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If the papers of 4 students can be checked by any one of the 7 teachers, then the probability that all the 4 papers are checked by exactly 2 teachers is:

(B)  $\frac{12}{47}$  (C)  $\frac{32}{343}$  (D)  $\frac{6}{49}$ (A)  $\frac{2}{7}$ A tetrahedron has vertices O(0, 0, 0), A(1, 2, 1), B(2, 1, 3)and C(-1, 1, 2). The angle between the faces OAB and ABC is:

(A)  $\cos^{-1}\left(\frac{19}{35}\right)$  (B)  $\cos^{-1}\left(\frac{17}{31}\right)$  (C) 30° (D) 90<sup>0</sup>

The area bounded by the curve y = f(x), y = x and the lines

x = 1, x = t is  $(t + \sqrt{1 + t^2}) - \sqrt{2} - 1$  sq. units for all t > 1. If f(x) satisfying f(x) > x for all x > 1, then f(x) is equal to:

(A) 
$$x + 1 + \frac{x}{\sqrt{1 + x^2}}$$
 (B)  $x + \frac{x}{\sqrt{1 + x^2}}$   
(C)  $1 + \frac{x}{\sqrt{1 + x^2}}$  (D)  $\frac{x}{\sqrt{1 + x^2}}$ 

The differential equation representing the family of the curves  $y^2 = 2c(x + \sqrt{c})$ , where 'c' is a positive parameter, is of:

(A) order 1, degree 3 (B) order 2, degree 2 (C) order 3, degree 3 (D) order 4, degree 4 Let  $f(x) = \frac{x - [x]}{1 + x - [x]}$ ,  $x \in \mathbb{R}$ , then the range of f is:

A) 
$$[0, 1]$$
 (B)  $\left[0, \frac{1}{2}\right]$  (C)  $\left[0, \frac{1}{2}\right]$  (D)  $(0, 1)$ 

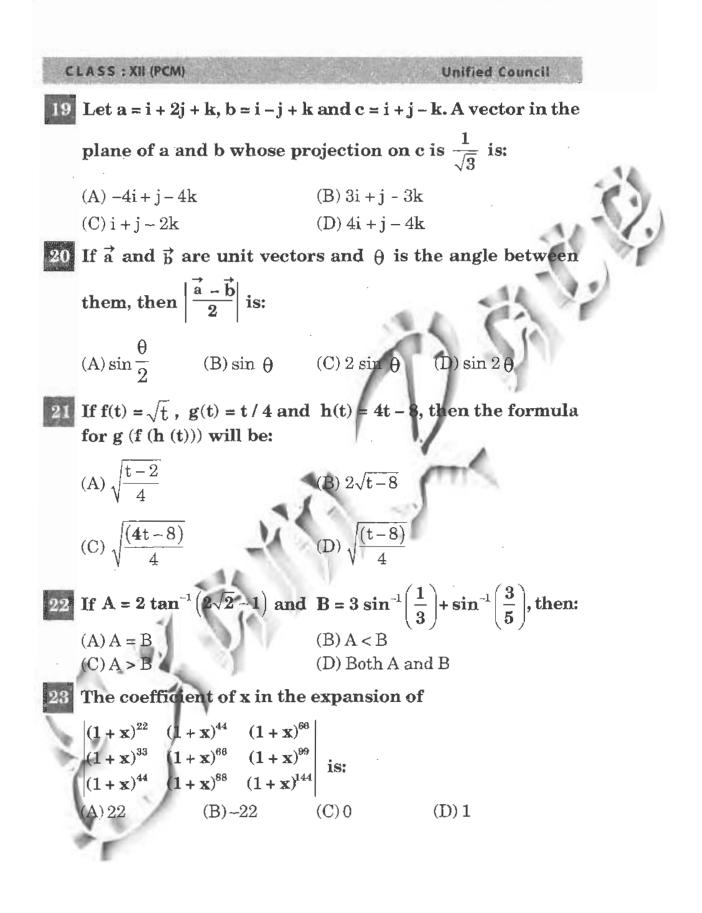
12 Value of 
$$\sum_{\mathbf{r}=0}^{\infty} \tan^{-1} \left( \frac{1}{1+\mathbf{r}+\mathbf{r}^2} \right)$$
 is equal to:  
(A)  $\frac{\pi}{2}$  (B)  $\frac{3\pi}{4}$  (C)  $\frac{\pi}{4}$  (D)  $\frac{5\pi}{4}$ 

(A) 
$$\frac{1}{2}$$
 (B)  $\frac{--}{4}$  (C)  $\frac{1}{4}$ 

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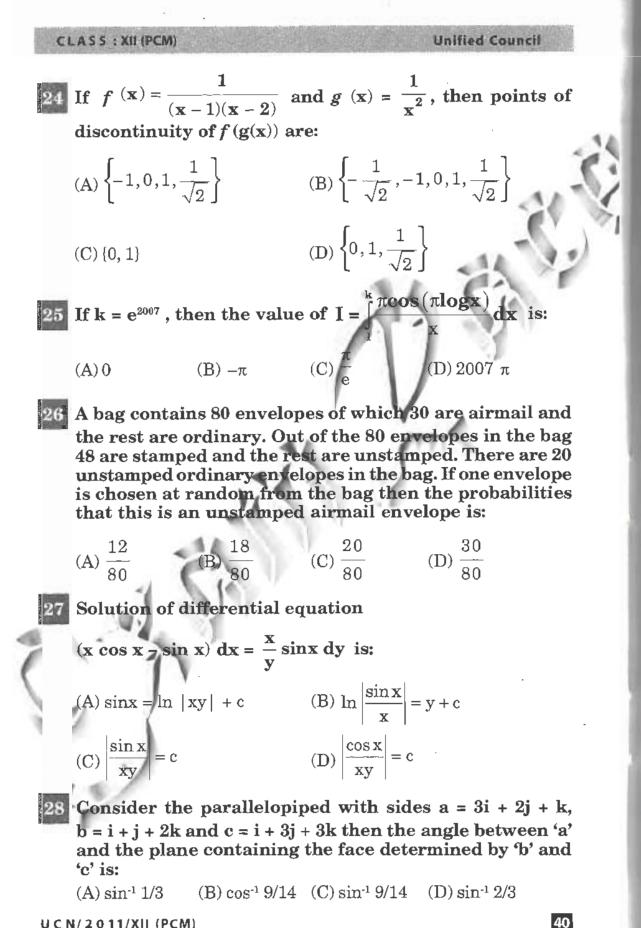
**Unified Council** CLASS : XII (PCM) If A<sup>k</sup> = 0, for some value of k,  $(I - A)^{p} = I + A + A^{2} + \dots + A^{k-1}$ , thus p is: (A is nilpotent with index k) (D)-4(C) - 3(A) - 1(B) - 2Which of the following could not be true if  $f''(x) = x^{-1/3}$ ? (A)  $f(x) = \frac{3}{2} x^{2/3} - 3$  (B)  $f(x) = \frac{9}{10} x^{5/3} - 7$ (C)  $f'''(x) = -\frac{1}{3}x^{-4/3}$  (D)  $f'(x) = \frac{3}{2}x^{2/3} + 6$ 15 Let  $f''(x) > 0 \forall x \in R$  and g(x) = f(2 - x) + f(4 + x), then g(x)is increasing in: (B)  $(-\infty, 0)$ (D)  $(-2, \infty)$ (A)  $(-\infty, -1)$ (C)  $(-1, \infty)$ 16 Of the 25 questions in a unit, a student has worked out only 20. In a sessional test of that unit, two questions were asked by the teacher. The probability that the student can solve both the questions correctly, is: (B) 17/25 (C) 9/10 (D) 19/30 (A) 8/25 The volume of the tetraheron whose vertices are with position vectors  $\hat{i} - 6\hat{j} + 10\hat{k}$ ,  $-\hat{i} - 3\hat{j} + 7\hat{k}$ ,  $5\hat{i} - \hat{j} + \lambda\hat{k}$  and  $7\hat{i} - 4\hat{j} + 7\hat{k}$  is 11 cubic unit if  $\lambda$  equals: (B) 3 (C)7(A) -3 (D) - 118 If for the differential equation  $y^1 = \frac{y}{x} + \phi \left(\frac{x}{y}\right)$  the general solution is  $y = \frac{x}{\log |cx|}$ , then  $\phi\left(\frac{x}{y}\right)$  is given by: (A)  $-\frac{x^2}{x^2}$  (B)  $\frac{y^2}{x^2}$  (C)  $\frac{x^2}{y^2}$  (D)  $\frac{-y^2}{x^2}$ 

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 29
 If 
$$|\mathbf{a}| = 2$$
,  $|\mathbf{b}| = 3$   $|\mathbf{c}| = 4$  and  $\mathbf{a} + \mathbf{b} + \mathbf{c} = 0$  then the value of  $\mathbf{b}, \mathbf{c} + \mathbf{c}$ .  $\mathbf{a} + \mathbf{a}$ .  $\mathbf{b}$  is equal to:  
 (A) 19/2 (B) - 19/2 (C) 29/2 (D) - 29/2

 30
 If the pair of lines represented by the equation  $6x^2 + 17xy + 12y^2 + 22x + 31y + 20 = 0$  be  $2x + 3y + p = 0$  and  $3x + 4y + q = 0$  then:  
 (A)  $p + q = 19$  (B)  $p^2 + q^2 = 41$  (C)  $3p - 2q = 22$  (D)  $4p - 3q = 61$ 

 31
 If  $\mathbf{I} = \frac{15}{8} \frac{dx}{(x-3)\sqrt{x+1}}$ , then I equals:  
 (A)  $\frac{1}{2} \log \frac{5}{3}$  (B)  $2 \log \frac{1}{3}$  (C)  $\frac{1}{2} \log \frac{5}{10}$  (D)  $2 \log \frac{5}{3}$ 

 32
 If  $\mathbf{a} \sin^{-1} \mathbf{x} - \mathbf{b} \cos^{-1} \mathbf{x} = \mathbf{c}$ , then  $\mathbf{a} \sin^{-1} \mathbf{x} + \mathbf{b} \cos^{-1} \mathbf{x}$  is equal to:  
 (A)  $0$  (B)  $\frac{\pi ab + c(b-a)}{a+b}$  (C)  $\frac{\pi}{2}$  (D)  $\frac{\pi ab + c(a-b)}{a+b}$ 

 33
 The inverse of a skew symmetric matrix of odd order is:  
 (A)  $\mathbf{a}$  symmetric matrix (D) does not exist

 34
 If  $\begin{vmatrix} \mathbf{x} & \mathbf{3} & \mathbf{6} \\ \mathbf{6} & \mathbf{x} & \mathbf{3} \end{vmatrix} = \begin{vmatrix} \mathbf{x} & \mathbf{7} & \mathbf{2} \\ \mathbf{7} & \mathbf{2} & \mathbf{x} \end{vmatrix} = \begin{vmatrix} \mathbf{5} & \mathbf{x} & \mathbf{4} \\ \mathbf{x} & \mathbf{4} & \mathbf{5} \end{vmatrix} = 0$ , then  $\mathbf{x}$  is equal to:  
 (A)  $9$  (B)  $-9$  (C) (D) (D) 1

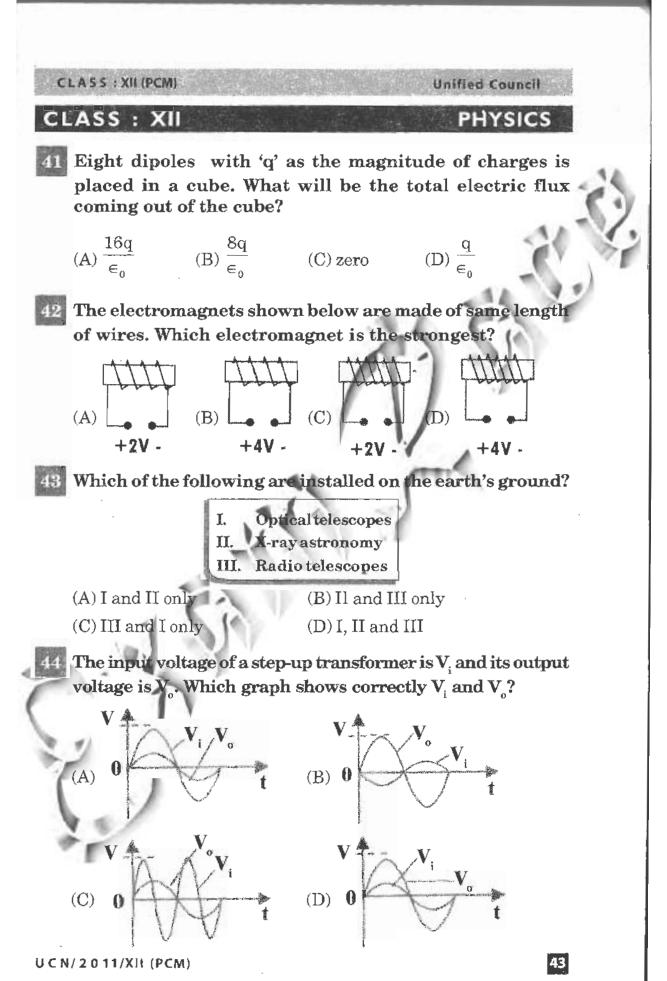
 35
 If  $\cos^{-1}\left(\frac{\mathbf{x}^2 - \mathbf{y}^2}{\mathbf{x}^2}\right) = \log a$ , then  $\frac{dy}{dx}$  is equal to:  
 (A)  $\frac{y}{\mathbf{x}}$  (B)  $\frac{x}{\mathbf{y}}$  (C)  $\frac{x^4}{y^2}$  (D)  $\frac{y^2}{x^2}$ 

 36
 If  $\cos^{-1}\left(\frac{\mathbf{x}^3 - \mathbf{y}^2}{\mathbf{x}^3 + \mathbf{y}^2}\right) = \log a$ , then  $\frac{dy}{dx}$  is equal to:  
 (A)  $(\pm 4/\sqrt{3}, -2)$  (B)  $(\pm \sqrt{\frac{11}{3}, 1)$   
 (C)  $(0, 0)$  (D)  $(\frac{\pm \sqrt{\frac{3}{3}, 2}$ 

CLASS : XH (PCM) **Unified Council** 37 If I =  $\int \frac{5+3x}{\sqrt{(x-1)(x+2)}} dx$ , then I equals: (A)  $3\sqrt{(x-1)(x+2)} + \frac{7}{2}\log|x+\frac{1}{2} + \sqrt{(x-1)(x+2)}| + c$ (B)  $3\sqrt{x^2 - x - 2} + \frac{7}{2} \log \left| x + \frac{1}{2} + \sqrt{x^2 - x - 2} \right| + c$ (C)  $3\log \left| x + \frac{1}{2} + \sqrt{(x-1)(x+2)} \right| + c$ (D)  $3\sin^{-1}\sqrt{\frac{x-1}{x-2}} + c$ 38 Area bounded by the curve y = (x - 1)(x - 2)(x - 3) and x-axis lying between the ordinates x = 0 and x = 3 is equal to: (B)  $\frac{11}{4}$  sq.unit (A)  $\frac{9}{4}$  sq. unit (C)  $\frac{13}{4}$  sq. unit (D)  $\frac{15}{4}$  sq. unit 39 If the foot of the perpendicular from the origin to a plane is (a, b, c), then the equation of the plane is: (A)  $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 3$ (B) ax + by + cz = 3

(C)  $ax + by + cz = a^2 + b^2 + c^2$  (D) ax + by + cz = a + b + c40 Let us define the length of a vector  $a\hat{i} + b\hat{j} + c\hat{k}$  as

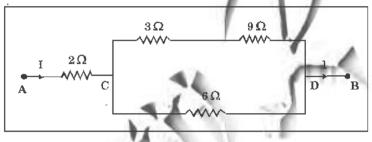
 $|\mathbf{a}| + |\mathbf{b}| + |\mathbf{c}|.$  This definition coincides with the usual definition of length of a vector  $\mathbf{a} \cdot \mathbf{i} + \mathbf{b} \cdot \mathbf{j} + \mathbf{c} \cdot \mathbf{k}$  iff: (A)  $\mathbf{a} = \mathbf{b} = \mathbf{c} = 0$  (B) any two of a, b and c are zero (C)  $\mathbf{a} + \mathbf{b} + \mathbf{c} = 0$  (D) any one of a, b and c is zero



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- 45 A ray of light in a liquid of refractive index 1.6, approaches the boundary surface between the liquid and air at an angle of incidence i where sini = 0.7. Which of the following statements is *true* about the behaviour of the light?
  - (A) It is impossible to predict the behaviour of the light ray on the basis of the information supplied
  - (B) The sine of the angle of refraction of the emergent ray will be less than 0.7
  - (C) The ray will be internally reflected
  - (D) The sine of the angle of refraction of the emergent ray will be greater than 0.7.

## 6 Look at the circuit given below.



The resistance 6  $\Omega$  develops 24 cal s<sup>-1</sup> due to the current flowing through it. Find the rate of heat developed in 2  $\Omega$  resistance?

(A)  $2 \operatorname{cal} s^{-1}$  (B)  $18 \operatorname{cal} s^{-1}$  (C)  $8 \operatorname{cal} s^{-1}$  (D)  $24 \operatorname{cal} s^{-1}$ 

Find the binding energy of the least strongly bound neutron in a  ${}_{6}C^{13}$  nucleus. (Given atomic mass of  ${}_{6}C^{13}$  = 13.00335 U, Atomic mass of  ${}_{6}C^{12}$  = 12 U, the mass of a neutron = 1.00867 U, 1 U = 931 MeV)

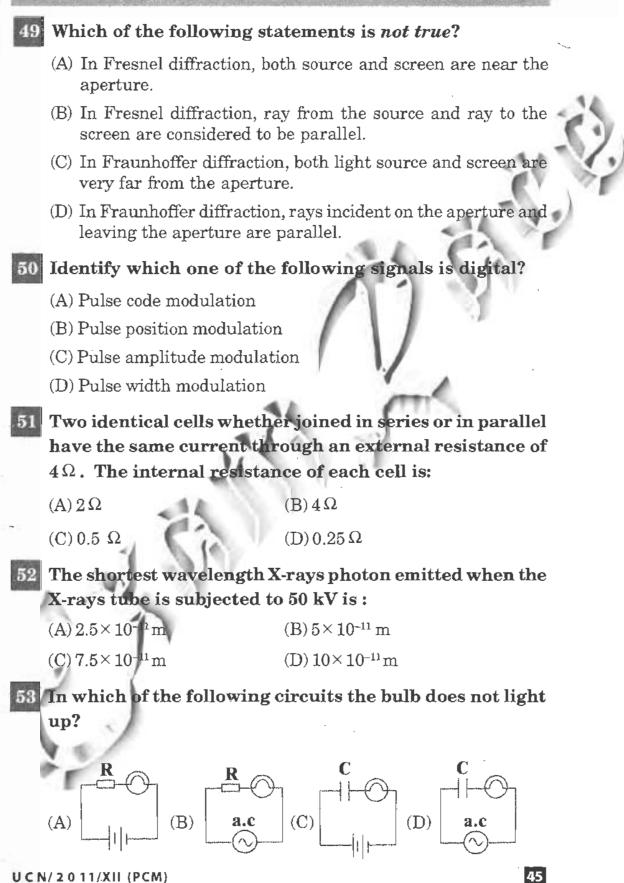
(A) 3.4 MeV	(B) 4.953 MeV
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(C) 6.879 MeV (D) 1.84 MeV

48 Which gate can act as a building block for the digital circuits?

(A) OR (B) AND (C) NOT (D) NAND

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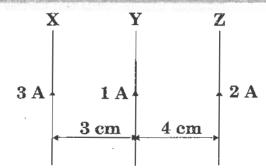


1

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If the length of the wire Y is 0.5 m, then what force is experienced by it?

(A)  $10^{-5}$  N from left to right (B)  $10^{-5}$  N from right to left

(C) 5×10<sup>-6</sup> N from left to right (D) 5×10<sup>-6</sup> N from right to left

60 According to Maxwell's hypothesis a changing electric field gives rise to:

(A) changing magnetic field(B) changing electric field(C) an e.m.f.(D) gravitational field

61 If x and y are the distance of an object and its image from the focus of a spherical mirror (focal length f), then identify the correct relation between x, y and f.

(A) xy = f (B)  $xy = f^2$  (C)  $xy = f^3$  (D)  $\frac{x}{y} = f$ 

62 What will be the change in the resistance of a circuit consisting of 5 similar conductors if two similar conductors are added as shown in figure.

If  $R_1$  and  $R_2$  are resistances in two cases respectively, then find the ratio of  $R_2$  to  $R_1$ .

(A) 7:5 (B) 2:5 (C) 1:2 (D) 3:5

A parallel plate condenser with plate A is filled with two dielectrics K<sub>1</sub> and K<sub>2</sub> occupying equal space lengthwise as shown.

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CLASS : XII (PCM) +Ve K<sub>1</sub> K<sub>2</sub> -Ve

If the separation between the two plates is 't' for each dielectric, then find the capacity C.

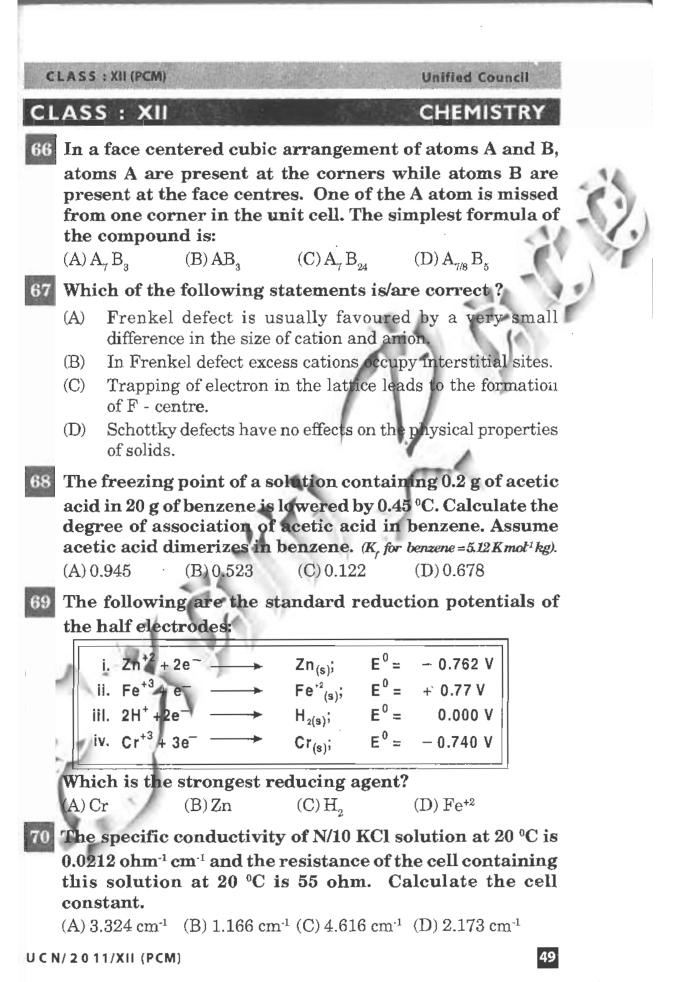
(A) 
$$C = \frac{\epsilon_0 A(K_1 + K_2)}{t}$$
 (B)  $C = \frac{\epsilon_0 A(K_1 + K_2)}{2t}$   
(C)  $C = \frac{2\epsilon_0 A(K_1 + K_2)}{t}$  (D)  $C = \frac{\epsilon_0 A(K_1 - K_2)}{2t}$ 

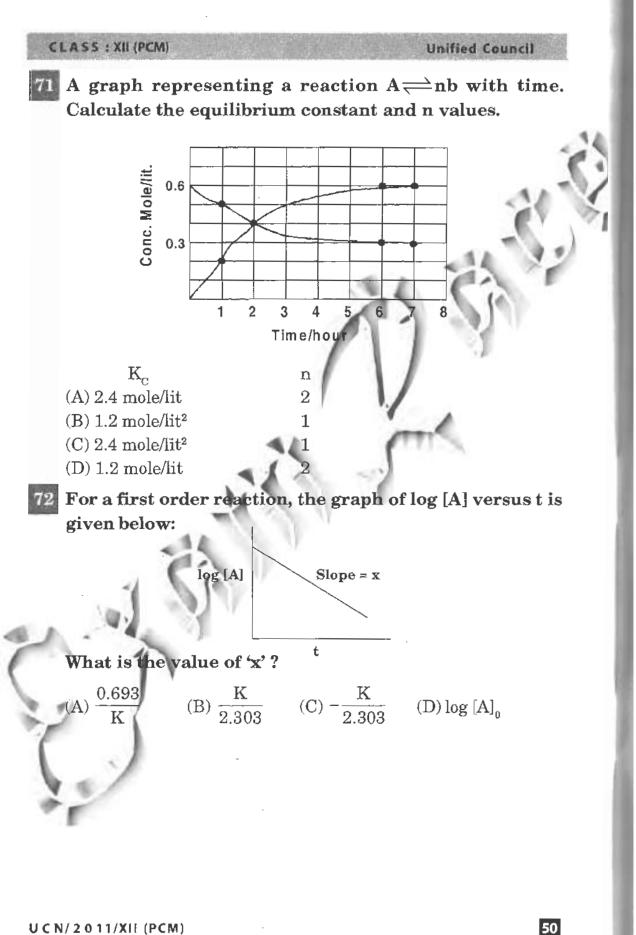
64 A horizontal wire AB of mass  $3 \times 10^{-3}$  kg and length one metre carries a current of 9.8 A. The wire lies in the magnetic field acting perpendicular to the wire. What is the magnitude of the field which can support the weight of the wire?

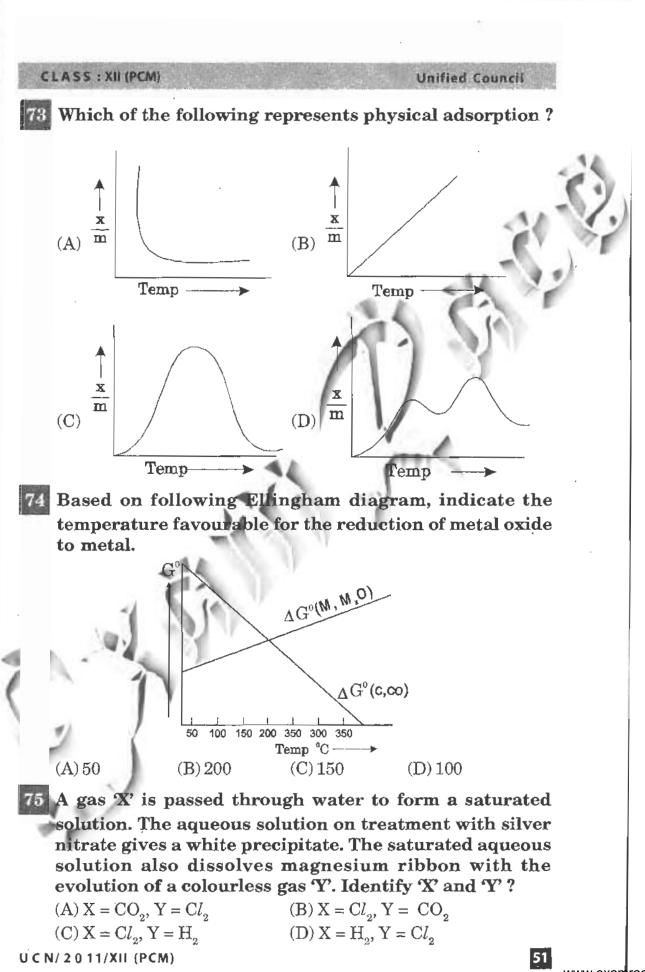
(A) 
$$3 \times 10^{-3}$$
 T  
(B)  $3 \times 10^{-3} \times 9.8$  T  
(C)  $\frac{3 \times 10^{-3}}{9.8}$  T  
(D)  $\frac{1}{3 \times 10^{-3}}$  T

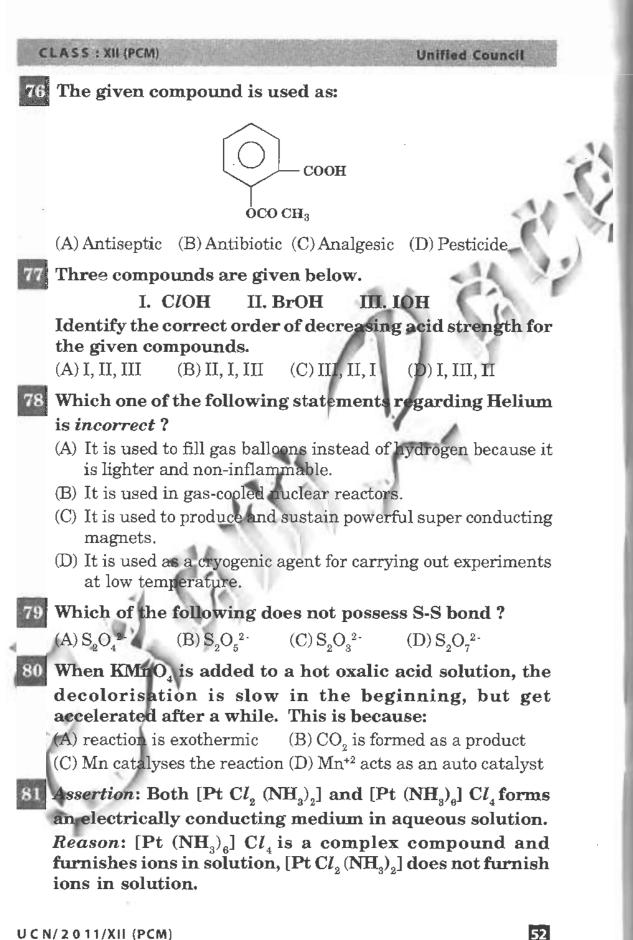
Which of the following statements regarding zener diode is *true*?

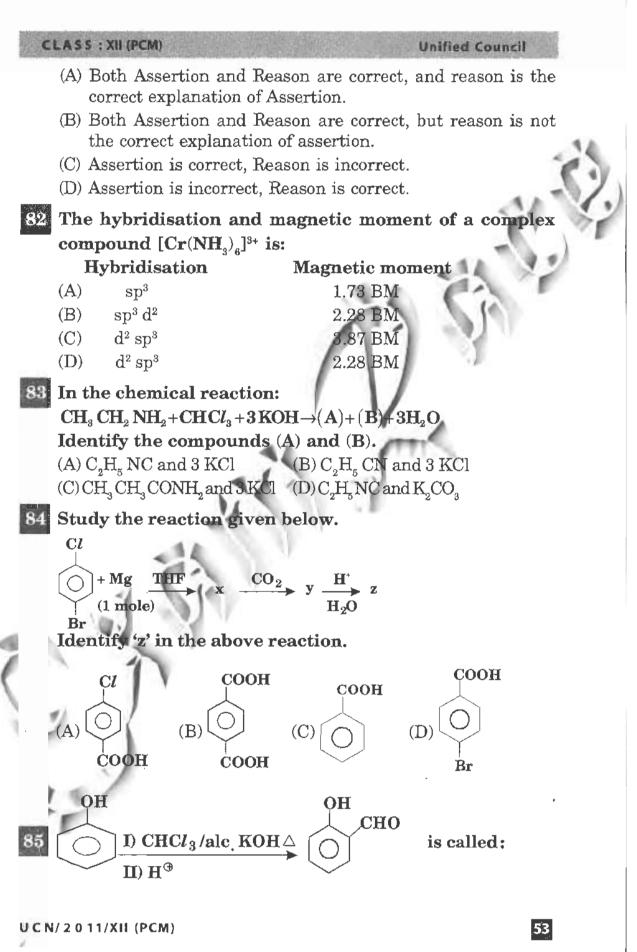
- (A) A zener can operate only in the forward biased condition
- (B) Zener breakdown occurs when applied voltage is less than zener breakdown voltage
- (C) The current in the zener region is in opposite direction to that of the forward biased diode
- (D) Zener diode is used as a half wave rectifier

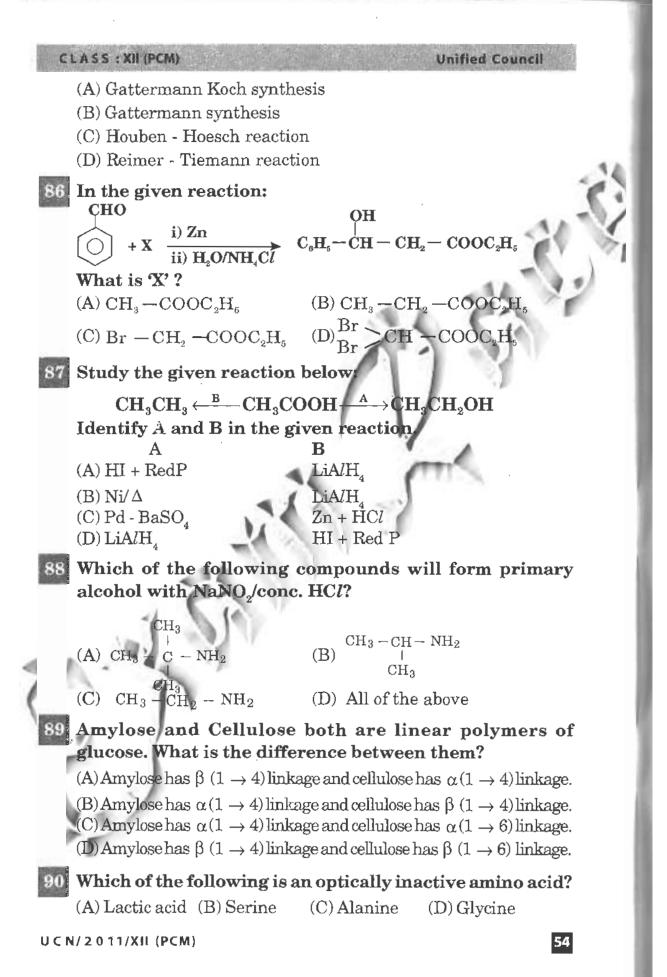


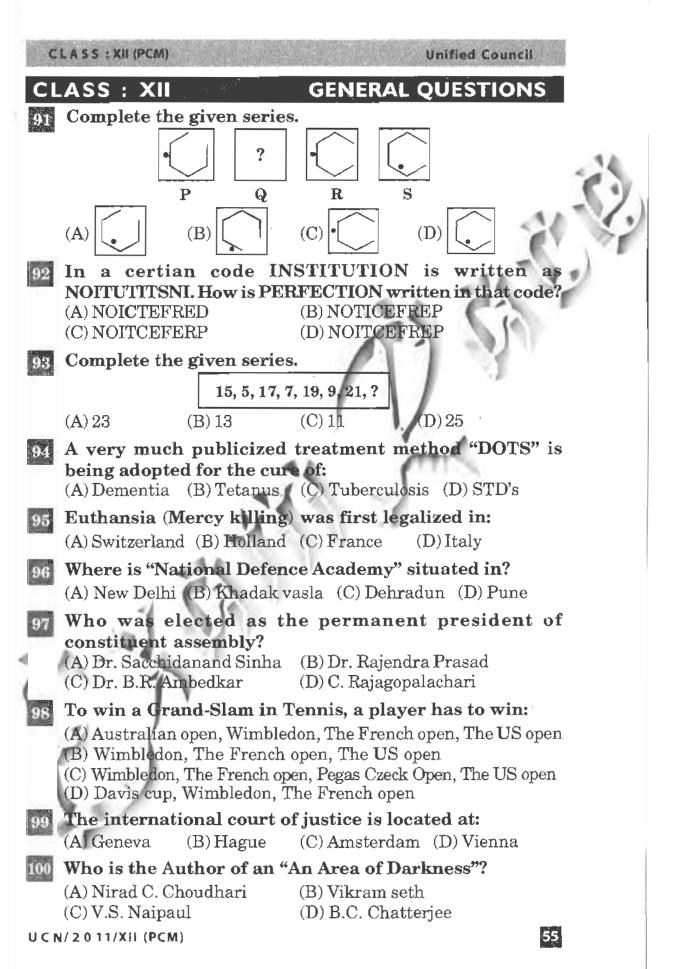














## Q.P.-2011 **KEY FOR THE** 5. 6. 2. 3. D 4. D В A 7. С В D 8. 1. A A 10. 11. С 12. A 13. A 14. A 15. С 16. D 9. A С 19. 20. 21. 22. 23. 17. С 18. D A A A С 24. В 28. 29. D 30. В 31. A 32. 25. 26. 27. А A С С D 33. D 34. В 35. 36. 37. 38. В 39. С 40. В A D A 42. 43. 45. C 46. 47. 48. 41. C В D С 44 В В D 49. 50. A 51. В 52. 53. С 55. 56. B 54. A В C А 57. A 58. В 59. С 60. A 61. В 62. D 63. В 64. A 66. 67. 68. 70. 71. 65. C С С А 69. В В D 72. C 75. 76. 78. 73. A 74. В С С 77. А A 79. D 80. D 81. 83. A 85. D C D С D С 84. 86. 82. Α 87. 88. 89. 90. D 91. A 92. D 93. С С 95. B 94. В 96. в 97. B 100. C 98. 99. B A