BT6/M11

8616

Digital Signal Processing

Paper—ECE-306E

Time: Three Hours]

[Maximum Marks: 100

Note: —Attempt any FIVE questions in all, selecting at least ONE question from each unit.

UNIT-I

- Let x(n) be a sequence with z-transform X(z). Determine, in 1. terms of X(z), the z-transform of $x_1(n) = x\left(\frac{n}{2}\right)$, if n even.
 - Use contour integration to determine the sequence x(n) where: (b)

$$X(z) = \frac{\left(1 - \frac{1}{4}z^{-1}\right) \text{ NOWLEDGE}}{\left(1 - \frac{1}{6}z^{-1} - \frac{1}{6}z^{-2}\right)}, |z| > \frac{1}{2}.$$

(c) Compute the quantity $\sum_{n=0}^{(N-1)} x_1(n) x_2(n)$ if:

$$x_1(n) = \delta(n) + \delta(n-8)$$

 $x_2(n) = u(n) - u(n-N)$.

2. Determine the signal x(n) with z-transform: (a)

$$X(z) = e^z + e^{1/z}, |z| \neq 0.$$
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Determine if the following FIR system is minimum phase :-5

$$h(n) = [5, 4, -3, -4, 0, 2, 1].$$

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(c) Prove the identity:

$$\sum_{\ell=-\infty}^{+\infty} \delta(n+\ell N) = \frac{1}{N} \sum_{k=0}^{(N-1)} e^{j\left(\frac{2\pi}{N}\right)kn}.$$

UNIT-II

3. (a) Consider a causal IIR system with system function:

$$H(z) = \frac{1 + 2z^{-1} + 3z^{-2} + 2z^{-3}}{1 + 0.9z^{-1} - 0.8z^{-2} + 0.5z^{-3}}.$$

Determine the equivalent lattice ladder structure.

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(b) Consider the system described by the difference equation

$$y(n) = ay(n-1) - ax(n) + x(n-1)$$

Show that it is all-pass.

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(ii) Obtain the direct form II realization of the system.

4. (a) Determine the state-space model for the system described by

$$y(n) = y(n-1) + 0.11 y(n-2) + x(n)$$

and sketch the type 1 and type 2 state-space realizations.

5+5+5

(Contd.)

(b) Determine a direct form realization of following linear phase filters:

$$h(n) = \{1, 2, 3, 4, 3, 2, 1\}.$$
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UNIT—III

(a) Determine the unit sample response {h(n)} of a linear-phase
 FIR filter of length M = 4 for which the frequency response at

$$w = 0$$
 and $w = \frac{\pi}{2}$ is specified as $H_r(0) = 1$, $H_r\left(\frac{\pi}{2}\right) = \frac{1}{2}$. 10

(b) Write a short note on "Alternation Theorem".

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6. (a) Explain the Gibbs phenomenon with example.

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(b) Design an FIR linear-phase, digital filter approximating the ideal frequency response:

$$H_{d}(w) = \begin{cases} 1, & \text{for } |w| \le \pi/6 \\ 0, & \text{for } \frac{\pi}{6} < |w| \le \pi. \end{cases}$$

 (i) Determine the coefficient of a 25-tap filter based on window method with a rectangular window.

(ii) Repeat part (i) using Hamming window.

UNIT-IV

 A digital low-pass filter is required to meet the following specifications:—

Passband ripple : ≤ 1 dB

Passband edge: 4 kHz

Stopband attenuation : ≥ 40 dB

Stopband edge: 6 kHz

Sample rate: 24 kHz; Assume t = 1.

The filter is to be designed by performing a bilinear transformation on an analog system function. Determine what order Butterworth, Chebyshev and Elliptic analog designs must be used to meet the specifications in the digital implementation.

6+6+8

8. Explain the design of digital filters based on Least-squares method.

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