

MODEL SOLUTIONS TO IIT JEE 2009 Paper I

PART I

1	2	3	4	5	6	7	8	
B	В	С	Α	B	Α	D	B	
	9	10		11		12		
B	, C	C, D		A, C,	D	A, I)	
	-							
	13	14	15	16	17	18		
	D	С	B	B	Α	В		
أغبره		9			20)		
	A – p,	q, r, t	Γ.	A	<u> </u>	q, s, t		
	B – q,	, r, s, t			B –	s, t	1	
	C – p), q, r	. 1		C –	р	C .	
	D – p,	q, r, s			D -	ere 🗸		
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Section I

1. Atomic mas

s of Fe
=
$$\frac{(54 \times 5) + (56 \times 90) + (57 \times 5)}{100}$$

= 55.95

- 2. $\frac{an^2}{v^2}$ is the term that corrects for the attractive forces present in a real gas in the van der Waals equation.
- Sb₂S₃ sol is negatively charged.
 ∴ The most effective coagulating agent among the given is Al₂(SO₄)₃ due to the highest charge on the cation (Al³⁺).
- 4. $\begin{aligned} P_2 &= Kx_2 \\ & 5 \times 0.8 \text{ atm} = 1 \times 10^5 \text{ atm} \times x_2 \\ & x_2 &= 4 \times 10^{-5} \\ & \text{Mole fraction of } N_2 \text{ dissolved in 10 moles of } \\ & \text{water} = 4 \times 10^{-5} \times 10 \\ & = 4 \times 10^{-4} \end{aligned}$

- P_4O_6 is formed when P_4 is burnt in a limited supply of air. O_2 diluted with N_2 produces that condition.
- Carboxylic acids are more acidic than phenols. Presence of electron donating groups such as –CH₃ group decreases the acid strength of carboxylic acids. Presence of electron withdrawing group such as –Cl increases the acid strength of phenol.
- 7. Natural rubber is an elastomer. The intermolecular force of attraction is the weakest for elastomers.
- 8. -CN group has higher priority over -OH and -Br which are given in alphabetical order.

Section II

9. Frenkel defect is favoured by a large difference in sizes of cation and anion. It is a dislocation

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effect. Trapping of electrons in lattice sites leads to the formation of F-centres. Schottky defects have effect on the physical properties of solids.

- 10. [Pt(en)₂Cl₂]Cl₂ and Pt(NH₃)₂Cl₂ exhibit geometrical isomerism.
- 11. In excess of air Na₂O is not formed only Na₂O₂ is formed. Small amounts of NaO2 is also formed which is responsible for the yellow colour of commercial Na₂O₂. Pure Na₂O₂ is colourless. Air always contains varying amounts of moisture which produces small amounts of NaOH.
- 12. (A) Total number of stereo isomers is 6 cis d, l and cis l, d (enantiomers), trans d, I and trans I, d (enantiomers), cis d, d (same as cis I, I) meso (plane of symmetry), trans d, d (same as trans I I) meso (centre of symmetry)
 - (D) Two enantiomers are possible cis d, I and its mirror image cis I, d

Section III

- 13. Na₂S Na₂S forms a sulphur bridge in two p-amino-N,Ndimethyl aniline.
- 14. FeCl₃ FeCl₃ oxidises compound the above to methylene blue
- 15. $\operatorname{Fe}^{3+} + [\operatorname{Fe}(\operatorname{CN})_6]^{3-} \to \operatorname{Fe}[\operatorname{Fe}(\operatorname{CN})_6]$







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- 19. (A) (p) By MOT B₂ is paramagnetic
 - (q) Boron can be burnt to B_2O_3
 - (r) Boron can be reduced with metals to form metal borides.
 - (t) In B₂ molecule by MOT 2s and 2p orbitals mix to bring the energy of $\sigma 2p_z$ above that of $\pi 2p_x$ and $\pi 2p_y$ (It is equivalent to say that $\sigma 2p_z$ and $\sigma^* 2s$ interact to bring $\sigma 2p_z$ above the $\pi 2p_x$ and $\pi 2p_v$).
 - (B) (q) N_2 can be oxidised to NO by air.
 - (r) N₂ undergoes reduction to NH_{3.}
 - (s) Bond order in N_2 is 3.
 - (t) In N₂ molecule also there is mixing of 2s and 2p as in the above case of B₂.
 - (C) (p) O_2^- is paramagnetic by MOT.
 - (q) In hydrolysis of NaO2 with water it is (r)
 - oxidized to O2 and reduced to H2O2 simultaneously.

- (D) (p) By MOT O₂ is paramagnetic.
 - (q) O_2 can be oxidized to OF_2 by F_2 and $O_2^+ PtF_6^- by PtF_6$
 - (r) O_2 can be reduced to CaO by Ca and CO₂ by C
 - (s) Bond order in O_2 is 2.
- 20. (A) \rightarrow p, q, s, t
 - $(B) \rightarrow s, t$
 - $(C) \rightarrow p$
 - $(D) \rightarrow r$

Alkyl cyanides can be reduced to amines by H₂ / Pd / C. Reduction of cyanides with SnCl₂ / HCI or DIBAL-H followed by hydrolysis gives corresponding aldehydes. Cyanides can undergo alkaline hydrolysis to form sodium salt of carboxylic acid and NH₃. DIBAL -H reduces esters to aldehydes.

Esters can be catalytically reduced to alcohols and they undergo alkaline hydrolysis.

undergo i.nes undergo H. i. with CHCl₃ and alco Double bonds undergo catalytic reduction . Primary amines undergo Hofmann's carbylamine reaction with CHCl₃ and alcoholic KOH.

PART II



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But f(x) is non negative in [0, 1] $\therefore f(x) = \sin x$

$$\sin\frac{1}{2} < \frac{1}{2}$$
$$\sin\frac{1}{3} < \frac{1}{3}$$

24.
$$(z\overline{z})(\overline{z})^2 + (\overline{z} z)z^2 = 350$$

 $|z|^2 (z^2 + \overline{z}^2) = 350$
 $(x^2 + y^2) \{2(x^2 - y^2)\} = 350$
 $x^4 - y^4 = 175$
 $(x^2 + y^2) (x^2 - y^2) = 175$
 $x^2 = 16 \implies x = \pm 4$
 $y^2 = 9 \implies y = \pm 3$
∴ Area of the rectangle = 8 × 6 = 48

25.

M В $\frac{x^2}{9} + \frac{y^2}{1} = 0$ Auxiliary O is $x^2 + y^2 = 9$ A(3, 0) B(0, 1) Slope of AB = $-\frac{1}{3}$ Triumphant Ed $y=-\frac{1}{3}(x-3)$ 3y = -x + 3 $y = \frac{-x}{2} + 1$ $x^2 + \left(\frac{-x}{3} + 1\right)^2 = 9$ $x^{2} + \frac{x^{2}}{9} + 1 - \frac{2x}{3} = 9$ 9 3 9x² + x² + 9 - 6x = 81 10x² - 6x - 72 = 0 5x² - 3x - 36 = 0 x = $\frac{3 \pm \sqrt{9 + 720}}{10} = \frac{3 \pm 27}{10}$ $=3, -\frac{12}{5}$ $y = \frac{-12}{5x-3} + 1$ $=\frac{4}{5}+1=\frac{9}{5}$ Area OAM = $\frac{27}{5} \times \frac{1}{2} = \frac{27}{10}$

26. Given $(\overline{a} \times \overline{b}) \cdot (\overline{c} \times \overline{d}) = 1$ $\left|\overline{a} \times \overline{b}\right| \left|\overline{c} \times \overline{d}\right| \cos \gamma = 1$ where γ is the angle between $(\overline{a} \times \overline{b})$ and $(\overline{c} \times \overline{d})$ $\Rightarrow \sin \alpha \sin \beta \cos \gamma = 1$ (since $\left|\overline{a}\right| = \left|\overline{b}\right| = \left|\overline{c}\right| = \left|\overline{d}\right| = 1$ and we assume that angle between \overline{a} and \overline{b} is α and that, the angle between \overline{c} and \overline{d} is β) \Rightarrow sin α = 1, sin β = 1, cos γ = 1 $\Rightarrow \alpha = \beta = \frac{\pi}{2}, \ \gamma = 0$ $\Rightarrow \overline{a}$ and \overline{b} are orthogonal; \overline{c} and \overline{b} are orthogonal; $\overline{a} \times \overline{b}$ is parallel to $\overline{c} \times \overline{d}$. $\Rightarrow \overline{a}, \overline{b}, \overline{a} \times \overline{b}$ form a mutually orthogonal triad $\overline{c}, \overline{d}, \overline{c} \times \overline{d}$ form a mutually orthogonal triad Suppose $\overline{a} \parallel \overline{d}$ and $\overline{b} \parallel \overline{c}$ Let $\overline{b} = k\overline{c}$ $\overline{a} \perp \overline{b} \Rightarrow \overline{a}.\overline{b} = 0$ $\Rightarrow \overline{a}.k\overline{c}=0$

a contradiction

∴ D is false.

Here $\beta = 2\beta$

As \overline{a} not parallel to \overline{c} we should have that \overline{b} parallel to \overline{c}

:. (C) is the choice

27. $\sum_{m=1}^{15} Im \, z^{2m-1} = \sin \theta + \sin 3\theta + \sin 5\theta + ... + \sin 29\theta$

We have $\sin \alpha + \sin(\alpha + \beta) + \sin(\alpha + 2\beta) + ... + \sin(\alpha + n - 1\beta)$

$$\frac{\sin\left(\frac{\alpha+\alpha+n-1}{2}\frac{\beta}{2}\right)\sin\left(\frac{n\beta}{2}\right)}{\sin\frac{\beta}{2}}$$

$$\therefore \sin \theta + \sin 3\theta + \dots + \sin 2\theta\theta$$

$$= \frac{\sin\left(\frac{\theta + \theta + 14 \times 2\theta}{2}\right)\sin\left(\frac{15 \times 2\theta}{2}\right)}{\sin\frac{2\theta}{2}}$$

$$= \frac{\sin^2 15\theta}{\sin \theta}$$

$$= \frac{\sin^2 30^\circ}{\sin 2^\circ} = \frac{1}{4\sin 2^\circ}$$

28. $x_1 + x_2 + x_3 + x_4 + x_5 + x_6 + x_7 = 10$ $(x + x^2 + x^3)^7 = x^7 (1 + x + x^2)^7$ Coefficient of x^3 in $(1 + x + x^2)^7$ = Coefficient of x^3 in $\frac{(1 - x^3)^7}{(1 - x)^7}$

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 solution

= Coefficient of
$$x^3$$
 in $(1 - x^3)^7 (1 - x)^{-7}$
= $\frac{7.8.9}{1.2.3} - 7 \times 1$
= $84 - 7 = 77$

Section II





$$= e \times 1 - \int_{0}^{1} e^{x} dx$$
$$= e - \int_{0}^{1} e^{x} dx$$
$$= e - (e - 1) = 1$$
$$\int_{1}^{e} \ln y dy = [y \log y - y]_{1}^{e}$$
$$= (e - e) - (0 - 1)$$
$$= 1$$
$$\int_{1}^{e} \ln y dy = \int_{1}^{e} \ln (1 + e - y) dy$$

30.
$$L = \lim_{x \to 0} \frac{a - \sqrt{a^2 - x^2} - \frac{x}{4}}{x^4} (a > 0) \left(\frac{0}{0} \text{ form}\right)$$
$$= \lim_{x \to 0} \frac{\left(-\frac{1}{2}\right) \frac{(-2x)}{\sqrt{a^2 - x^2}} - \frac{x}{2}}{4x^3}$$
$$= \lim_{x \to 0} \frac{\frac{1}{\sqrt{a^2 - x^2}} - \frac{1}{2}}{4x^2}$$
It is given that L is finite $\Rightarrow \frac{1}{a} = \frac{1}{2}$
$$\Rightarrow a = 2$$
When $a = 2$
$$L = \lim_{x \to 0} \frac{2 - \sqrt{4 - x^2} - \frac{x^2}{4}}{x^4}$$

v2

•

$$= \lim_{x \to 0} \frac{\left(2 - \frac{x^2}{4}\right)^2 - \left(4 - x^2\right)}{x^4 \left(2 - \frac{x^2}{4} + \sqrt{4 - x^2}\right)} = \lim_{x \to 0} \frac{1}{16} \frac{1}{4} = \frac{1}{64}$$

31.
$$2 \cos \frac{B+C}{2} \cos \frac{B-C}{2} = 4 \sin^2 \frac{A}{2}$$

 $2 \sin \frac{A}{2} \cdot \cos \frac{B-C}{2} = 4 \sin^2 \frac{A}{2}$
 $\cos \left(\frac{B-C}{2}\right) = 2 \sin \frac{A}{2}$
 $= 2 \cos \frac{B+C}{2}$
 $\cos \frac{B}{2} \cos \frac{C}{2} + \sin \frac{B}{2} \sin \frac{C}{2}$
 $= 2 \left\{ \cos \frac{B}{2} \cos \frac{C}{2} - \sin \frac{B}{2} \sin \frac{C}{2} \right\}$
 $\sin \frac{B}{2} \tan \frac{C}{2} = 3 \sin \frac{B}{2} \sin \frac{C}{2}$
 $\tan \frac{B}{2} \tan \frac{C}{2} = \frac{1}{3}$
 $\Rightarrow \sqrt{\frac{(s-c)(s-a)}{s(s-b)}} \sqrt{\frac{(s-a)(s-b)}{s(s-c)}} = \frac{1}{3}$
 $\Rightarrow \frac{s-a}{s} = \frac{1}{3}$
 $3s - 3a = s$
 $2s - 3a = 0$
 $a+b+c-3a = 0$
 $b+c = 2a$ means
 $CA + BA = 2a, a \text{ constant}}$
 $\Rightarrow \text{Locus of A is an ellipse}$
32. Given $\frac{\sin^4 x}{2} + \frac{\cos^4 x}{3} = \frac{1}{5} - (1)$
Dividing by $\cos^4 x$
 $\frac{\tan^4 x}{2} + \frac{1}{3} = \frac{\sec^4 x}{5}$
 $= \frac{(1+\tan^2 x)^2}{5}$
 $\Rightarrow \tan^4 x (\frac{1}{2} - \frac{1}{5}) - \frac{2}{5} \tan^2 x + \frac{1}{3} - \frac{1}{5} = 0$
 $\Rightarrow \frac{3}{10} \tan^4 x - \frac{2}{5} \tan^2 x + \frac{2}{15} = 0$

$$\Rightarrow 9\tan^{4}x - 12\tan^{2}x + 4 = 0$$

$$\Rightarrow (3\tan^{2}x - 2)^{2} = 0$$

$$\Rightarrow \tan^{2}x = \frac{2}{3} - (2)$$

$$\therefore (A) \text{ is true}$$

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$$\frac{\sin^{8} x}{8} + \frac{\cos^{8} x}{27}$$

$$= \cos^{8} x \left\{ \frac{\tan^{8} x}{8} + \frac{1}{27} \right\}$$

$$= (\cos^{2} x)^{4} \left\{ \frac{\left(\frac{2}{3}\right)^{4}}{8} + \frac{1}{27} \right\}$$

$$= \left(\frac{1}{1 + \tan^{2} x}\right)^{4} \left\{ \frac{16}{81 \times 8} + \frac{1}{27} \right\}$$

$$= \left(\frac{3}{5}\right)^{4} \left\{ \frac{2}{81} + \frac{1}{27} \right\}$$

$$= \frac{81}{625} \times \frac{5}{81} = \frac{1}{125}$$
Equation (2) $\Rightarrow \frac{\sin^{2} x}{2} = \frac{\cos^{2} x}{2} = k$
 $\Rightarrow \sin^{2} x = 2k \text{ and } \cos^{2} x = 3k$
 $\therefore 2k + 3k = 1$
 $\Rightarrow k = \frac{1}{5}$
 $\therefore \frac{\sin^{8} x}{8} + \frac{\cos^{8} x}{27} = \frac{(2k)^{4}}{8} + \frac{(3k)^{4}}{27}$
 $= k^{4}[2+3] = 5k^{4} = \frac{1}{125}$

Section III

33. A symmetric matrix can be written as $\begin{pmatrix} a & d & e \\ d & b & f \\ e & f & c \end{pmatrix}$

But we have five 1s and four 0s. The three symmetrical pairs can be filled as pe the following.

Case 1

2 pairs of 1s and 1 pair of 0s. This is done in 3 ways. The main diagonal is filled using the remaining 1, 0, 0 in 3 ways.

∴ 9 ways.

Case 2

1 pair of 1s and 2 pairs of 0s. This is done in 3 ways. The main diagonal is filled using the remaining 1, 1, 1

∴ Total 3 ways

- ∴ 9 + 3 = 12 matrices
- 34. The matrices are

$ \begin{pmatrix} 1 \\ 0 \\ 0 \\ (0) \\ 1 \\ 1 \end{pmatrix} $	0 1 (1) 1 0 (4)	$\begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}$ $\begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$	$ \begin{pmatrix} 1 \\ 0 \\ 1 \\ (2) \\ 0 \\ 1 \end{pmatrix} $	0 1 0 1 1 (5)	1 0 1) 1 0)	$ \begin{pmatrix} 1 \\ 1 \\ 0 \\ (3) \\ \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} $	1 0 1 1 (6	$\begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$ $\begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$
$\begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$	0 0 1 (7)	1 1 0)	(1 1 0	1 0 1 (8)	0 1 0	$\begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \end{pmatrix}$	1 0 0 (9)	1 0 0)
$\begin{pmatrix} 0\\1\\1 \end{pmatrix}$	1 0 0 (10)	1 0 1)	$\begin{pmatrix} 0\\1\\0 \end{pmatrix}$	1 0 1 (11	0 1 1)		0 0 1 12)	1 1 1)

Determinants of the matrices 1, 2, 3, 6, 9 and 12 are zeros and all the other 6 matrices are non – singular. Each of these six matrices provide a unique solution to the given system.

35. When we observe matrices 1and 9, since right

hand side is $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$, they vanish for all Δ_i and thus

give infinite number of solutions. Matrices 2, 3, 6 and 12 give inconsistent systems.

36.
$$P(X = 3) = \frac{5}{6} \cdot \frac{5}{6} \cdot \frac{1}{6} = \frac{25}{216}$$

37.
$$P(X \ge 3) = 1 - P(X = 1 \text{ or } X = 2)$$

= $1 - \left[\frac{1}{6} + \frac{5}{6} \cdot \frac{1}{6}\right] = 1 - \frac{11}{36} = \frac{25}{36}$

38.
$$P(X \ge 6 / X > 3) = P\left(\frac{(X \ge 6) \cap (X > 3)}{P(X > 3)}\right)$$
$$= \frac{P(X \ge 6)}{P(X \ge 4)}$$
$$= \frac{\left(\frac{5}{6}\right)^5 \cdot \frac{1}{6} + \left(\frac{5}{6}\right)^6 \cdot \frac{1}{6} + \dots}{\left(\frac{5}{6}\right)^3 \cdot \frac{1}{6} + \left(\frac{5}{6}\right)^4 \cdot \frac{1}{6} + \dots}$$
$$= \frac{\left(\frac{5}{6}\right)^5}{\left(\frac{5}{6}\right)^3} = \frac{25}{36}$$

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Section IV

39. (A)
$$\frac{dy}{dx} = \frac{-y}{(x-3)^2}$$
$$\frac{dy}{y} = -\frac{dx}{(x-3)^2}$$
$$\ln y = \frac{1}{x-3}$$
$$y = e^{\frac{1}{x-3}}$$

Domain of non zero solution is $D : R - \{3\}$ Intervals contained in the domain D are

$$\begin{pmatrix} -\frac{\pi}{2}, \frac{\pi}{2} \end{pmatrix}, \begin{pmatrix} 0, \frac{\pi}{2} \end{pmatrix}, \begin{pmatrix} 0, \frac{\pi}{8} \end{pmatrix}$$

$$\therefore A \rightarrow p, q, s$$

(B) $I = \int_{1}^{5} (x-1)(x-2)(x-3)(x-4)(x-5) dx$
$$= \int_{-2}^{2} (t+2)(t+1) t (t-1) (t-2) dt$$

$$= 0$$

$$(\because \int_{-a}^{a} f(x) dx = 0, \text{ if } f(-x) = -f(x))$$

Intervals containing the value $I = 0$ are
$$\left(-\frac{\pi}{2}, \frac{\pi}{2} \right), (-\pi, \pi)$$

 $B \rightarrow (p, t)$

(C) $y = \cos^2 x + \sin x$ $y' = -2\cos x \sin x + \cos x$ $= \cos x (-2\sin x + 1) = -\sin 2x + \cos x$ For extremum, y' = 0 $\Rightarrow \cos x = 0$ or $\sin x = \frac{1}{2}$ $y'' = -2\cos 2x - \sin x$ When $\cos x = 0$, y'' = 2(1) - 1 > 0 $\therefore \cos 2 = 0$ gives a local minimum When $\sin x = \frac{1}{2}$, $y'' = -2\left(1 - \frac{2}{4}\right) - \frac{1}{2} < 0$ $\Rightarrow \sin x = \frac{1}{2}$ gives a local maximum $\Rightarrow x = n\pi + (-1)^n \frac{\pi}{6}$ $\therefore C \Rightarrow p, q, r, t$

(D)



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PART III

	41 B	42 B	43 C	44 A	45 C	46 4 D	47 A	48 D	
		49	5()	51		52		
		A	С,	D	A, I)	B, D		
		53	54	55	56	57	58		
		D	Α	B	Α	B	D		
		-	59			60			
		A –	p, r, s			A – p,	t		
		B -	- r, s			B – q , s	, t		
		C –	p, q, t			C – p, r	, t		
		D -	- r, s			D – q			
	Section 1				46. o	♦ = AB, current in c	increas lirectior	ses. By L n dc and ab	enz's law, induced
41.	$\frac{Q_1}{R_1^2} = \frac{Q_1 + Q_2}{R_2^2} = \frac{Q_1 + Q_2}{R_3^2}$	+ Q ₃			47. (Charged er	nclosed	$I = \frac{1}{2}$ that	on disc + $\frac{1}{4}$ that on
	$\Rightarrow \frac{4}{Q_1} = 3; \ \frac{4}{Q_1} = 5;$					rod + point $\therefore \phi = -2C$	charge ∕ ε ₀	-7c	1°
42.	At 60°, mgsin $\theta \frac{h}{2}$ > mgcos θ . it will topple at $\theta < 60^{\circ}$	$\frac{a}{2}$			48.	T = 8s, pha	se = - <u>-</u>	$\frac{\pi}{\pi}$ $t = \frac{\pi}{2}$	
43.	$v^2 = 2gs = 2 \times 10 \times (20 - 12)$	8) ⇒				$\omega = \frac{2\pi}{T} \therefore$	a = -œ	$r^{2}A.sin\frac{\pi}{3}$ (A	A = 1 cm)
	$v = 12 \text{ m s}^{-1}$ $v' = \mu \times v = \frac{4}{3} \times 12 = 16 \text{ m}$	s ⁻¹		100	(1) (1) (1)		=	$\frac{\sqrt{3}}{32}\pi^2$.cm s	- ²
44.	$y_{\rm CM} = \frac{\rm ma + ma + m.0 + m}{10m}$	(-a) + 6r	$\frac{n.0}{1} = \frac{a}{1}$		1		S	ection II	
45	v A av	Ma	Sec. 1	0	49. l I	Internal for masses sy couple exe	ces car stem). rts no f	n convert K Since Ne orce but a t	.E to P.E (eg. Spring wton's third law. A torque.
40.		12	20°		50.	•		1	
	1202 1200				-	Reading	f	Error	
		1.11			-	(42, 50)	24	0	$0.2 \times (\frac{24}{56})^{-1}$
	2v 120°	After 2 nd				(48, 48)	24	0	$0.2 \times \left(\frac{24}{48}\right)^2$
	After 1 st 2v c	ollision,				(60, 40)	24	0	$0.2 \times (24/40)^2$
	3	Collisio	n at A		ŀ	(00.00)			()0

Reading	f	Error	Calculation
(42, 56)	24	0	$0.2 \times \left(\frac{24}{56}\right)^2$
(48, 48)	24	0	$0.2 \times \left(\frac{24}{48}\right)^2$
(60, 40)	24	0	$0.2 \times \left(\frac{24}{40}\right)^2$
(66, 33)	22	-2	$0.2 \times \left(24/33\right)^2$
(78, 39)	26	+2	$0.2 \times \left(24/39\right)^2$

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51. $R_{eq} = 3.2 \text{ K}\Omega \Rightarrow I = \frac{24v}{3.2 \text{ K}\Omega} = 7.5 \text{ mA}$ $V_{RL} = 7.5 \text{ mA} \times 1.2 \text{ K}\Omega = 9V$

Effective emf formula = $\frac{E_{R_1}}{\frac{1}{R_4} + \frac{1}{R_5}}$ and

$$\frac{\frac{E}{R_2}}{\frac{1}{R_2} + \frac{1}{R_1}} \Rightarrow ratio = 3$$

 \therefore Ratio of power = 9

52.
$$C_p - C_v = R$$
 for all gases
 $C_v = \frac{3}{2}R$ for monoatomic
 $\frac{5}{2}R$ for diatomic

Section III

- 53. High temperature ionizes the gas
- 54. Total KE = 3KT = P.E = $\frac{e^2}{4\pi\varepsilon_0}$
 - \therefore T \simeq 1.4 \times 10⁹ K
- 55. Multiply and check nt with Lawson Number
- 56. $n\frac{\lambda}{2} = a$ $p = \frac{h}{\lambda}$ $E = \frac{p^2}{2m} \Rightarrow E \propto \frac{1}{\lambda^2} \propto \frac{1}{\lambda^2}$

57.
$$E = \frac{h^2}{8ma^2}\Big|_{for n = 1} = 8 \times 10^{-3} \text{ eV}$$

$$E = \frac{p^2}{2m} = \frac{\left(\frac{h}{\lambda}\right)^2}{2m} = \frac{\left(\frac{h}{2a}\right)^2}{2m} = \frac{h^2}{8ma^2}$$

58.
$$\mathbf{v} \propto \mathbf{p}, \mathbf{p} = \frac{\mathbf{h}}{\lambda} \Rightarrow \lambda \propto \frac{1}{\mathbf{n}}$$
$$\Rightarrow \mathbf{p} \propto \mathbf{h} \Rightarrow \mathbf{v} \propto \mathbf{n}$$

Section IV

- 59. Unlike charges moving along a circle \Rightarrow no current (say reason 1)
 - (p) +, charges are symmetric
 ∴ E = 0
 Same reason, V = 0
 Due to reason 1, B = 0 and μ = 0

 (a) Haracenetic distribution on shore
 - (q) Unsymmetric distribution or charges about M. Hence E \neq 0 and V = 0 Due to reason (1), B = 0 and μ = 0
 - (r) Due to symmetry E = 0, V \neq 0 Clearly B \neq 0, $\mu \neq$ 0
 - (s) By symmetry, E = 0, distances being not commensurate, V ≠ 0, negative currents reinforce B plus charges oppose but of different magnitude.
 - (t) Due to lack of symmetry $E \neq 0$. But V can be zero. Due to reason (1) $B = 0 \Rightarrow \mu = 0$
- 60. (p) Y has constant velocity. Therefore, reaction force is equal to weight.
 PE is continuously decreasing. Mechanical energy decreasing due to frictional loss. Torque is variable
 - (q) Magnetic force between Z and Y is Mg
 ∴ Normal reaction is 2 Mg. Since it is moving up gravitational P.E is increasing and thus mechanical energy is increasing. By symmetry, torque is zero
 - (r) Pulley supports the mass M. So reaction force = $(m_0 + \sqrt{2}M)g$. Since it is moving down gravitational P.E is decreasing and so the mechanical energy is decreasing. Torque is a non-zero constant
 - (s) Sphere moving down with uniform acceleration. Therefore force < Mg. Gravitational P.E of x is increasing and Mechanical energy is conserved. Torque is a non-zero constant
 - (t) Terminal velocity ⇒ net force zero. Gravitational P.E of x is increasing, but mechanical energy is decreasing because of frictional forces. Torque is a non-zero constant.

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