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ఎిజ్జయు : గెణొత
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## Subject : MATHEMATICS

( ఇంగ్లిలటో భృషాంతర / English Version )

దినృంళ : 09. 04. 2012 ]

ய゙రふృఎధ̣ అంశగళు : 100 ]
[ Date: 09. 04. 2012
[ Time : 10-30 A.M. to 1-45 P.M.
[ Max. Marks : 100

FOR OFFICE USE ONLY

| $\begin{gathered} \text { G. } \\ \text { No. } \end{gathered}$ | Marks | $\begin{aligned} & \mathbf{G} . \\ & \text { No. } \end{aligned}$ | Marks | $\begin{gathered} \mathbf{Q} . \\ \text { No. } \end{gathered}$ | Marks | $\begin{gathered} \text { G. } \\ \text { No. } \end{gathered}$ | Marks | $\mathbf{~ G}$ | Marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. |  | 14. |  | 27. |  | 40. |  | 53. |  |
| 2. |  | 15. |  | 28. |  | 41. |  | 54. |  |
| 3. |  | 16. |  | 29. |  | 42. |  | 55. |  |
| 4. |  | 17. |  | 30. |  | 43. |  | 56. |  |
| 5. |  | 18. |  | 31. |  | 44. |  | 57. |  |
| 6. |  | 19. |  | 32. |  | 45. |  | 58. |  |
| 7. |  | 20. |  | 33. |  | 46. |  | $\times$ |  |
| 8. |  | 21. |  | 34. |  | 47. |  | $\times$ |  |
| 9. |  | 22. |  | 35. |  | 48. |  | $\times$ |  |
| 10. |  | 23. |  | 36. |  | 49. |  | $\times$ |  |
| 11. |  | 24. |  | 37. |  | 50. |  | $\times$ |  |
| 12. |  | 25. |  | 38. |  | 51. |  | $\times$ |  |
| 13. |  | 26. |  | 39. |  | 52. |  | $\times$ |  |
| Total Marks |  |  |  |  |  |  |  |  |  |
|  | al Marks <br> words |  |  |  |  |  |  | Total |  |
| 1. $\checkmark$ |  |  |  |  | $\checkmark$ |  |  |  |  |
| 2. $\checkmark$ |  |  |  |  |  |  |  | $\checkmark$ |  |
| Signature of Evaluators |  |  | Registration No. |  | Signature of the Deputy Chief |  |  | Signature of the Room Invigilator |  |

General Instructions :
i) The Question-cum-Answer Booklet consists of objective and subjective types of questions having 58 questions.
ii) Space has been provided against each objective type question. You have to choose the correct choice and write the complete answer along with its alphabet in the space provided.
iii) For subjective type questions enough space for each question has been provided. You have to answer the questions in the space.
iv) Follow the instructions given against both the objective and subjective types of questions.
v) Candidate should not write the answer with pencil. Answers written in pencil will not be evaluated. ( Except Graphs, Diagrams \& Maps )
vi) In case of Multiple Choice, Fill in the blanks and Matching questions, scratching / rewriting / marking is not permitted, thereby rendering to disqualification for evaluation.
vii) Candidates have extra 15 minutes for reading the question paper.
viii) Space for Rough Work has been printed and provided at the bottom of each page.
I. Four alternatives are given for each of the following questions / incomplete statements. Only one of them is correct or most appropriate. Choose the correct alternative and write the complete answer along with its alphabet in the space provided against each question.
$20 \times 1=20$

1. If $A, B$ and $C$ are non-empty sets then the 'Intersection of sets is distributive over union of sets' is represented as
(A) $\quad A \cup(B \cap C)=(A \cup B) \cap(A \cup C)$
(B) $A \cap(B \cap C)=(A \cap B) \cap(A \cap C)$
(C) $(A \cup B) \cap C=(A \cap C) \cup(B \cap C)$
(D) $(A \cap B) \cup C=(A \cup C) \cap(B \cup C)$

Ans. :
2. In a sequence, if $T_{n+1}=4 n+5$ then $T_{n}$ is
(A) $4 n-5$
(B) $4 n-1$
(C) $4 n+1$
(D) $4 n+5$.

Ans. : $\qquad$
3. Which is the correct relation ?
(A) $\frac{{ }^{n} C_{r}}{{ }^{n} P_{r}}=r$
(B) $\frac{{ }^{n} P_{r}}{{ }^{n} C_{r}}=\bigsqcup r$
(C) $\frac{{ }^{n} P_{r}}{{ }^{n} C_{r}}=r$
(D) $\frac{{ }^{n} C_{r}}{{ }^{n} P_{r}}=\bigsqcup r$.

Ans. : $\qquad$
4. The standard deviation ( $\sigma$ ), mean ( $\bar{X}$ ) are given. The formula for calculating coefficient of variation ( C.V.) is
(A) $\quad$ C.V. $=\frac{\sigma}{\bar{X}} \times 100$
(B) C.V. $=\frac{\bar{X}}{\sigma} \times 100$
(C) C.V. $=\frac{\sigma \cdot \bar{X}}{100}$
(D) $\bar{X}=\frac{\mathrm{C} . \mathrm{V} .}{\sigma} \times 100$.

Ans. : $\qquad$
5. $\quad A$ is a matrix of order $2 \times 3$ and $B$ is a matrix of order $2 \times 1$. If $A X=B$ then the order of the matrix $X$ is
(A) $1 \times 2$
(B) $3 \times 1$
(C) $2 \times 1$
(D) $1 \times 3$.

Ans. : $\qquad$
6. The H.C.F. of $\left(a^{2}-9\right)$ and $\left(a^{2}+5 a+6\right)$ is
(A) $(a-9)$
(B) $(a-3)$
(C) $(a+3)$
(D) $(a+9)$.

Ans. : $\qquad$
7. $\quad A$ and $B$ are the two algebraic expressions, $H$ and $L$ are the H.C.F. and L.C.M. of them, respectively. The correct relation among these is
(A) $H \times B=A \times L$
(B) $H+L=A+B$
(C) $H+B=A+L$
(D) $H \times L=A \times B$.

Ans. : $\qquad$
8. If $\sum a=0$ then the value of $\sum\left[(a+b)^{2}-c^{2}\right]$ is $a, b, c$
$a, b, c$
(A) 1
(B) 0
(C) 2
(D) -2 .

Ans. : $\qquad$
9. If $a+b+c=0$ then $3 a b c$ is equal to
(A) $a^{3}+b^{3}+c^{3}$
(B) $a^{2}+b^{2}+c^{2}$
(C) $-\left(a^{2}+b^{2}+c^{2}\right)$
(D) $-\left(a^{3}+b^{3}+c^{3}\right)$.

Ans. : $\qquad$
10. If $a+b+c=0$ then $a^{2}-b c$ is equal to
(A) $(a b+b c+c a)$
(B) $(a b-b c-c a)$
(C) $-(a b-b c-c a)$
(D) $-(a b+b c+c a)$.

Ans. : $\qquad$
11. Which one of the following is not a pure quadratic equation ?
(A) $x^{2}+2=6$
(B) $2 m^{2}=72$
(C) $P^{2}=9$
(D) $K^{2}=K$.

Ans. : $\qquad$
12. The area ( $A$ ) of a triangle, whose base is 4 units longer than its altitude $(x)$ is
(A) $A=\frac{1}{2} x(x-4)$
(B) $A=\frac{1}{2} x(x+4)$
(C) $A=\frac{1}{2}(4 x)$
(D) $A=\frac{1}{2}(x+4 x)$.

Ans. : $\qquad$
13. The reduced form of the surd $\sqrt[n]{a^{n+1} \cdot b^{n-1}}$ is
(A) $a b \sqrt[n]{\frac{b}{a}}$
(B) $a b \sqrt[n]{a b}$
(C) $a b \sqrt[n]{\frac{a}{b}}$
(D) $a b \sqrt[n]{a}$.

Ans. : $\qquad$
14. The sum of roots of the equation $a x^{2}+b x+c=0$ is
(A) $\frac{b}{a}$
(B) $\frac{-c}{a}$
(C) $\frac{c}{a}$
(D) $\frac{-b}{a}$.

Ans. : $\qquad$
15. In the given figure, $T A$ and $T B$ are tangents to the circle of centre $O$. If $\angle A T B=60^{\circ}$, then $\angle A O B$ is

(A) $120^{\circ}$
(B) $90^{\circ}$
(C) $60^{\circ}$
(D) $240^{\circ}$.

Ans. : $\qquad$
16. The Pythagorian triplets among the following is
(A) $8,15,17$
(B) $5,8,17$
(C) $5,12,17$
(D) $3,6,9$.

Ans. : $\qquad$
17. Two circles of radii 5 cm and 3 cm touch each other as shown in the figure. The distance between their centres is

(A) 8 cm
(B) 2 cm
(C) 5 cm
(D) 3 cm .

Ans. : $\qquad$
18. The volume ( $V$ ) of a cylinder with radius of its base ( $r$ ) and height ( $h$ ), is calculated using the formula
(A) $V=\frac{1}{3} \pi r^{2} h$
(B) $V=2 \pi r h$
(C) $V=\pi r^{2} h$
(D) $V=\pi r h$.

Ans. : $\qquad$
19. The circumference of the circular base of a cone is 50 cm . If the slant height of it is 10 cm , the curved surface area of the cone is
(A) $125 \mathrm{sq} . \mathrm{cm}$
(B) $2500 \mathrm{sq} . \mathrm{cm}$
(C) $500 \mathrm{sq} . \mathrm{cm}$
(D) $250 \mathrm{sq} . \mathrm{cm}$.

Ans. $\qquad$
20. If $\triangle A B C\left|\left|\mid D E F, \angle A=\angle D\right.\right.$ and $\angle B=\angle E$ then $\frac{\text { Area of } \triangle A B C}{\text { Area of } \triangle D E F}$ is
(A) $\frac{A C^{2}}{D F^{2}}$
(B) $\frac{A B^{2}}{D F^{2}}$
(C) $\frac{A C^{2}}{E F^{2}}$
(D) $\frac{B C^{2}}{D E^{2}}$.

Ans. : $\qquad$
II. Fill in the blanks with suitable answers :
$10 \times 1=10$
21. The formula for finding $n^{\text {th }}$ term of an Arithmetic progression, where $a=$ first term,$d=$ common difference is $\qquad$
Ans. $\qquad$
22. If $A, G, H$ are Arithmetic Mean, Geometric Mean and Harmonic Mean respectively, then $\sqrt{A H}=$ $\qquad$ .

Ans. : $\qquad$
23. If $A$ and $B$ are two matrices conformable for multiplication then $(A B)^{\prime}=$ $\qquad$ .

Ans. : $\qquad$
24. ( $\left.a^{2}+b^{2}+c^{2}\right)$ can be expressed using $\sum$ notation as $\qquad$ .

Ans. : $\qquad$
25. The discriminant ( $\Delta$ ) of a quadratic equation $a x^{2}+b x+c=0$ is $\qquad$
Ans.: $\qquad$
26. A quadratic equation in $x$ whose roots are $m$ and $n$ is $\qquad$
Ans. : $\qquad$
27. The H.C.F. of $(a+b)$ and $(a-b)$ is $\qquad$ .

Ans. : $\qquad$
28. In the figure $\angle A B C=\angle A E D=90^{\circ}, \frac{A D}{A C}=\frac{D E}{B C}=\frac{?}{?}$


Ans. : $\qquad$
29. The formula to find the surface area of a sphere is $\qquad$ .

Ans. : $\qquad$
30. Euler's formula for verifying a network is generally given by $\qquad$ .

Ans. : $\qquad$
(SPACE FOR ROUGH WORK )
III. 31. Universal set $U=\{1,2,3,4,5,6,7,9\}$ and
$A=\{x: x$ is a prime number less than 10$\}$
$B=\{x: x$ is a multiple of 3 less than 10$\}$. Verify $(A \cap B)^{\prime}=A^{\prime} \cup B^{\prime} .2$
32. Represent the following information in Venn diagram :
$n(U)=$ Number of families of TV viewers in a village $=1000$
$n(K)=$ Number of families view Kannada programmes $=800$
$n(E)=$ Number of families view Hindi programmes $=400$
$n(K \cap E)=$ Number of families view both Kannada and Hindi programmes $=300$.
Also shade the region of number of families who view neither of the programmes.
33. Three numbers are in harmonic progression. The harmonic mean between 1 st and 3 rd numbers is 20 . If the 1 st number is twice the 3 rd number then find the three terms of the progression.
34. Find the sum of the series $3+7+11+$ $\qquad$ up to 20 terms.

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35. If $\left[\begin{array}{cc}3 x^{2} & 1 \\ 3 & 2\end{array}\right]+\left[\begin{array}{cc}6 x & 5 \\ 2 & 7\end{array}\right]=\left[\begin{array}{ll}0 & 6 \\ 5 & 9\end{array}\right]$ then find $x$.
36. If $(n+1) P_{3}=120$ then find the value of $n$.
37. A square field has length of its side $(a+b)$ units. At one end of its corner a square platform is made whose length of side is $c$ units. Show that the remaining area of the field is $4 s(s-c)$ where $\frac{a+b+c}{2}=s$.
38. Find the product of $\sqrt[3]{3}$ and $\sqrt[4]{2}$. 2
39. Simplify by rationalising the denominator $\frac{5}{\sqrt{3}+\sqrt{2}}$.
40. Solve the equation $x^{2}-5 x+3=0$ by using formula.
41. If $m$ and $n$ are the roots of the equation $2 x^{2}-4 x+1=0$, find the value of $(m+$ $n)^{2}+4 m n$. 2
42. Construct Cayley's table for $S=\{2,4,6,8\}$ under multiplication modulo 10 .
43. In a circle of radius 5 cm , construct a chord of length 8 cm . Measure the distance between the centre and the chord.
44. In the given figure, name (a) a pair of direct common tangents, (b) transverse common tangent, (c) a pair of equal tangents and (d) secant.

45. Water is filled in a hemispherical vessel of radius $r$ units. If a solid spherical ball of radius $\left(\frac{r}{2}\right)$ units is immersed in it, the water spills out of the vessel. Show that the quantity of the water that spills is $\frac{\pi r^{3}}{2}$ cubic units.
46. Draw a plan of a level ground using the given information :
[ Scale : $20 \mathrm{~m}=1 \mathrm{~cm}$ ]

|  | To C (in m ) |  |
| :---: | :---: | :---: |
|  | 140 |  |
| To D 40 | 100 |  |
|  | 80 | 60 to B |
| To E 60 | 40 |  |
|  | From A |  |

47. Draw the graph for the given matrix :

$$
\left[\begin{array}{lll}
2 & 1 & 1 \\
1 & 2 & 1 \\
1 & 1 & 2
\end{array}\right]
$$

48. Verify Euler's formula for 'Octahedron'.
IV. 49. There are 5 bowlers and 10 batsmen in a cricket club. Sharath and David are good batsmen. Since Sharath is injured he is not participating in any matches. In how many ways a team of 11 be selected so that the team contains a maximum of 7 batsmen ? 3
49. Calculate the standard deviation for the given frequency distribution :

| C.I. | $\boldsymbol{f}$ |
| :---: | :---: |
| $10-14$ | 2 |
| $15-19$ | 3 |
| $20-24$ | 5 |
| $25-29$ | 3 |
| $30-34$ | 2 |

51. Find the L.C.M. of the given expressions

$$
x^{3}-3 x^{2}-10 x+24 \text { and } x^{3}-2 x^{2}-9 x+18
$$

52. The area of an equilateral triangle whose side is $x \mathrm{~cm}$ is $16 \sqrt{3}$ sq.cm. Find the perimeter of the triangle.
53. $A D$ is the altitude from $A$ to $B C$ in the $\triangle A B C$ and $D B: C D=3: 1$. Prove that $B C^{2}=2\left(A B^{2}-A C^{2}\right)$.
54. Prove that, "if two circles touch each other externally, the point of contact and the centres of the circles are collinear".
V. 55. In a geometric progression the sum of 2 nd and 4 th terms is 30 . The difference of 6 th and 2 nd terms is 90 . Find the 8th term of a geometric progression, whose common ratio is greater than 1. 4
55. Prove that, "the areas of similar triangles are proportional to the squares of the corresponding sides." 4
56. Two circles of radii 5 cm and 3 cm , have their centres 10 cm apart. Draw two direct common tangents to the circles and measure them. 4
57. Draw the graphs of $y=x^{2}$ and $y=2 x+3$ and hence solve the equation $x^{2}-2 x-3=0$.

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