3) intermolecular forces
- (4) total energies
- **89.** The terminal velocity of a small sized spherical body of radius 'r' falling vertically in a viscous liquid varies with

(1)
$$\frac{1}{r^2}$$
 (2) $\frac{1}{r}$ (3) r (4) r^2

90. Zinc and aluminium metals produces hydrogen gas with dilute H_2SO_4 . The ratio of moles of H_2 produced when 1 mole of each reacts with excess dilute H_2SO_4 will be

(1) 1 : 1.5 **(2)** 3 : 1 **(3)** 1 : 3 **(4)** 1 : 2

91. For the redox reaction

(3) 5, 16, 2

 $xMnO_{4}^{-1} + yC_{2}O_{4}^{-2} + zH^{+} \longrightarrow$ $Mn^{+2} + CO_{2} + H_{2}O, \text{ the correct stoichio-metric coefficients } x, y \text{ and } z \text{ are respectively}$ (1) 2, 5, 16 (2) 16, 5, 2

(4) 2, 16, 5

- **92.** For a reaction to be spontaneous at all temperatures
 - (1) ΔG and ΔH should be negative
 - (2) $\Delta G = \Delta H = 0$
 - (3) ΔG and ΔH should be positive
 - **(4)** ΔG = ΔH
- **93.** Which of the following is correct for the equilibrium of the following reaction?

 $C_{(graphite)} + H_2O_{(g)} \longrightarrow CO_{(g)} + H_{2(g)}$

- (1) $pH_2 \propto pH_2O$
- (2) $pH_2 \propto \sqrt{pH_2O}$
- (3) $pH_2 \propto p^2 H_2 O$
- (4) $pH_2 \propto p^2 H_2O/pCO$.
- **94.** The chemical reaction, $2O_{3(g)} \longrightarrow 3O_{2(g)}$ proceeds as given below
 - $O_{3(g)} \rightleftharpoons O_{2(g)} + (O)$ fast,

 $2(O) + O_2 \longrightarrow 2O_{2(Q)}$ slow.

The rate law expression is

- (1) rate = $k[O_3]^2$
- (2) rate = $k[O_3]^2 [O_2]^+$
- (3) rate = $k[O_3][O_2]$
- (4) rate = $k[O_3]^{-2}$
- **95.** Which one is zero order reaction among the following?
 - (1) $CH_3COOC_2H_5 \xrightarrow{H^+} CH_3COOH + CH_3CH_2OH$
 - (2) $C_{12} H_{22} O_{11(aq)} \xrightarrow{H^+} Glucose$ + Fructose
 - (3) $CH_3COOC_2H_5 + NaOH \longrightarrow CH_3COONa + CH_3CH_2OH$
 - (4) $NH_{3(g)} \xrightarrow{Au} N_{2(g)} + 3H_{2(g)}$
- **96.** The oxidation numbers of oxygen in KO_2 , OF_2 , H_2O_2 are respectively
 - **(1)** − 2, − 2, − 2
 - **(2)** + 2, 1, + 1
 - **(3)** 1/2, + 2, 1
 - **(4)** -1, +2, +1

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- **97.** Among the following anions, the strongest Bronsted base is
 - (1) CIO^{-1} (2) CIO_{2}^{-2}

(3) CIO_3^{-1}

- 98. Which is a false statement?
 - (1) Work is a state function.
 - (2) Work appears at the boundary of the system.

(4) CIO⁻¹

- (3) Temperature is a state function.
- (4) Enthalpy is an extensive property.
- **99.** Which of the following statements is wrong for a zero order reaction?
 - (1) The rate is independent of the concentration of the reactants.
 - (2) The half-life of the reaction depends on the concentrations of the reactants.
 - (3) The rate is independent of the temperature of the reaction.
 - (4) The rate constant has the unit of $mol^{-1} s^{-1}$.

- 100. In the following galvanic cell, (m = concentration (1 m))
 - (1) cations migrate to the cathode and are reduced on the cathode surface.
 - (2) anions migrate to the cathode and are reduced on the anode.
 - (3) Zn and Cu dissolved as a result of reaction.
 - (4) Zn^{+2} and Cu^{+2} ions react with each other to give complex ions.
- 101. The cause of Brownian movement is due to
 - (1) heat change in liquid state.
 - (2) convectional current.
 - (3) the collision of the molecules of the dispersion medium with dispersed particles.
 - (4) the attractive forces between the colloidal particles and molecules of the dispersion medium.
- **102.** In a body-centred cubic packing of equal sized spheres, the maximum radius of a sphere that can fit into the void is

(1) 0.154 R	(2) 0.225 R
(3) 0.414 R	(4) 0.747 R

103. An inorganic substance liberates $O_{2(g)}$ on heating, turns acidified $KI_{(aq)}$ to brown colour solution and decolorise acidified KMnO₄ solution. The substance may be

(1) $K_2 CrO_4$ (2) H_2O_2

- (3) Cl₂ (4) KClO₃
- **104.** When borax $(Na_2B_4O_7)$ dissolved in water,
 - (1) only $B(OH)_3$ is formed.
 - (2) only $\left[B(OH)_4\right]^-$ is formed.
 - (3) both $B(OH)_3$ and $\left[B(OH)_4\right]^-$ are formed.
 - (4) both $B(OH)_3$ and B_2O_3 are formed.
- 105. The carbon atoms in diamond are bonded to each other in
 - (1) a linear configuration
 - (2) a planar configuration
 - (3) an octahedral configuration
 - (4) a tetrahedral configuration

- **106.** Which of the following statements is wrong?
 - (1) The molecular formula of tetramethyl silane is $(CH_3)_4$ SiH₄.
 - SiCl₄ undergoes hydrolysis due to the presence of empty d-orbitals in Si.
 - (3) Fluorosilicic acid (H_2SiF_6) is a strong acid, exist only in solution.
 - (4) The octahedral SiF_6^{-2} ion is the only halogen complex of silicon which involves sp^3d^2 hybridisation.
- **107.** Which of the following statements is correct?
 - (1) N_2O_5 solid exist as $NO_2^+ NO_3^-$ (nitronium nitrate).
 - (2) The nitronium ion (NO_2^+) is isoelectronic with CO_2 and are isostructural (V shape).
 - (3) The nitrate ion $\left(NO_{3}^{-}\right)$ has a T-shaped structure.
 - (4) The NO_2^- ion has a pyramidal structure.

108. The metallic sulphide with highest solubility product value (K_{sp}) in water at 278 K is

(1) PbS (2) CuS (3) Ag₂S (4) ZnS

- **109.** A greenish yellow poisonous gas reacts with alkali metal hydroxide to form a halate $\left[XO_3^{-}\right]$ which is used in firework and safety matches. The gas and the halate respectively are
 - (1) Br_2 and $KBrO_3$
 - (2) Cl_2 and $KClO_3$

(3) I_2 and KIO_3

(4) Cl_2 and $KClO_4$

- **110.** The XeF_6 molecule is
 - (1) tetrahedral with one lone pair of electrons.
 - (2) octahedral with one lone pair of electrons.
 - (3) capped octahedral with one lone pair of electrons.
 - (4) capped octahedral with two lone pair of electrons.

- Hypo solution is used in photography for fusing films. Its function is to undecomposed
 - (1) remove the the reduced silver metal by forming a soluble complex.
 - (2) remove the undecomposed AgBr by forming a soluble complex.
 - (3) remove bromine forming a soluble salt.
 - (4) decompose AgBr to metal Ag and bromine.
- 112. Calcium cyanamide is produced by heating
 - (1) calcium carbide in an electric furnace in nitrogen atmosphere at 1100°C.
 - (2) quick lime with nitrogen at 1000°C.
 - (3) gypsum with coke and nitrogen in electric furnace.
 - (4) limestone with NH_3 and coke at 2000°C.

- **113.** ZnSO₄ on boiling with NaHCO₃ solution produces
 - (1) ZnCO₃

(2) Zn(OH)₂

(3) $ZnCO_3 \cdot Zn(OH)_2$

(4) $Na_2 ZnO_2$

- 114. Which of the following statements is wrong?
 - (1) Lead salts are poisonous to living system.
 - (2) Metal lead is used in lead accumulation.
 - (3) Lead is corroded by water in presence of dissolved oxygen is known as plumbo solvency.
 - (4) Lead is a good conductor of electricity.
- 115. Stainless steel contains
 - (1) Fe, Cr, Ni, C (2) Fe, Al
 - (3) Fe, Mn, Cr (4) Fe, Co, Ni

- **116.** The IUPAC name of $\left[CO(NH_3)_6\right]\left[Cr(CN)_6\right]$ is
 - (1) hexaamminecobalt (III), hexacyanochromium (VI)
 - (2) hexaamminecobalt (III), hexacyanochromate (III)
 - (3) hexacyanochromium (III), hexaamminecobalt (III)
 - (4) hexacyanochromium cobalt hexaammine (VI)
- 117. The IUPAC name of the insecticide represented by the structural formula



- (1) dichloro diphenyl trichloroethane
- (2) trichloromethyl-bis-(4-chlorophenyl) methane
- (3) 1, 1, 1-trichloro-2, 2-bis-(4-chlorophenyl) ethane
- (4) 2, 2, 2-trichloro-1, 1-bis-(4-chlorophenyl) ethane

- **118.** Ethylenedichloride and ethylidene dichloride are
 - (1) geometrical isomers
 - (2) nuclear isomers
 - (3) position isomers
 - (4) anomers
- 119. The products of the following reaction A, B and C are respectively

$$C \xleftarrow{AgCN} CH_3 - CH_2I \xrightarrow{alc. KOH} A$$

$$\downarrow (1) CH_3ONa$$

$$\downarrow (2) \Delta$$
B

- (1) CH_3CH_2OH , $CH_3CH_2 O CH_3$, CH_3CH_2CN
- (2) CH_3CH_2OH , CH_3CH_2COONa , CH_3CH_2NC
- (3) $CH_2 = CH_2$, $CH_3CH_2 O CH_3$, CH_3CH_2NC
- (4) $CH = CH, CH_3CH_2OCH_3, CH_3CH_2CN$

120. The products A, B and C of the following reactions are respectively

$$C \xleftarrow{SOCI_2} CH_3COOH \xrightarrow{\text{LiAIH}_4} A$$

$$\downarrow Br_2/\text{Red P}$$
B

- (1) CH_3OH , $CH_2BrCOOH$, $CH_2CICOOH$
- (2) CH₃CH₂OH, CH₂BrCOOH, CH₃COCI
- (3) CH₃CH₂OH, CH₃COBr, CH₃COCI
- (4) CH₃OH, CH₂BrCOOH, CH₃COCI
- 121. The products A, B and C of the following reactions are respectively

$$C \xleftarrow{Br_2/KOH} CH_3CONH_2 \xrightarrow{P_2O_5} A$$
$$\downarrow HNO_2$$
B

- (1) CH_3CN , CH_3COOH , CH_3NH_2
- (2) $CH_3COOH, CH_3COOH, CH_3NH_2$
- (3) CH₃CN, CH₃OH, CH₃NH₂
- (4) CH₃CN, CH₃CH₂OH, CH₃NH₂

122. The products A, B and C of the following reactions are respectively



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- 123. Match the List I with List II and select the correct answers from the codes given below the list:
- 124. Match the List I with List II and select the correct answers using the codes given below the list:

List II

P. CCI₃NO₂

S. C₆H₆Cl₆

Q. $Na_2(Na_4(PO_3)_6)$

T. Barbituric acid derivatives

	Lis	st I		List II		List I					
A.	Insect	ticide	Ρ.	OH			Α.	Pyren	e	Ρ.	CCI3
				$\widehat{\bigcirc}$			В.	Calgo	n	Q.	Na ₂ (N
				\bigcirc			C.	Chlore	opicrin	R.	CCI_4
В.	Germ	icide	Q.	C ₁₇ H ₃₅ COOI	Na		D.	Hypno	otic	S.	C6H6
C.	Misce	lle	R.	AgNO3						Τ.	Barbit
D.	Lyoph	nobic	S.	C ₆ H ₆ Cl ₆							derivo
	SOI		т		Ч		Coo	des			
Coc	des		1.	Colloidal goi	G			А	В	С	D
	^	D	~	D			(1)	R	Q	Т	Р
	A	В	C	D			(2)	S	D	6	Þ
(1)	S	Т	Q	Р			(2)	0	ĸ	Q	
(2)	S	Р	Q	Т			(3)	R	Q	Ρ	Т
(3)	S	R	Q	Р			(4)	S	Q	Т	Р
(0)	-	-	- -								
(4)	Р	S	Q	R							

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125.	Matc corre	h the List I w ct answer f	ith Li rom	st II and select the the codes given	С	oc	les	
	belov	v the list:		0			A	В
		List I		List II	(1)	Ρ	S
		(Test for)		(Observation)	(2)	S	R
	Α.	Phenol	Ρ.	evolution of NH ₃ with hot alkali	(3)	S	Т
	Β.	Mono- carboxylic acid	Q.	evolution of H ₂ with Grignard reagent	(4)	S	Ρ
	C.	Amide	R.	evolution of H ₂ with zinc				
	D.	Acidic hydrogen	S.	purple colour with neutral				

FeCl₃ T. effervescence with hot aqueous NaHCO₃

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С

Т

Ρ

Ρ

Т

D

Q

Q

Q

Q

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PART IV: ENGLISH PROFICIENCY AND LOGICAL REASONING

(a) ENGLISH PROFICIENCY

Directions for questions 126 to 128: Read the following passage carefully and answer the questions that follow.

The young are those to whom we look for future strength and for future good; and the longer we live, the more anxious we become that they who are to be the fresh recruits should be morally of right stature. Around them are peculiar temptations and trials, witching, cunning, insidious and forceful and we are obliged to see thousands falling by the way, whose fall seems and needless. They like ourselves, are to have but one chance in life. We who are somewhat advanced in years, seeing how many perils there are round about that one chance, feel an earnest desire that every advantage should be given to those who are coming onto fill our places. We can live but once, and life is usually moulded and takes its shape very early.

- **126.** Which one of the following is correct? The author looks upon the young as
 - (1) handsome and healthy.
 - (2) an embodiment of possibilities.

- (3) strong and hard working.
- (4) a group of boys and girls who are obedient and dutiful.
- **127.** What does the phrase "morally of right stature" mean?
 - (1) Being highly educated
 - (2) Having a good personality
 - (3) Having rectitude
 - (4) Feeling superior to others
- 128. Which one of the following is correct? The failure of many a young men and women is
 - (1) well deserved
 - (2) unwarranted
 - (3) fortuitous
 - (4) sad

Directions for questions 129 to 133: Each question below has a word capitalised followed by four words or phrases numbered 1 to 4. Choose the word that has nearly the same meaning as the capitalised word.

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129.	USURP		Direction for questions 134 to 136: Each of the				
	(1) to be lazy		follow usage	ving sentence has a mistake in grammar e or idiom. Each sentence is broken up			
	(2) to climb		into Choc	four parts sequentially 1, 2, 3 and 4.			
	(3) to seize power	or position illegally	acco	ordingly.			
	(4) to yield		134.	(1) The carpet was badly stained			
130.	MERCURIAL			(2) to such an extent			
	(1) mechanical	(2) heavy		(3) that you could n't tell			
	(3) clownish	(4) quick-changing					
131.	ALLEVIATE			(4) Its original colour			
	(1) to release	(2) to lessen	135.	(1) It is greatly to tom's credit			
	(3) to deprive	(4) to deceive		(2) that he gave back			
132.	EXTENUATE			(3) the money he found			
	(1) to lessen in deg	gree		(4) his honesty does for him credit			
	(2) to express		136.	(1) A terrific hue and crv			
	(3) suggest						
	(4) object			(2) was raised			
133.	RECTITUDE			(3) at the new tax proposals			
	(1) refuse	(2) integrity		(4) no error			
	(3) reaching out	(4) revenge					

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sente that each the w	nce below has a bl something has bee sentence four word ord that makes the s	ank space indicating en left out. Following ds are given. Choose sentence meaningful.		valu cons are of b	e only in terr sequence and the sole test o eliefs.	ms of their practical that practical results of the truth or validity
137.	In the 20 th cent made their greate the characteristi objects like the ato	ury, physicists have est discoveries about cs of om and its parts.		(1) r (3) p	əalist oragmatist	(2) optimist (4) utopian
	(1) infinitesimal	(2) infinite			(b) LOGICAL	REASONING
138.	 (3) microscopic His moral decade his from and honesty. (1) declivity (3) opprobrium 	 (4) kaleidoscope nce was marked by the ways of integrity (2) obsession (4) departure 	Direct the fo certai follow the p relatio	ions bllow n re ed b bair bnship	for questions to ing questions lationship bet by four pairs nu wherein the poto the origina	41 to 144: In each of a pair of words with ween them is given mbered 1 to 4. Select words have closest al pair.
Direct	tions for questions	39 and 140: In each	141.	EDU	CATION : DEVE	ELOPMENT ::
of th alterr	e following question natives given, choos	ons, out of the four e the one which can		(1)	/lan : Speech	(2) Nutrition : Health
be sul	ostituted for the giver	n words or sentence.		(3) 🤅	Game : Play	(4) Child : Growth
139.	A person, such a officer etc., who be strict discipline.	as a teacher, army lieves in and enforces	142.	HOU	ISE : ROOM ::	(2) Iransport - Car
	(1) maudlin	(2) martinet		(1) 0		
	(3) maverick	(4) malthusian		(3) S	chool : College	e (4) Boy : Girl

31 Directions for questions 137 and 138: Each | 140. A person who believes that ideas have

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- 143. GILL : FIN ::
 - (1) Salad : Rice
 - (2) Sea : Fish
 - (3) Kill : Bomb
 - (4) Question : Team
- 144. BREAK : PIECE ::
 - (1) Writer : Pen
 - (2) Bread : Bake
 - (3) Kick : Football
 - (4) Muddy: Unclear

Directions for questions 145 to 147: In each question you find a set of sentences arranged in a haphazard way. Choose the correct arrangement of sentences as indicated by the number to make a coherent paragraph.

- 145. A. Indian films, cuisine and yoga have always been popular in China.
 - B. 33 year old Jin Shan Shan, a Jawaharlal University alumnus is actively promoting Bharatnatyam among her compatriots.
 - C. She has established a school for Bharatnatyam in China.
 - D. It has always been a passion for her to become an exponent of Bharatnatyam.

- E. Around 50 Chinese children attend classes every week to learn the intricacies of the classical dance.
- F. Now classical Indian dance has caught the imagination of the Chinese.
- (1) AFBDCE (2) ECDFBA
- (3) ABFDCE (4) EDCBFA
- **146.** A. Our leaders decided to move towards progress through five year plans.
 - B. In the years that followed Independence, India had to tackle many problems.
 - C. We have decided to be a democracy and we have continued to remain so.
 - D. This path was laid down in the constitution we gave ourselves.
 - E. Sixty years have gone by and we have grown as a nation in many ways.
 - F. Leaders like Nehru and Ambedkar set the course our country was to take.
 - (1) EFDCBA (2) BEACDF
 - (3) BEDAFC (4) BDEACF

- 147. A. However, there may be times when enforcement of norms and limits leads to conflicts.
 - B. Norms and limits help children learn mutual respect, responsibility and cooperation.
 - C. Conflict resolution tools which can be used include decision-making, communication skills, managing aggressive behaviour and forgiveness.
 - D. Therefore, we need to understand conflicts and learn how to resolve them effectively.
 - E. Understanding conflicts is important when trying to comprehend concepts of positive discipline and physical and psychological punishment.
 - F. Conflict is a part of everybody's life.
 - (1) EFDCAB (2) CBDFEA
 - (3) DACFBE (4) BADCFE

Direction for question 148: In the following question, four out of the five alternatives are similar and form a group. Find the odd one that does not belong to the group.

- 148. (1) Rectangle
 - (2) Rhombus
 - (3) Square
 - (4) Circle
 - (5) Trapezium

Direction for question 149: Select the figure which does not belong to the group.



150. Choose the figure from the five alternatives 1, 2, 3, 4 and 5 that can be formed by joining the figures given in box marked (X).





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BITSAT 2008 MTP 4/SOLNS

MOCK TEST 4 FOR STUDENTS OF OUR ONE/TWO-YEAR POSTAL COURSE TOWARDS BITSAT, 2008

BRILLIANT'S

SOLUTIONS

PART I: MATHEMATICS

1. (4) $|\vec{c}| = \sqrt{3} \Rightarrow 1 + \alpha^2 + \beta^2 = 3$ $\Rightarrow \alpha^2 + \beta^2 = 2$ $\vec{a}, \vec{b}, \vec{c}$ are linearly dependent $\Rightarrow \vec{c} = x\vec{a} + y\vec{b}$ $\Rightarrow \hat{i} + \alpha \hat{j} + \beta \vec{k}$ $= x(\vec{i} + \vec{j} + \vec{k}) + y(4\vec{i} + 3\vec{j} + 4\vec{k})$ x + 4y = 1 $x + 3y = \alpha$ $x + 4y = \beta$ $\Rightarrow \beta = 1 \text{ and } \alpha^2 = 2 - \beta^2 = 2 - 1 = 1$ $\alpha = \pm 1$ 2. (1) $h(x) = y - y^2 + y^3$ where y = f(x) $\frac{dh}{dy} = 3y^2 - 2y + 1$ $= 3\left(y - \frac{1}{3}\right)^2 + \frac{2}{3} > 0$ \therefore h increases with y or h is increasing whenever f(x) is increasing or equivalently h is decreasing whenever f(x) is decreasing.

3. (2) $\sin \theta = \text{Imaginary part of}$ $(\cos \theta + i \sin \theta)^n$

$$= {}^{n}C_{1} \cos^{n-1} \theta \sin \theta$$
$$- {}^{n}C_{3} \cos^{n-3} \theta \sin^{3} \theta + \dots$$
$$= n (1 - \sin^{2} \theta)^{\frac{n-1}{2}} \sin \theta$$
$${}^{n}C_{3}(1 - \sin^{2} \theta)^{\frac{n-3}{2}} \sin^{3} \theta + \dots$$
$$= n \sin \theta + \alpha \sin^{3} \theta + b \sin^{5} \theta + \dots$$
$$= b_{0} + b_{1} \sin \theta + b_{2} \sin^{2} \theta + \dots$$
Comparison gives $b_{0} = 0$ and $b_{1} = n$

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4. (1) $240 = 2^4 \times 3 \times 5$

Factors of 240 are the terms of $(1 + 2 + 2^2 + 2^3 + 2^4)$ (1 + 3) (1 + 5) 4n + 2 = 2 $(2n + 1) = 2 \times$ odd number. Such factors are 2×1 , 2×3 , 2×5 , 2×15

These are four in number.

5. (4) $h(x) = min \{x, x^2\}$ for all x implies

$$h(x) = \begin{cases} x & \text{for } -\infty < x \le 0 \\ x^2 & \text{for } 0 \le x \le 1 \\ x & \text{for } 1 \le x < \infty \end{cases}$$

h(x) is continuous at 0 and 1 and hence for all x.

h(x) is not differentiable at x = 0and at x = 1



$$h'(0-) = 1$$
 and $h'(0+) = 0$
 $h'(1-) = 2$ and $h'(1+) = 1$
Also $h'(x) = 1$ for all $x > 1$

6. (2) If the sides of the Δ are p, q, r then sin P, sin Q, sin R are in A.P \Rightarrow p, q, r are in A.P. (since p \approx sin P etc.)

$$\Rightarrow \frac{\Delta}{PD}, \frac{\Delta}{QE}, \frac{\Delta}{RF} \text{ are in A.P.}$$
since $\frac{1}{2}p \cdot PD = \frac{1}{2}q \cdot QE$

$$= \frac{1}{2}r \cdot RF = \Delta$$

$$\Rightarrow \frac{1}{PD}, \frac{1}{QE}, \frac{1}{RF} \text{ are in A.P.}$$

$$\Rightarrow \text{ altitudes are in H.P.}$$

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7. (4)
$$f(x) = \frac{x^2 - 1}{x^2 + 1} = 1 - \frac{2}{x^2 + 1}$$
$$\min f(x) \longleftrightarrow \max \frac{2}{x^2 + 1} \longrightarrow$$

min $(x^2 + 1)$ which corresponds to x = 0

 \therefore minimum f(x) = -1

8. (2) First arrange the seven white (all different) balls in a row in $\lfloor 7 \\$ ways and then arrange the three black balls in 8 (6 interspaces plus two outside spaces) in ${}^{8}P_{3}$ ways

$$=\frac{LZ \times {}^{8}p_{3}}{|10} = \frac{7}{15}$$

9. (3) It is given that

р

$$\alpha_{n} = \frac{1}{nC_{0}} + \frac{1}{nC_{1}} + \dots + \frac{1}{nC_{n}}$$
Let $S = \sum_{r=0}^{n} \frac{r}{nC_{r}}$

$$= \frac{0}{nC_{0}} + \frac{1}{nC_{1}} + \frac{2}{nC_{2}}$$

$$+ \dots + \frac{n}{nC_{n}}$$

$$= \frac{n}{nC_{0}} + \frac{n-1}{nC_{1}} + \frac{n-2}{nC_{2}}$$

$$+ \dots + \frac{0}{nC_{n}}$$

$$2S = \frac{n}{nC_{0}} + \frac{n}{nC_{1}} + \dots + \frac{n}{nC_{r}}$$

$$\Rightarrow S = \frac{n}{2} \cdot \alpha_{n}$$

10. (2) $x^2 + y^2 = 2^2$ and $(x - 3)^2 + (y - 4)^2 = 7^2$ touch internally, $d = r_1 - r_2 = 5$

Number of common tangents = 1

11. (4)
$$(1 + \omega - \omega^2)^7 = (-2\omega^2)^7 = -128 \omega^{14}$$

= $-128 \omega^2$

12. (1)
$$\int_{0}^{x} f(t) dt = x + \int_{x}^{1} t f(t) dt$$

Differentiating w.r.t.x by Leibnitz rule 1 {f(x)} = 1 - {xf(x)} 1

:
$$f(x) = \frac{1}{1 + x}$$
 and $f(1) = \frac{1}{2}$

13. (3) Equating slopes of PQ and RS, $\frac{b-7}{a-5} = \frac{4}{3} \text{ or } 4a - 3b = -1.$ Equating slopes of PS and RQ, $\frac{b-2}{a-1} = \frac{1}{1} \text{ or } a - b = -1$ $\therefore a = 2 \text{ and } b = 3$

- 14. (3) A, B, D are all equal as they represent box product $[\overline{u} \ \overline{v} \ \overline{w}]$ whereas $c \rightarrow \overline{v} \cdot (\overline{u} \times \overline{w}) = -[\overline{u} \ \overline{v} \ \overline{w}]$
- **15. (2)** Let y = 3x 5; Then $x = \frac{y + 5}{3}$; Interchanging x and y, we get $y = \frac{x + 5}{3} \therefore f^{-1}(x) = \frac{x + 5}{3}$
- 16. (1) Case I ; W W B $p_1 = \frac{3}{4} \times \frac{2}{4} \times \frac{3}{4}$ Case II ; W B W $p_2 = \frac{3}{4} \times \frac{2}{4} \times \frac{1}{4}$

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Case III ; B W W $p_{3} = \frac{1}{4} \times \frac{2}{4} \times \frac{1}{4}$ $\therefore p = p_{1} + p_{2} + p_{3} = \frac{26}{64} = \frac{13}{32}$ 17. (3) $T_{n} = \frac{1}{m} \Rightarrow \frac{1}{m} = a + (n - 1) c$ $T_{m} = \frac{1}{n} \Rightarrow \frac{1}{n} = a + (m - 1) c$ Solving $a = \frac{1}{mn}$ and $d = \frac{1}{mn}$ $\therefore T_{mn} = a + (mn - 1) d$ $= \frac{1}{mn} + (mn - 1) \frac{1}{mn} = 1$ 18. (1) If f(x) = sin² x and g(x) = \sqrt{x} $f(g(x)) = f(\sqrt{x}) = (sin \sqrt{x})^{2}$

$$g(f(x)) = g(sin^2 x) = \sqrt{sin^2 x} = |sin x|$$

3 and 2 do not fit, on verification.

19. (4)
$$\begin{vmatrix} 6i & -3i & 1 \\ 4 & 3i & -1 \\ 20 & 3 & i \end{vmatrix} = \begin{vmatrix} 6i + 4 & 0 & 0 \\ 4 & 3i & -1 \\ 20 & 3 & i \end{vmatrix}$$

= (6i + 4) (3i² + 3) = 0
∴ x + iy = 0 ⇒ x = 0, y = 0

20. (2) Each digit can be any one of 2, 5, 7, thus each digit can have 3 values. Hence there are 3^n , distinct n digit numbers. $3^n > 900 \Rightarrow n \ge 7$ since, $3^6 = 729$.

BITSAT/MTP 4/Obj/Solns - 3

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21. (1)
$$(F \cap E) \cup (F \cap \overline{E}) = F \cap (E \cup \overline{E}) = F \cap X = F$$

Also $F \cap E$ and $F \cap \overline{E}$ are disjoint.

$$\therefore P(F \cap E) + P(F \cap \overline{E}) = P(F)$$

$$\therefore \frac{P(F \cap E)}{P(F)} + \frac{P(F \cap \overline{E})}{P(F)} = 1$$

(i.e.) $P\left(\frac{E}{F}\right) + P\left(\frac{\overline{E}}{F}\right) = 1$

Similar result is true if F is replaced bv F.

= x - 0 = x in (0, 1)

22. (1) If
$$f(x) = x - (x)$$

then $f(x) = x - (-1) = x + 1$ in $(-1, 0)$

$$\therefore \int_{-1}^{1} f(x) dx = \int_{-1}^{0} (x + 1) dx + \int_{0}^{1} x dx$$

$$= \left[\frac{x^{2}}{2} + x\right]_{-1}^{0} + \left[\frac{x^{2}}{2}\right]_{0}^{1} = 1$$

23. (2) Any point on $xy = c^2 is\left(ct, \frac{c}{t}\right)$

Point of intersection are given by $c^{2}t^{2} + \frac{c^{2}}{c} - c^{2}$

$${}^{2}t^{2} + \frac{c}{t^{2}} = a$$

$$c^{2} t^{4} - a^{2} t^{2} + c^{2} = 0$$
 with roots t_{1} , t_{2}
 t_{3} , t_{4}

$$\therefore \ \Sigma t_1 = 0, \ \Sigma t_1 t_2 = - \ \alpha^2; \ \Sigma t_1 t_2 t_3 = 0; \\ t_1 t_2 t_3 t_4 = 1$$

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 $\therefore \Sigma x_1 = c\Sigma t_1 = 0$ $\sum y_{1} = c \sum \frac{1}{t_{1}} = \frac{c}{t_{1}t_{2}t_{3}t_{4}} \sum t_{1}t_{2}t_{3} = 0$ $x_1x_2x_3x_4 = c^4 \cdot t_1t_2t_3t_4 = c^4$ $y_1 y_2 y_3 y_4 = \frac{c^4}{t_1 t_2 t_3 t_4} = c^4$

24. (2) Since only two tests are needed, one faulty machine should be caught in the first test and the other one in the second test

$$\therefore p = \frac{2}{4} \times \frac{1}{3} = \frac{1}{6}$$

25. (2)
$$\sum_{n=1}^{13} i^{n} + \sum_{n=1}^{13} i^{n+1}$$
$$= \frac{i(1-i^{13})}{1-i} + \frac{i^{2}(1-i^{13})}{1-i}$$
$$= \frac{(i+i^{2})(1-i)}{(1-i)} = -1 +$$

- **26.** (1) $\overline{u} \cdot (\overline{v} \times \overline{w})$ is meaningful.
- 27. (4) The first three choices demand either $E \subset F$ or $F \subset E$ which are not implied by $P(E) \leq P(F)$ and $P(E \cap F) > 0$
- 28. (1) Each toss is independent of the earlier tosses and hence the probability of "head" appearance in the fifth toss = $\frac{1}{2}$
- 29. (3) y = mx + c touches the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ if $c = \pm \sqrt{a^2 m^2 + b^2}$.

This is only a numerical example.

30. (3) $y = A \cos (x + B) + Ce^{x}$ where $C_{1} + C_{2}$ = A and $C_{4} e^{C_{5}} = C$. Thus there are only three arbitrary constants and hence the differential equation will be of 3rd order.

$$y' = -A \sin (x + B) + Ce^{x}$$

$$y'' = -A \cos (x + B) + Ce^{x}$$

$$y''' = A \sin (x + B) + Ce^{x}$$

$$\therefore \frac{y + y''}{y' + y'''} = \frac{2Ce^{x}}{2Ce^{x}} = 1$$

or y''' - y'' + y' - y = 0 is the differential equation.

31. (4) Slope of $PR \times slope$ of QS

$$= -\frac{1}{3} \times \frac{6}{2} = -1$$

Diagonals are at right angles \Rightarrow parallelogram is a rhombus.

32. (3) Number of newspapers

$$=\frac{300\times5}{60}=25$$

33. (3)
$$A_{1}A_{0}A_{2} = 30^{\circ}$$
$$\therefore A_{0}A_{2} = 2 \cdot 1 \cdot \cos 30^{\circ} = \sqrt{3}$$
$$A_{4}A_{3}$$
$$A_{5}A_{4}A_{3}$$
$$A_{5}A_{1}A_{2}$$

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$$A_0 A_4 = A_0 A_2 = \sqrt{3}$$

$$\therefore (A_0 A_1) (A_0 A_2) (A_0 A_4)$$

$$= 1 \cdot (\sqrt{3}) (\sqrt{3}) = 3$$

34. (3)
$$\frac{x^2}{25} + \frac{y^2}{16} = 1$$
 is the ellipse with $a = 5$,
 $b = 4$, $e = \frac{3}{5}$
 $\therefore ae = 3$
 $\therefore (3, 0) \text{ and } (-3, 0) \text{ are the foci.}$
 $\therefore PF_1 + PF_2 = 2a = 10$

35. (2) $f(x) = \cos x + \cos (\sqrt{2} x)$ attains its maximum value 2 when x = 0; If $x = 2\pi$ or any even multiple of π , $\sqrt{2} x = 2\sqrt{2} n\pi$ and $\cos (2\sqrt{2} n\pi) \neq 1$. Similarly, if $\sqrt{2}x = 2m\pi$, $x = \sqrt{2}m\pi$ and $\cos x \neq 1$. The only value of x for which f(x) is maximum is x = 0.

36. (4)
$$\lim_{x \to 1} \frac{\sqrt{1 - \cos 2(x - 1)}}{x - 1}$$
$$= \lim_{y \to 0} \frac{\sqrt{2 \sin^2 y}}{y}$$
$$= \lim_{y \to 0} \frac{\sqrt{2} |\sin y|}{y}$$
$$= \begin{cases} \sqrt{2} |\sin y| \\ -\sqrt{2} |\sin y \to 0 + \\ -\sqrt{2} |\sin y \to 0 - \end{cases}$$

Hence the left hand and right hand limits are unequal and therefore limit does not exist.

37. (2) x, y, z in G.P.

$$\Rightarrow y^{2} = xz$$

$$\Rightarrow 2 \log y = \log x + \log z.$$

$$\Rightarrow \ln x, \ln y, \ln z \text{ are in A.P.}$$

$$\Rightarrow 1 + \ln x, 1 + \ln y, 1 + \ln z \text{ are in A.P.}$$

$$\Rightarrow \text{ their reciprocals are in H.P.}$$

38. (3)
$$3\sin^2 x - 7\sin x + 2 = 0$$

 $\Rightarrow (3\sin x - 1)(\sin x - 2) = 0$
 $\Rightarrow \sin x = \frac{1}{3}$ only. Hence $x = \alpha$
 $= \sin^{-1} \frac{1}{3}; \pi - \alpha, 2\pi + \alpha, 3\pi - \alpha,$
 $4\pi + \alpha, 5\pi - \alpha,$ satisfy $\sin x = \frac{1}{3};$ six values.

39. (2) (i) Centroid =
$$\left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$$
 is a rational point.

(ii) Equations of altitudes will contain only rational coefficient and hence the orthocentre will also be a rational point.

(iii) Similar argument gives the circumcentre to be a rational point.

(iv) The length of the sides a, b, c may not be rational and hence the incentre may not be a rational point.

40. (3) $\sin 15^{\circ} \cos 15^{\circ} = \frac{1}{2} \sin 30^{\circ} = \frac{1}{4}$.

The other three are
sin 15° =
$$\frac{\sqrt{3}-1}{2\sqrt{2}}$$
, cos 15° = $\frac{\sqrt{3}+1}{2\sqrt{2}}$

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and sin $15^{\circ} \cdot \cos 75^{\circ} = \sin^2 15^{\circ}$

$$=\left(\frac{\sqrt{3}-1}{2\sqrt{2}}\right)^2 = \frac{2-\sqrt{2}}{4}$$

are irrational.

41. (2)
$$\int_{0}^{\pi^{2}} \sin \sqrt{x} \, dx = \int_{t=0}^{\pi} 2t \, \text{sint } dt,$$

by putting $x = t^{2}$

$$= 2 \left\{ t(-\cos t) \right\}_{0}^{\pi} - \int_{0}^{\pi} (-\cos t) (+1) dt$$
$$= 2 \left[\pi + (\sin t)_{0}^{\pi} \right] = 2\pi$$

42. (1)
$$\frac{x^2}{\frac{5}{3}} + \frac{y^2}{\frac{5}{4}} = 1$$

$$m_0 = -3, m_1 m_0 = -\frac{b^2}{a^2}$$

$$\Rightarrow m_1 = -\frac{b^2}{a^2 m_0} = -\frac{\frac{5}{4}}{\left(\frac{5}{3}\right)(-3)}$$
$$= \frac{1}{4}.$$

Hence the equations of the conjugate diameter is $y = \frac{1}{4}x$.

i.e.,
$$4y - x = 0$$

43. (4)
$$p^2y + p(x - y) - x = 0$$

$$\Rightarrow p = \frac{y - x \pm \sqrt{(x - y)^{2} + 4xy}}{2y}$$

$$= \frac{y - x \pm (x + y)}{2y} = 1 \text{ or } -\frac{x}{y}$$

If $\frac{dy}{dx} = -\frac{x}{y}$, then $x \, dx + y \, dy = 0$
 $\Rightarrow x^2 + y^2 = c^2$
44. (3) $T_5 + T_6 = 0$
 $\Rightarrow {}^{n}C_4 a^{n-4} b^4 - {}^{n}C_5 a^{n-5} b^5 = 0$

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$$\Rightarrow a^{n-5}b^4 \left\{ \frac{n(n-1)(n-2)(n-3)}{24} \right\}$$
$$\left\{ a - \frac{(n-4)b}{5} \right\} = 0$$
$$\Rightarrow 5a - nb + 4b = 0$$
$$\Rightarrow \frac{nb - 5a}{b} = 4$$

45. (1) (3, 4, 5) satisfies 4x + 4y - 5z = 3 and $(2, 3, 4) \cdot (4, 4, -5) = 0$.

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and $m_1 + M_2 = m_2 + M$... (ii)

where M is the actual mass of the block.

Subtracting equation (ii) from (i), we get, $M - M_2 = M_1 - M$

or M =
$$\frac{M_1 + M_2}{2}$$

For S₂: Unequal Lengths of Arm

Let ℓ_1 and ℓ_2 be the lengths of the left and right arm of the physical balance. If M_1 and M_2 are the measured mass of the block, which is successively placed in the left and right pans of the balance, then from the condition of equilibrium, we get

$$\ell_1 M = \ell_2 M_1$$
 ... (iii)

and
$$\ell_1 M_2 = \ell_2 M$$
 ... (iv)

where M is the actual mass of the block.

Dividing equation (iii) and (iv), we get

$$\frac{M}{M_2} = \frac{M_1}{M}$$
$$M = \sqrt{M_1 M_2}$$

75. (4)

76. (2)

77. (2)

78. (2)

79. (2)

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80. (2)
$$m = \frac{E_m}{E_s} = \frac{15}{60} = 0.25$$

81. (3) $W = \vec{F} \cdot \vec{S}$
 $\Rightarrow 6 = (3\hat{i} + c\hat{j} + 2\hat{k}) \cdot (-4\hat{i} + 2\hat{j} + 3\hat{k})$
 $\Rightarrow 6 = -12 + 2c + 6$
 $\Rightarrow c = 6$

82. (2)

83. (4)
$$V = L^3$$

 $\frac{\Delta V}{V} \times 100 = \frac{3\Delta L}{L} \times 100$
 $\Rightarrow \frac{\Delta V}{V} = 0.03\%$

84. (3) f_p = focal length of each planoconvex lens

$$\frac{1}{F_{a}} = \frac{1}{f_{p}} + \frac{1}{f_{p}}$$
$$\Rightarrow F_{a} = \frac{f_{p}}{2}$$
Similarly, $F_{b} = \frac{f_{p}}{2}$, $F_{c} = \frac{f_{p}}{2}$

85. (1) I =
$$\frac{E}{2+3} = \frac{E}{5}$$
 amp
m = ZIt = $\frac{EZ}{5}$ gm/s, where Z Ω is
included so,
effective resistance = $\frac{2 \times 2}{2+2} + 3 = 4 \Omega$
 \Rightarrow I' = $\frac{E}{4} \Rightarrow$ m' = $\frac{ZE}{8}$ gm/s
 $\Delta m = \frac{m-m'}{m} = \frac{300 \times 5}{40}$

= 37.5% (decrease)



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		PART IV: ENGLISH PROFICIENC	Y AN	ID LO	DGICAL REASONING
		(a) ENGLISH PROFICIENCY	138. 139.	(4) (2)	
126.	(3)		140.	(3)	
127.	(3)				(b) LOGICAL REASONING
128. 129.	(3)		141.	(2)	Nutrition is a cause for health.
130.	(4)		142.	(2)	Car is a part of transport system.
131.	(2)		143	(1)	Salad and rice are part of food.
132.	(1)		144.	(3)	'kick' is an action that makes the football move.
133.	(2)		145.	(1)	
134.	(1)	'The carpet was stained' in place of 'The carpet was badly stained.	146.	(1)	
135.	(4)	'his honesty did him credit' in	147.	(4)	
		place of 'his honesty does for him credit'	148.	(4)	
136	(1)	(A highlight and ch') in place of $(A$	149.	(2)	All other figures can be rotated
150.	(I)	terrific hue and cry'.	150		inio each oiner.
137.	(3)		150.	(3)	

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