RITSAT-PILANI **ENGINEERING ENTRANCE**

A-PDFsMerger, DFMO: Purchas

Mathematics

			by	5,	the	least	positive	
remain	nder	is :						

(a) 4 (c) 2

(d) 6

2. If wis a complex cube root of unity, then

$$\begin{vmatrix}
1 & \omega & \omega^2 \\
\omega & \omega^2 & 1 \\
\omega^2 & 1 & \omega
\end{vmatrix}$$
 is equal to:

(d) w (c) 0

a. The ends of the latus rectum of the conic $x^2 + 10x - 16y + 25 = 0$ are :

(a) (3 - 4), (13 4) (b) (-3-4), (13-4) (c) (3, 4), (-13, 4) (d) (5, -8), (-5, 8)

4. The equation to the hyperbola having its eccentricity 2 and the distance between its foci

is 8, is:
(a)
$$\frac{x^2}{12} - \frac{y^2}{4} = 1$$
 (b) $\frac{x^4}{4} - \frac{y^2}{12} = 1$

(c) $\frac{x^2}{8} - \frac{y^2}{2} = 1$ (d) $\frac{x^2}{16} - \frac{y^2}{9} = 1$ **5.** The solution of $\sin^{-1} x - \sin^{-1} 2x = \pm \frac{\pi}{3}$ is :

(a)
$$\pm \frac{1}{3}$$
 (b) $\pm \frac{1}{4}$

(a)
$$\pm \frac{1}{3}$$

(c) $\pm \frac{\sqrt{3}}{2}$
(d) $\pm \frac{1}{2}$

6. In a \triangle ABC if the sides are a = 3, b = 5 and c = 4, then $\sin \frac{B}{2} + \cos \frac{B}{2}$ is equal to : (b) $\frac{\sqrt{3}+1}{3}$

(a)
$$\sqrt{2}$$
 (b) $\frac{1}{2}$

(c) \frac{\sqrt{3}-1}{2} (d) 1 7. The two circles $x^2 + y^2 - 2x + 22y + 5 = 0$ and $x^2 + y^2 + 14x + 6y + k = 0$ Intersect orthogonally provided k is equal to -(a) 47 (b) - 47

(c) 49 (d) -49 8. The radius of the $x^2 + y^2 + 4x + 6y + 13 = 0$ is: (a) \(\sqrt{26} \) (b) \(\sqrt{13} \)

(c) \23 (d) 0 9. The centre of the circle $x = 2 + 3\cos\theta$. $y = 3 \sin \theta - 1 \text{ is}$:

(a) (3, 3) (b) (2, -1) (c) (-2, 1) (d) (-1, 2) 10. The sum of the focal distances of any point op

the conic $\frac{x^2}{25} + \frac{y^2}{16} = 1$ is :

11. The solutions of the equation 2 5 x = 0

12. If $A = \begin{bmatrix} 3 & 5 \\ 2 & 0 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 17 \\ 0 & -10 \end{bmatrix}$, then | AB| is equal to :

equal to:
(a) 80
(b) 100
(d) 92
(c)
$$-110$$
(d) 92

13. The inverse of the matrix $\begin{bmatrix} 5 & -2 \\ 3 & 1 \end{bmatrix}$ is:

(a) $\frac{1}{11}\begin{bmatrix} 1 & 2\\ -3 & 5 \end{bmatrix}$ (b) $\begin{bmatrix} 1 & 2\\ -3 & 5 \end{bmatrix}$ (c) $\frac{1}{13}\begin{bmatrix} -2 & 5\\ 1 & 3 \end{bmatrix}$ (d) $\begin{bmatrix} 1 & 3\\ -2 & 5 \end{bmatrix}$

14. The projection of the vector $2\hat{\mathbf{i}} + \hat{\mathbf{j}} - 3\hat{\mathbf{k}}$ on the vector $\hat{\mathbf{i}} - 2\hat{\mathbf{j}} = \hat{\mathbf{k}}$ is: (a) $-\frac{3}{\sqrt{14}}$ (b) $\frac{3}{\sqrt{34}}$ (c) $-\frac{1}{\sqrt{3}}$ (d) $\frac{3}{\sqrt{2}}$ 15. If $12\cos^2 0 - 31\cos^2 0 + 32 = 0$, then the value of $\sin 0 \sin 0$ (a) $\frac{3}{5}$ or 1 (b) $\frac{2}{3}$ or $-\frac{2}{3}$	23. (0, -1) and (0, 3) are two opposite vertices q_0 square. The other two vertices are : (a) (0, 1), (0, -3) (b) (3, -1), (0, 0) (c) (2, 1), (-2, 1) (d) (2, 2), (1, 1) (24. The equation to the line bisecting the p_0 in, (3, -4) and (5, 2) and having its interceps, the x -axis and the y -axis in the ratio 2 : $1_{\mathbf{S}}$ (a) $x + y - 3 = 0$ (b) $2x - y = 9$ (c) $x + 2y - 2$ (d) $2x + y = 7$ 25. The distance between the pair of parallel $ \mathbf{x} $ $x^2 + 2y + y^2 - 8y - 9 + 9^2 + 0$ is:
(c) $\frac{4}{5}$ or $\frac{3}{4}$ (d) $\pm \frac{1}{2}$ 16. The circumradius of the triangle whose sides are 13, 12 and 5, is:	(a) $2\sqrt{5}a$ (b) $\sqrt{10}a$ (c) $10a$ (d) $5\sqrt{2}a$
are 15, 12 and 3, 12 and 3, 13 and 3, 13 and 3, 14 and 3, 15 and	26. The equation to the circle with centre (2 and touching the line $3x + 4y - 5$ is: (a) $x^2 + y^2 - 4x - 2y + 5 = 0$ (b) $x^2 + y^2 - 4x - 2y - 5 = 0$ (c) $x^2 + y^2 - 4x - 2y + 4 = 0$ (d) $x^2 + y^2 - 4x - 2y + 4 = 0$ 27. The condition for a line $y = 2x + c$ to touch
18. The amplitude of $\frac{1+i\sqrt{3}}{\sqrt{3+i}}$ is : (a) $\frac{\pi}{3}$ (b) $\frac{\pi}{4}$ (c) $\frac{2\pi}{3}$ (d) $\frac{\pi}{6}$	circle $x^2 + y^2 = 16$ is: (a) $c = 10$ (b) $c^2 = 80$ (c) $c = 12$ (d) $c^2 = 64$ 28. $\int \frac{\sin(2x)}{1 + \cos^2 x} dx$ is equal to:
19. If ${}^{\infty}C_{12} = {}^{\infty}C_{6}$, then ${}^{\infty}C_{2}$ is equal to: (a) 72 (b) 153 (c) 306 (d) 2556	(a) $-\frac{1}{2}\log(1 + \cos^2 x) + c$ (b) $2\log(1 + \cos^2 x) + c$ (c) $\frac{1}{2}\log(1 + \cos 2x) + c$
20. The middle term in the expansion of $\left(x - \frac{1}{x}\right)$	(d) $c - \log(1 + \cos^2 x)$

(b) -18C₉
(d) -18C₁₀

(b) $\frac{15}{4}$ (d) 4

21. If α , β , γ are the roots of the equation $2x^3 - 3x^2 + 6x + 1 = 0$, then $\alpha^2 + \beta^2 + \gamma^2$ is

22. If a b and c are mutually perpendicular unit

vectors, then $|\vec{a} + \vec{b} + \vec{c}|$ is equal to: (a) 3 _____ (b) $\sqrt{3}$

(c) $(\sqrt{a^2 + b^2 + c^2})$

equal to :

(a) - 15

29. $\int \frac{e^x(1+\sin x)}{1+\cos x} dx$ is equal to:

(a) $e^x \tan\left(\frac{x}{2}\right) + c$

(c) $e^x \left(\frac{1 + \sin x}{1 - \cos x} \right) + c$

30. $\int_{\pi/4}^{\pi/2} \csc^2 x \, dx$ is equal to :

(b) 1

(d) $\frac{1}{2}$

(d) $c - e^x \cot\left(\frac{x}{2}\right)$

(a) - 1

(c) 0

(b) $e^x \tan x + c$

- 1. (3/4 log (1 + tan x) dx is equal to 1
 - (a) $\frac{\pi}{8} \log_e 2$ (b) $\frac{\pi}{4} \log_2 e$

 - (c) $\frac{\pi}{4} \log_{\epsilon} 2$ (d) $\frac{\pi}{8} \log_{\epsilon} (\frac{1}{2})$
- 32. The modulus and amplitude of $\frac{1+2i}{2}$ are:
- (a) $\sqrt{2}$ and $\frac{\pi}{2}$ (b) 1 and 0
- (c) 1 and $\frac{\pi}{2}$ (d) 1 and *
- 33. $\lim_{x \to 0} \frac{\tan x \sin x}{x}$ is equal to :
 - (b) $-\frac{1}{2}$
 - (a) $\frac{1}{2}$
- 34. If $f(x) = \begin{cases} \frac{\sin 5x}{x^2 + 2x}, & x \neq 0 \\ k + \frac{1}{2}, & x = 0 \end{cases}$
- r = 0, then the value of k is :
 - (a) 1
 - (c) 2
- 35. The area bounded by the parabola y2 = 4ax and the line x = a and x = 4a is:
 - (c) 7a2
- (b) 4a* (d) $\frac{56a^2}{a^2}$
- 36. A population p(t) of 1000 bacteria introduced into nutrient medium grows according to the relation $p(t) = 1000 + \frac{8^{2008} \text{ according to the}}{1000 + t^2}$. The maximum
 - size of this bacterial population is: (b) 1250 (a) 1100 (d) 5250
- (c) 1050 37. The differential equation representing a family of circles touching the y-axis at the origin is:
 - (a) $x^2 + y^2 2xy \frac{dy}{dx} = 0$
 - (b) $x^2 + y^2 + 2xy \frac{dy}{dx} = 0$
 - (c) $x^2 y^2 2xy \frac{dy}{dx} = 0$ (d) $x^2 - y^2 + 2xy \frac{dy}{dx} = 0$
- 38. The general solution of the differential equation (2x - y + 1) dx + (2y - x + 1) dy = 0

- (a) $x^2 + y^2 + xy x + y = c$
- (b) $x^2 + y^2 xy + x + y = c$ (c) $x^2 - y^2 + 2xy - x + y = c$
- (d) $x^2 y^2 2xy + x y = 0$
- 39. If $y = \tan^{-1} \frac{\sqrt{1 + x^2} \sqrt{1 x^2}}{\sqrt{1 + x^2} + \sqrt{1 x^2}}$, then dy is equal to :
 - (a) $\frac{x^2}{\sqrt{1-x^4}}$ (b) $\frac{x^2}{\sqrt{1+x^4}}$
 - (c) $\frac{x}{\sqrt{1+x^4}}$ (d) $\frac{x}{\sqrt{1-x^4}}$

 - 40. If $x = \sin t$, $y = \cos pt$, then: (a) $(1-x^2)y_2 + xy_1 + n^2y = 0$
 - (b) $(1 x^2) y_0 + xy_1 p^2 y = 0$ (c) $(1 + x^2) y_0 = xy_1 + p^2 y = 0$
 - (d) $(1 x^2) y_2 xy_1 + p^2 y = 0$
 - 41. If ST and SN are the lengths of the subtangent
 - and the subnormal at the point $\theta = \frac{\pi}{2}$ on the curve $x = a(\theta + \sin \theta)$, $y = a(1 - \cos \theta)$, $a \neq 1$, then:
 - (a) ST = SN(c) $ST^2 = a SN^3$ (d) $ST^3 = aSN$
 - 42. If θ is the acute angle of intersection at a real point of intersection of the circle $x^2 + y^2 = 5$ and the parabola $y^2 = 4x$, then $\tan \theta$ is equal
 - (a) 1 (c) 3
 - 43. Universal set. $U = \{x \mid x^5 - 6x^4 + 11x^3 - 6x^2 = 0\}$
 - $A = \{x \mid x^2 5x + 6 = 0\}$
 - $R = \{x | x^2 3x + 2 = 0\}$ what is $(A \cap B)'$ equal to?
 - (b) {1, 2, 3} (a) {1, 3} (d) {0, 1, 2, 3}
 - (c) {0, 1, 3} 44. Which of the following statements is not correct for the relation R defined by aRb, if and
 - only, if b lives within on kilometre from a? (a) R is reflexive (b) R is symmetric
 - (c) R is not anti-symmetric (d) None of the above

are surbar is the value of $\frac{(1001)_2^{(11)_2} - (101)_2^{(11)_2}}{(1001)_2^{(10)_2} + (1001)_2^{(01)_2} (101)_2^{(01)_2} + (101)_2^{(10)_2}}?$ (a) (1001). (h) (101). (c) (110), (d) (100).

Physics

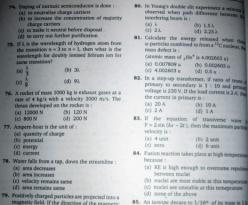
- 46. The angle turned by a body undergoing circular motion depends on time as $\theta = \theta_0 + \theta_0 t + \theta_0 t^2$. Then the angular acceleration of the body is (b) 0-
 - (a) B (d) 20, (c) 28.
- 47. The moment of inertia of a circular disc about an axis passing through the circumference perpendicular to the plane of the disc is :
 - (a) MR2
 - (c) MR2
- 48. A body of mass 5 kg is suspended by a spring balance on an inclined plane as shown in figure. The spring balance measure : (a) 50 N (b) 25 N
 - (c) 500 N (d) 10 N
- 49. Under the action of a force F = Cx, the position of a body changes from 0 to x. The work done is:
 - (a) $\frac{1}{2} Cx^2$ (c) Cx
- (h) Cx2
- (d) 1 Cx
- 50. If A B = A × B, then angle between A and B is:
 - (a) 45° (b) 30° (c) 60° (d) 90°
- 51. Each resistance shown in figure is 2Ω . The equivalent resistance between A and B is :



- (a) 2Ω (b) 4 \O (d) 10
- 52. A physical quantity is given by X = [M³] The percentage error in measurement of w and T are a, B and y respectively. Then maximum % error in the quantity X is : (a) a α + bβ + cγ (b) a α + bβ - cγ
- (d) none of these
- 53. If emf induced in a coil is 2 V by changing current in it from 8 A to 6 A in 2 x 10-3 s H the coefficient of self induction is :
 - (a) 2×10⁻³ H (b) 10⁻³ H (c) 0.5 × 10⁻³ H (d) 4 × 10⁻³ H
- 54. A hollow metallic sphere of radius R is given charge Q. Then, the potential at the centre's
 - (a) zero (b) $\frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{R}$ (c) $\frac{1}{4\pi\epsilon_0} \cdot \frac{2Q}{R}$ (d) $\frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{2R}$
- 55. Susceptibility of ferromagnetic substance is (a) > 1 (b) < 1
- (c) zero (d) 1 56. What is the refractive index of a prism wh angle A = 60° and angle of minimum devid = 30° ?
 - (a) $\sqrt{2}$
 - (c) 1
- 57. A satellite of mass m is placed-at a dista from the centre of earth (mass M). mechanical energy of the satellite is:
- 58. A cell of constant emf first connected I resistance R1 and then connected resistance R2. If power delivered in both 6

- is same then the internal resistance of the cell
- (a) JR.R. (c) $\frac{R_1 - R_2}{R_1 - R_2}$
- (b) $\sqrt{\frac{R_1}{R_2}}$ (d) $R_1 + R_2$
- co. Energy gas between valence band and conduction band of a semiconductor is :
 - (a) zero (b) infinite (c) 1 eV (d) 10 eV
- so. At what point of a projectile motion. acceleration and velocity are perpendicular to each other ?
 - (a) At the point of projection (b) At the point of drop
 - (c) At the top most point
 - (d) Anywhere in between the point of projection and top most point
- 61. An object is placed at a distance 20 cm from the pole of a convex mirror of focal length 20 cm. The image is produced at :
 - (b) 20 cm (a) 13.3 cm
 - (d) 10 cm
- 62. Angular momentum is conserved :
 - (a) always
 - (b) never (c) when external force is absent
- (d) when external torque is absent 63. The plano-convex lens of focal length 20 cm and 30 cm are placed together to form a double
 - convex lens. The final focal length will be : (a) 12 cm
 - (b) 60 cm (d) 30 cm
- (c) 20 cm 64. Initially two gas samples 1 and 2 are at the same condition. The volume of the two are halved, one isothermally and the other adiabatically. What is the relation between the final pressure P1 and P2?
 - (a) $P_1 = P_2$
 - (b) P > P
 - (d) Cannot be determined
- 65. A can is taken out from a refrigerator at 0°C. The atmospheric temperature is 25°C. If t1 is the time taken to heat from 0°C to 5°C and t2 is the time taken from 10°C to 15°C, then :
 - (a) t1 > t2
- (b) t1 < t2
- (d) there is no relation

- 66. A simple pendulum hanging from the ceiling of a stationary lift has time period; . When the lift moves downward with constant velocity the time period is t 2, then : (a) to is infinity (b) t2>t1
 - (c) to < to (d) t2=t1
- 67. Two progressive waves having equation $x_1 = 3 \sin \omega \tau$ and $x_2 = 4 \sin (\omega \tau = 90^\circ)$ are super imposed. The amplitude of the resultant wave is -
 - (a) 5 unit (b) 1 unit (c) 3 unit (d) 4 unis
- 68. In a magnetic field of 0.05 T area of coil changes from 101 cm2 to 100 cm2 without changing the resistance which is 20. The amount of charge that flow during this period
 - (b) 2 x 10-6 C (a) 2.5 × 10⁻⁶ C
- (c) 10-6 C (d) 8 × 10-6 C 69. A dielectric is introduced in a charged and isolated parallel plate capacitor, which of the following remains unchanged?
 - (a) Energy (b) Charge
 - (c) Electric field
- (d) Potential difference 70. If in a triode valve amplification factor is 20 and plate resistance is 10 kQ, then its mutual
 - conductance is:
 - (a) 2 milli mho (b) 20 milli mho
 - (c) (1/2) milli mho (d) 200 milli mho
 - 71. Which of the following is a fusion reaction? (a) $_{1}H^{2} + _{1}H^{2} \rightarrow _{2}He^{4}$
 - (b) $_{1}H^{2} + _{1}H^{2} \rightarrow 2(_{1}He^{2})$
 - (c) $_{1}H^{1} + _{3}H^{1} \rightarrow _{2}He^{4}$ (d) $_{1}H^{1} + _{1}H^{2} \rightarrow _{2}He^{4} + n$
 - 72. The correct relation between α and β in a transistor is:
 - (b) $\beta = \frac{\alpha}{1 + \alpha}$ (a) $\beta = \frac{\alpha}{1-\alpha}$
 - (c) $\beta = \frac{1+\alpha}{\alpha}$ (d) $\beta = 1 - \alpha$
 - 73. Which of the following law states that "good absorbers of heat are good emitters"? (b) Kirchhoff's law (a) Stefan's law
 - (d) Wien's law (c) Planck's law



- magnetic field. If the direction of the magnetic field is along the direction of motion of the charge particles, the particles get :
- (a) accelerated
- (b) decelerated
- (c) deflected
- (d) no changed in velocity

Chemistry

86. The crystal field splitting energy for octahedral (Δ.) and tetrahedral (Δ.) complexes is related

(b)
$$\Delta_t = \frac{1}{2} \Delta_o$$

(c)
$$\Delta_o = 2\Delta_o$$

(d)
$$\Delta_o = \frac{4}{9} \Delta$$

(a) 15 min

87. What is the product A in the following?

- Cl + Mg -- A

What is the half-life period of the isotope?

(c) 12 min (d) 10 min

(b) 30 min

ss. Which of the following species has a bond order other than 3?

(a) CO (b) CN (c) NO (d) O:

(c) NO (d) O₂

39. The number of waves in an orbit are:

(a) n² (b) n (c) n-1 (d) n-2

90. When glucose reacts with bromine water the main product is:

(a) gluconic acid (b) glyceraldehyde (c) sorbitol (d) saccharic acid

91. The ion which exhibits green colour?
(a) Cu²⁺
(b) Mn²⁺

(a) Cu²⁺ (b) Mn²⁺ (c) Co²⁺ (d) Ni²⁺ 92. The probability of finding the electron in the

orbital is: (a) 100% (b) 90-95%

(c) 70–80% (d) 50–60% 93. Which destroy antigens ?

(a) Insulin (b) Antibodies
(c) Chromoprotein (d) Phosphoprotein

94. In 2HI — H₂ + I₂, the forward reaction is not affected by change in :

(a) catalyst (b) pressure
(c) volume (d) temperature

95. Nylon-66 is an example of :

(a) poly propylene (b) polyester

(c) polyamide (d) polystyrene

96. 1 mole of N₂O₄(g) at 300 K is kept in a closed container under one atmosphere. It is heated to

container under one atmosphere. It is heated to 600 K when 20% by mass of N₂O₄(g) decomposes to NO₂(g). The resultant pressure

is:
(a) 1.2 atm
(b) 2.4 atm

(c) 2.0 atm (d) 1.0 atm

97. A hypothetical reaction A → 2B, proceeds

through following sequence of steps: (i) $A \longrightarrow C$; $\Delta H = q$

(ii) $C \longrightarrow D$; $\Delta H = V$ (iii) $\frac{1}{5}D \longrightarrow B$; $\Delta H = X$

(iii) $\frac{1}{2}D \longrightarrow B$, B?

Then the heat of reaction is:

(a) q - v + 2x (b) q + v - 2x(c) q + v + 2x (d) q + 2v - 2x 98. Following reaction is :



(a) S_N (b) S_E
(c) E1 (d) EI-CB

99. The cathodic reaction of a dry cell is

represented by $2MnO_2(s) + Zn^{2s} + 2e^- \longrightarrow ZnMn_2O_2(s)$

 $2MnO_2(s) + Zn^{2s} + 2\varepsilon \longrightarrow ZnMn_2O_4(s)$ If, there are 8 g of MnO_2 in the cathodic

compartment then the time for which the dry cell will continue to give a current of 2 milliampere is:

(a) 25.675 day

(b) 51.35 day

(c) 12.8 day (d) 6.423 day

100. On heating with oxalic acid at 110°C, glycerine gives:

gives : (a) glyceryl trioxalate

(b) formic acid

(c) glyceryl dioxalate (d) none of the above

101. Which of the following is not the example of pseudounimolecular reactions?

(a) $CH_3COOC_2H_5 + H_2O \xrightarrow{H^*} CH_3COOH + C_2H_3OH$

(b) $C_{12}H_{22}O_{11} + H_2O \xrightarrow{H^*} C_6H_{12}O_6 + C_6H_{12}O_6$ $C_6H_{12}O_6 + C_6H_{12}O_6$ (Fluctose)

(c) $CH_3COCl + H_2O \longrightarrow CH_3COOH + HCl$

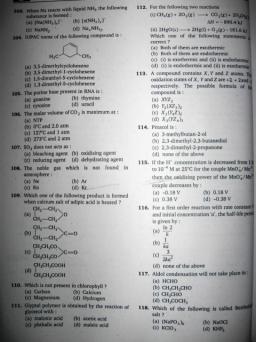
(d) $CH_3COOC_2H_5 + H_2O \xrightarrow{CH_3COOH} + C_2H_5OH$

102. The compound, whose stereo-chemical formula is written below, exhibits x geometrical isomers and y optical isomers.

 CH_3 $C = C < H_2 - CH_2 - CH_3$

The values of x and y are:
(a) 4 and 4
(b) 2 and 2

(a) 4 and 4 (b) 2 and 2 (c) 2 and 4 (d) 4 and 2



119. Which of the following is a Boyle plot at very low pressure?



120. Calgon used as water softner is :
(a) Na_INa_(PO_2)_c1 (b) Na_INa_(PO_2)_c1

(c) Na₂[Na₄(PO₄)₅] (d) none of these 121. How many asymmetric carbon atoms are

- present in :
 (i) 1.2-dimethylcyclohexane.
 - (ii) 3-methylcyclopentene and (iii) 3-methylcyclohexene?

- (a) two, one, one (b) one, one one (c) two, none, two (d) two, none, one
- 122. For which order half-life period is independent of initial concentration?

 (a) Zaro.

(c) Second (d) Third 123. In the reaction

CH₃CN + 2H HCl X boiling H₂O

The term Y is :

(a) acetone (b) ethanamine (c) acetaldehyde (d) dimethyl amine

124. The speices that undergoes disproportionation in an alkaline medium is:

(a) MnO₄² (b) ClO₄² (c) NO₂ (d) all of these

125. On shaking H₂O₂ with acidified potassium

dichromate and ether, etheral layer becomes:

(a) green (b) red

(c) blue (d) brown

English

Directions: Read the following passage carefully and answer the questions given below it.

PASSAGE

India is a country which has been subjected to foreign invasions since the dawn of Indian history. The fertile plains of India have been attracting avaricious tribals from all over the world. Long back the Aryans from Central Asia invaded India and settled down permanently in this beautiful land where food and fodder were available in plenty. After a chain of invasions from the bordering countries through land routes, the European nations, including the British, finally came to India to exploit her rich resources. The Englishmen came to India as traders but stealthily became her masters. India became the 'brightest Jewel' in the British diadem. They proclaimed to civilise her and started to exploit her. Neither the imperialist might, nor the treachery of some of her sons, nor the treachery of some of her sons, nor the nerve-racking exploitation could cuth the indomitable urge for freedom of the prople who bid defiance to time. They fought and fought hertically, they never submitted. Their surugel for independence is an inspiring and exhilarating story. It is a story not only dot determination and will but also of sacrifice and suffering, a story of herpism and courage that happens in all Irevolutionaries.

- 126. Why did the Aryans settle permanently in
- India?

 (a) Because here food and fodder were available in plenty
 - (b) Because they invaded India
 - (c) Because here food was available in plenty (d) Because here fooder was available in
- plenty 127, British came to India:
 - (a) to exploit her rich resources
 - (b) to become her master
 - (c) to civilise her
 - (d) none of the above

- 128. The Indians indomitable urge for freedom could be curbed neither : (a) by the nerve-racking exploitation of the
 - (b) by the treachery of some of her sons
 - (c) by the imperialist might
 - (d) all of the above
 - Directions: In the following questions, out of the four alternatives choose the one which is most opposite in meaning to the word given in
- capital letters. 129, INGRATITUDE : (a) Stimulation
- (b) Reward (d) Thankfulness (b) Narrow
- (c) Sympathy 130. GIGANTIC:
- (a) Tiny (c) Vulgar
- (d) Attentive 131. COLOURLESS:
 - (a) Resolute
 - (b) Steadfast (d) Terrible (c) Pleasant Directions: Choose the word which is most
 - nearly the same in meaning to the word given in capital letters.
- 132 CONNOISSEUR -
 - (a) Lover of art (b) Interpreter (d) Jenorant
- (c) Delinquent 133. LETHAL : (a) Unlawful
 - (b) Sluggish (d) Smooth
- (c) Deadly 134. PICTURESOUE:
 - (a) Photogenic
 - (b) Ugly (c) Simple
 - (d) Stimulating
 - Directions: The following sentences have been divided into three parts (a), (b), (c). One of the parts may contain an error. Write down the part of the sentence that has an error. If there is No error., mark (d) as your answer.

- Whenever is the matter I shall 135 do this work because I have
 - to expose my working capacity at any cour

 - She is so lazy as she cannot
- 126 do this work properly and
 - cannot cooperate us in your scheme.
 - No error
- Directions: Each of the idioms or phrases is followed by four meanings out of which only one is correct. Pick out the correct meaning. 137. A hard put to crack :
 - (a) Difficult things require extra effort
 - - (c). A difficult problem solved effortlessly (d) Costly things need careful handling
- 138. To beat about the bush :
 - (b) Vigorous search for the culprit
 - (c) Easily achieved success without much
 - (d) Working hard to achieve the goal Directions: Choose the suitable preposition
- from the given alternatives to fill in the blanks in the following sentences.
- 139. So many servants attended him during his
 - (a) with (b) on (c) for (d) to
- 140. At last he yielded the tempfation.
 - (a) on (b) off (c) for (d) to

Reasoning

- 141. Kilogram is related to Quintal in the same way as Paisa is related to :
 - (a) Rupee (b) Coin
 - (c) Wealth
 - (d) Money

- 142. In the following question four groups of letters are given. Three of them are alike in a certain way while one is different. Select the one which is different.
 - (a) xXYA (c) hHIR
- (b) ilMP (d) DBCE

143. Select a figure from the four alternatives, which when placed in the blank space of fig. (x) would complete the pattern.









Statement: The data given by the U.S.

44. Labour Ministry indicate that till the year 2000.
there will be a shortage of 1,00,000
programmers. A spokesman from the industry
said, "We should understand this throughly
America needs Indian programmers. This is not
only the question of investment but also of the
talent with which the Indian programmers are
equipped."

Conclusions:

- (a) In other sectors also, there will be shortage of the talented labour till the year 2000.
- (b) Indian programmers are the most talented in the world
- (c) Indian programmers are available on comparatively less salary in comparison to the programmers from other countries.
- (d) Inspite of entering with huge capital in the Software Training Sector, U.S. could not be able to meet its own needs fully.
- 145. Consider the following three figures, marked X, Y, Z showing one fold in X, another in Y and cut in Z. From amongst the answer figures A, B, C and D, select the one, showing the unfolded position of Z.





Direction: In the following question, choose the set of figures which follows the given rule. 146. Closed figure becomes more and more open.



Direction: In the following question, find out which of the figures (a), (b), (c) and (d) can be formed from the pieces given in (X).

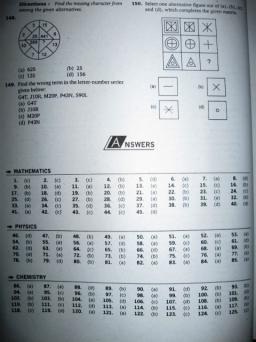
147.



(p) \[\sum_{(a)} \[\sum_{(b)} \]







126.	(a)	127.	(a)	128.	(m)	120	-								
134.	(a)	135.	(8)	128. 136.	(a)	137.	(p)	130.	(a) (a)	131.	(c)	132.	(a)	133.	(c)
# RE											(0)	140.	(d)		

→ RE															
141. 149.	(a) (b)	142. 150.	(d)	143.	(d)	144.	(b)	145.	(c)	146.	(a)	147.	(a)	148.	(a)



Mathematics

- 1. Since $2^1 = 2$, $2^2 = 4$, $2^3 = 8$, $2^4 = 16$, $2^5 = 32$. It is clear that unit place is repeated after every four power.
 - 2301 (24.75.2 Then. = (1675.2
 - .. Digit at unit place in (16)75 is 6.
 - .. Digit at units place in 2301
 - digit at units place in (6)-2
 - Hence, the remainder, when 2301 is divided by
- 5. is 2.
- $\begin{array}{c|cccc} & & & & & & & & & \\ & & & & & & & & \\ \hline 0 & \omega & & & & & \\ 0 & \omega^2 & 1 & & & \\ 0 & 1 & \omega & & & \\ \hline \end{array} \quad \begin{bmatrix} \ddots & 1 + \omega + \omega^2 = 0 \end{bmatrix}$
- 3. Given that $x^2 + 10x - 16y + 25 = 0$ $(x + 5)^2 = 16x$
 - - where X = x + 5, A = 4, Y = y.

- The ends of the latus rectum are (2A, A) and (-2A, A)
- x + 5 = 2(4)x = -8 - 5 = 3 y = 4
- and x + 5 = -2(4)= r = -8 - 5 = -13 v = 4
- (3.4) and (-13.4).
- 4. Let the equation of hyperbola is
 - $\frac{x^2}{x^2} \frac{y^2}{x^2} = 1$
 - Given e = 2 2ae = 8
 - $ae = 4 \Rightarrow a = 2$
 - $h^2 = a^2 (e^2 1)$ Now.
 - $h^2 = 4(4-1)$
 - $b^2 = 12$
 - : Equation of hyperbola is
 - $\frac{x^2}{1} \frac{y^2}{12} = 1$
- 5. $\sin^{-1} x \sin^{-1} 2x = \pm \frac{\pi}{2}$
 - $\Rightarrow \sin^{-1} x \sin^{-1} \left(\pm \frac{\sqrt{3}}{2} \right) = \sin^{-1} 2x$ $\Rightarrow \sin^{-1} \left[x \sqrt{1 - \frac{3}{4}} - \left(\pm \frac{\sqrt{3}}{2} \sqrt{1 - x^2} \right) \right] = \sin^{-1} 2x$

 - $\Rightarrow \frac{x}{2} \left(\pm \frac{\sqrt{3}}{2} \sqrt{1 x^2}\right) = 2x$
 - $-(\pm\sqrt{3}\sqrt{1-x^2})=3x$

On squaring, both sides we get,

$$3(1 - x^2) = 9x^2$$

$$\Rightarrow 1 = x^2 = 3x^2$$

$$\Rightarrow 4x^2 = 1$$

$$\Rightarrow x = \pm \frac{1}{2}$$

6. We know,
$$\cos B = \frac{a^2 + c^2 - b^2}{2ac}$$

$$\therefore \cos B = \frac{3^2 + 4^2 - 5^2}{2(3)(4)} = \frac{9 + 16 - 25}{2(3)(4)} = \frac{8 - 90^\circ}{2(3)(4)} = \frac{8 - 90^\circ}{1}$$

$$\therefore \sin \frac{B}{2} + \cos \frac{B}{2} = \sin 45^\circ + \cos 45^\circ$$

$$= \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} = \sqrt{2}$$

7. By using the condition that, if two circles are intersect orthogonally, then

$$2(g_1g_2 + f_1f_2) = c_1 + c_2$$

where $g_1 = -1$, $f_1 = 11$, $c_1 = 5$

 $g_n = 7$, $f_2 = 3$, $c_1 = k$ and 2(-1.7 + 11.3) = 5 + k

2(26) - 5 + 4

k = 47

8. Given equation is

$$x^2 + y^2 + 4x + 6y + 13 = 0$$

or $(x^2 + 4x + 4) + (y^2 + 6y + 9) + 13 = 4 + 9$
or $(x + 2)^2 (y + 3)^2 = 0$

.. Radius of circle = 0

9. Given parametric equations are $x = 2 + 3\cos\theta, y = 3\sin\theta - 1$ $\cos \theta = \frac{x-2}{3}$, $\sin \theta = \frac{y+1}{3}$

Since, $\sin^2 \theta + \cos^2 \theta = 1$

 $\Rightarrow \left(\frac{x-2}{3}\right)^2 + \left(\frac{y+1}{2}\right)^2 = 1$

 $(x-2)^2 + (y+1)^2 - 3^2$.: Centre of circle is (2, -1)

10. We know, if P is any point on the curve, then Sum of focal distances = length of major axis i.e., SP + S'P = 2a

$$= 2(5)$$
 [$\because a^2 = 5^2$]

11. Since,
$$\begin{vmatrix} x & 2 & -1 \\ 2 & 5 & x = 0 \\ -1 & 2 & x \end{vmatrix} = 0$$

$$\Rightarrow \begin{vmatrix} x & 2 & -1 \\ 2 & 5 & x \\ -3 & -3 & 0 \end{vmatrix} = 0 \quad R_3 \rightarrow R_3 - R_2$$

$$\Rightarrow -1(-6+15) - x[-3x+6] = 0$$

 $-9 + 3x^2 - 6x = 0$ $y^2 - 2x - 3 = 0$

(x-3)(x+1)=0

12. $A = \begin{bmatrix} 3 & 5 \\ 2 & 0 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 17 \\ 0 & -10 \end{bmatrix}$ $AB = \begin{bmatrix} 3 & 5 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} 1 & 17 \\ 0 & -10 \end{bmatrix}$

 $=\begin{bmatrix} 3+0 & 51-50 \\ 2+0 & 34-0 \end{bmatrix} =\begin{bmatrix} 3 & 1 \\ 2 & 34 \end{bmatrix}$ $|AB| = \begin{vmatrix} 1 & 1 \\ 2 & 24 \end{vmatrix}$

=102 - 2-100

13. Let $A = \begin{bmatrix} 5 & -2 \\ 3 & 1 \end{bmatrix}$

|A| = 5 + 6 = 11and adj $A = \begin{bmatrix} 1 & 2 \\ 2 & 2 \end{bmatrix}$

 $A^{-1} = \frac{1}{|A|} (adj A)$

 $=\frac{1}{11}\begin{bmatrix} 1 & 2 \\ -3 & 5 \end{bmatrix}$

14. Let $\vec{a} = 2\hat{i} + \hat{j} - 3\hat{k}$ and $\vec{b} = \hat{i} - 2\hat{j} + \hat{k}$

Projection of \vec{a} on $\vec{b} = \frac{\vec{a} \cdot \vec{b}}{\vec{b}}$

 $= \frac{(2\hat{\mathbf{i}} + \hat{\mathbf{j}} - 3\hat{\mathbf{k}}) \cdot (\hat{\mathbf{i}} - 2\hat{\mathbf{j}} + \hat{\mathbf{k}})}{\sqrt{1^2 + (-2)^2 + 1^2}}$ $=\frac{2-2-3}{\sqrt{6}}=-\frac{3}{\sqrt{6}}$

 $12 \cot^2 \theta - 31 \csc \theta + 32 = 0$ 15. $12\cos^2\theta - 31\sin\theta + 32\sin^2\theta = 0$ \Rightarrow 12 (1 - sin² θ) - 31 sin θ + 32 sin² θ = 0

20 sin2 0 - 31 sin 0 + 12 = 0 This is a quadratic equation in sin 0.

$$\sin \theta = \frac{31 \pm \sqrt{31^2 - 4 \cdot 20 \cdot 12}}{2 \cdot 20}$$

$$= \frac{31 \pm \sqrt{961 - 960}}{40} = \frac{31 \pm 1}{40}$$

$$\Rightarrow \sin \theta = \frac{4 - 3}{60} = \frac{31 \pm 1}{40}$$

16 Let sides are a = 13, b = 12, c = 5 $a^2 = b^2 + c^2$

Now $(13)^2 = (12)^2 + 5^2$

169 - 169

/A = 90°

We know, $R = \frac{u}{2 \sin A}$

$$R = \frac{13}{2 \cdot \sin 90^{\circ}} = \frac{13}{2}$$

17. Given that,
$$\sin x - \cos x = \sqrt{2}$$

$$\Rightarrow \frac{1}{\sqrt{2}} \sin x - \frac{1}{\sqrt{2}} \cos x = 1$$

$$\sqrt{2} \qquad \sqrt{2}$$

$$\Rightarrow \sin 45^{\circ} \sin x - \cos 45^{\circ} \cos x = 1$$

$$\Rightarrow \cos\left(x + \frac{\pi}{4}\right) = -1$$

$$\Rightarrow \cos\left(x + \frac{\pi}{4}\right) = \cos\left(\pi\right)$$

$$x + \frac{\pi}{4} = 2n\pi + \pi$$

$$\Rightarrow x = 2n\pi + \frac{3\pi}{4}$$

18. Let
$$z = \frac{1 + i\sqrt{3}}{\sqrt{3} + i}$$

$$= \frac{1+i\sqrt{3}}{(\sqrt{3}+i)} \times \frac{(\sqrt{3}-i)}{(\sqrt{3}-i)}$$

$$= \frac{\sqrt{3}-i+3i+\sqrt{3}}{3+1} = \frac{\sqrt{3}+i}{2}$$

$$amp(z) = tan^{-1} \left(\frac{1}{\sqrt{3}}\right)$$

19. Given that
$${}^{n}C_{12} = {}^{n}C_{6}$$
 or ${}^{n}C_{n-12} = {}^{n}C_{6}$

$$\Rightarrow n-12=6$$

$$n-12=6$$

$$n=18$$

$$n = 18$$
 $C_2 = \frac{18 \times 17}{2 \times 1}$

20. The general term in the expansion $\left(x-\frac{1}{x}\right)^{11}$ is given by

$$T_{r+1} = {}^{18}C_r(x)^{18-r} \left(-\frac{1}{x}\right)^r$$

.. The middle term is
$$T_{9+1}$$
, where $r = 9$
.. $T_{9+1} = {}^{18}C_9 (-1)^9 x^{18-2r}$
 $= -{}^{18}C_9 x^{18-18} = -{}^{18}C_9$

21. Since,
$$\alpha$$
, β , γ are the roots of the equation
$$2x^3 - 3x^2 + 6x + 1 = 0.$$

then
$$\alpha + \beta + \gamma = \frac{3}{2}$$
 ...(i) $\alpha\beta + \beta\gamma + \gamma\alpha = 3$...(ii)

$$\alpha\beta\gamma = -\frac{1}{2}$$
 ...(iii)
On squaring Eq. (i), we get

$$\alpha^{2} + \beta^{2} + \gamma^{2} + 2(\alpha\beta + \beta\gamma + \gamma\alpha) = \frac{9}{4}$$

 $\alpha^{2} + \beta^{2} + \gamma^{2} = \frac{9}{4} - 2(3)$ [from (ii)]

$$= \frac{9}{4} - 6 = -\frac{15}{4}$$

22. Since, a, b and c are mutually perpendicular to each other, then a-b=b.c=c.a-0

$$|\vec{\mathbf{a}} + \vec{\mathbf{b}} + \vec{\mathbf{c}}|^2 = (\vec{\mathbf{a}} + \vec{\mathbf{b}} + \vec{\mathbf{c}}) \cdot (\vec{\mathbf{a}} + \vec{\mathbf{b}} + \vec{\mathbf{c}})$$

 $[\because |\vec{\mathbf{a}}|^2 = \vec{\mathbf{a}} \cdot \vec{\mathbf{a}}]$

$$= |\vec{a}|^2 + |\vec{b}|^2 + |\vec{c}|^2 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a})$$

= 1 + 1 + 1 + 2(0 + 0 + 0)

$$[\because \vec{\mathbf{a}} \cdot \vec{\mathbf{b}} = \vec{\mathbf{b}} \cdot \vec{\mathbf{c}} = \vec{\mathbf{c}} \cdot \vec{\mathbf{a}} = 0]$$
$$|\vec{\mathbf{a}} + \vec{\mathbf{b}} + \vec{\mathbf{c}}|^2 = 3$$

$$|\vec{\mathbf{a}} + \vec{\mathbf{b}} + \vec{\mathbf{c}}| = \sqrt{3}$$

$$|\vec{\mathbf{a}} + \vec{\mathbf{b}} + \vec{\mathbf{c}}| = \sqrt{3}$$

$$|\vec{\mathbf{a}} + \vec{\mathbf{b}} + \vec{\mathbf{c}}| = \sqrt{3}$$

$$|\vec{\mathbf{a}} + \vec{\mathbf{c}}| = \sqrt{3}$$

$$|\vec{\mathbf{a}} + \vec{\mathbf{c}}| = \sqrt{3}$$

23. Let the points be $B(x_3, y_1)$ and $D(x_2, y_2)$ mid point of $BD = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$

$$D(x_0, y_0)$$
 $C(0,3)$ $B(x_0, y_0)$

We know, mid point of both the diagonal lie on the same point E.

$$\Rightarrow \frac{x_1 + x_2}{2} = 0 \text{ and } \frac{y_1 + y_2}{2} = 1$$

$$\Rightarrow x_1 + x_2 = 0$$

$$x_1 + x_2 = 0 \qquad ...(i)$$
and
$$y_1 + y_2 = 2 \qquad ...(ii)$$
Slope of $BD \times$ slope of $AC = -1$

...(iii)

$$\frac{(y_1 - y_2)}{(x_1 - x_2)} \times \frac{(3+1)}{(0-0)} = -1$$

$$\Rightarrow y_1 - y_2 = 0$$

Solving Eqs. (ii) and (iii), we get
$$y_1 = 1$$
, $y_2 = 1$

Now, slope of
$$AB \times$$
 slope of $BC = -1$

$$\Rightarrow \frac{(y_1 + 1)}{(x_1 - 0)} \times \frac{(y_1 - 3)}{(x_1 - 0)} = -1$$

$$\Rightarrow \frac{(x_1 - 0) \times (x_1 - 0)}{(x_1 - 0) \times (x_1 - 0)} = -1$$

$$\Rightarrow (y_1 + 1)(y_1 - 3) = -x^2$$

$$\Rightarrow 2(-2) = -x_1^2 \qquad [\because y_1 = 1]$$

$$\Rightarrow x_1 = \pm 2$$
The required points are (2, 1) and (-2, 1).

24. Let the points be A(3, -4) and B(5, 2) and mid point of AB = (4, -1)

mid point of AB = (4, -1).

It is given that the bisecting line intercept the co-ordinate axes in the ratio 2:1.

... Point of co-ordinate axes are (2k, 0) and (0, k). The equation of line passing through the above point is

$$y - 0 = \frac{k - 0}{0 - 2k} (x - 2k)$$

or
$$y = -\frac{1}{2}(x - 2k)$$
 ...(i)
Since, it is passing through the mid point of AB

Since, it is passing through the mid point of AB i. e., (4, -1)

$$-1 = -\frac{1}{2}(4-2k)$$

Putting the value of k in Eq. (i), we get

$$y = -\frac{1}{2}(x-2)$$

x + 2y = 225. Given equation is

$$x^{2} + y^{2} + 2xy - 8ax - 8ay - 9a^{2} = 0$$
or
$$x^{2} + y^{2} + (-4a)^{2} + 2xy$$

$$-8ax - 8ay - 25a^2 = 0$$

$$(x + y - 4a)^2 - (5a)^2 = 0$$

or
$$(x+y-9a)(x+y+a)=0$$

 $\Rightarrow x + y - 9a = 0$ or x + y + a = 0These lines are parallel. Now, we find a

distance from origin to the line. Let, $p_1 = \frac{0 + 0 - 9a}{\sqrt{1^2 + 1^2}}$, $p_2 = \frac{0 + 0 + a}{\sqrt{2^2 + 2^2}}$

$$\sqrt{1^2 + 1^2}$$
 $\sqrt{1^2 + 1^2}$
 $p_1 = -\frac{9a}{\sqrt{2}}, p_2 = \frac{a}{\sqrt{2}}$

$$|p_2 - p_1| = \frac{a}{\sqrt{2}} + \frac{9a}{\sqrt{2}} = \frac{10a}{\sqrt{2}}$$

= $5\sqrt{2}a$

26. Distance from centre (2, 1) to the line 3x + 4y - 5 = radius of circle

$$\Rightarrow \frac{|3(2) + 4(1) - 5|}{\sqrt{3^2 + 4^2}} = r$$

$$\Rightarrow \frac{5}{5} = r$$

⇒ r=1
∴ Equation of circle is

$$(x-2)^{2} + (y-1)^{2} = 1^{2}$$

$$\Rightarrow x^{2} + y^{2} - 4x - 2y + 4 + 1 = 1$$

$$\Rightarrow x^2 + y^2 - 4x - 2y + 4 = 0$$
27. If $y = mx + c$ touches the circle

 $x^2 + y^2 = a^2$, then $c^2 = a^2 (1 + m^2)$ Now, the line y = 2x + c touches the circle

$$x^2 + y^2 = 16$$
, if
 $c^2 = 16(1 + 4) = 16 \times 5$

or $c^2 = 80$ 28. Let $I = \int \frac{2 \sin x \cos x}{1 + \cos^2 x} dx$

Put
$$1 + \cos^2 x$$
$$1 + \cos^2 x = t$$

$$\Rightarrow -2\cos x \sin x \, dx = dt$$

$$\therefore I = \int -\frac{dt}{t} = -\log t + c$$

$$= -\log(1+\cos^2x) + c$$

29. Let
$$I = \int e^x \left(\frac{1 + \sin x}{1 + \cos x} \right) dx$$

$$= \int e^x \frac{\left(1 + 2 \sin \frac{x}{2} \cos \frac{x}{2} \right)}{2 \cos^2 x} dx$$

$$= \int \frac{1}{2} e^x \sec^2 \frac{x}{2} dx + \int e^x \tan \frac{x}{2} dx$$

$$= \frac{1}{2} \int 2e^x \tan \frac{x}{2} - \int 2e^x \tan \frac{x}{2} dx + \int e^x \tan \frac{x}{2} dx$$

$$e^{t} \tan \frac{x}{2} - \int e^{x} \tan \frac{x}{2} dx + \int e^{x} \tan \frac{x}{2} dx + c$$

$$e^{t} \tan \frac{x}{2} + c$$

30.
$$\int_{0}^{\pi/2} \csc^2 x \, dx = [-\cot x]_{1/4}^{\pi/2}$$

$$= \left(-\cot\frac{\pi}{2} + \cot\frac{\pi}{4}\right)$$

$$= -[0-(1)] = 1$$

31. Let
$$I = \int_0^{\pi/4} \log (1 + \tan x) dx$$

 $\Rightarrow I = \int_0^{\pi/4} \log \left[1 + \tan \left(\frac{\pi}{4} - x \right) \right] dx$

$$\Rightarrow I = \int_0^{\infty} \log \left[1 + \tan \left(\frac{\pi}{4} - x \right) \right] dx$$

$$\left[\because \int_0^a f(x) dx = \int_0^a f(a - x) dx \right]$$

$$= \int_0^{\pi/4} \log \left[1 + \frac{1}{1 + \tan x} \right] dx$$

$$= \int_0^{\pi/4} \log \left[\frac{1 + \tan x}{1 + \tan x} \right] dx$$

$$= \int_{0}^{\pi/4} \log 2 \, dx - \int_{0}^{\pi/4} \log (1 + \tan x) \, dx$$

$$\Rightarrow I = \log 2[x]_{0}^{\pi/4} - I \qquad \text{[from Eq. (i)]}$$

$$\Rightarrow I = \log 2[x]_0^{\pi/4} - I \qquad \text{[from }$$

$$\Rightarrow \qquad 2I = \frac{\pi}{4} \log_c 2$$

$$\Rightarrow I = \frac{\pi}{8} \log_e 2$$

32. Let
$$z = \frac{1+2i}{1-(1-i)^2}$$

$$= \frac{1+2i}{1-(1^2+i^2-2i)} = \frac{1+2i}{1+2i}$$
=1

= 1

$$|z| = 1$$
 and amp $(z) = \tan^{-1} \left(\frac{0}{1}\right) = 0$

33.
$$\lim_{x\to 0} \frac{\tan x - \sin x}{x^3} \left(\frac{0}{0} \text{ form} \right)$$

(using L'Hospital's rule)
$$= \lim_{x \to 0} \frac{\sec^2 x - \cos x}{3x^2} \qquad \left(\frac{0}{0} \text{ form}\right)$$
(using L'Hospital's rule)

(using L'Hospital's rule)
$$= \lim_{x \to 0} \frac{2 \sec^2 x \tan x + \sin x}{6x} \qquad \left(\frac{0}{0} \text{ form}\right)$$

$$= \lim_{x \to 0} \frac{2(\sec^2 x \sec^2 x + 2 \sec x)}{x \sec x \tan x \tan x} + \cos x$$

$$=\frac{3}{6}=\frac{1}{2}$$

34.
$$f(x) = \begin{cases} \frac{\sin 5x}{x^2 + 2x}, & x \neq 0 \\ k + \frac{1}{2}, & x = 0 \end{cases}$$

$$k + \frac{1}{2}, \quad x = 0$$

LHL
$$f(0^-) = \lim_{h \to 0} f(0 - h)$$

$$= \lim_{h \to 0} \frac{\sin 5 (0 - h)}{(0 - h)^2 + 2 (0 - h)}$$

$$= \lim_{h \to 0} \frac{\sin (-5h)}{h^2 - 2h}$$

$$\lim_{h \to 0} \frac{h^2 - 2h}{h^2 - 2h} = -\lim_{h \to 0} \frac{\sin 5h}{\frac{5h}{5}(h - 2)} = -\frac{1}{\frac{1}{5}(-2)}$$

Since, it is continuous at r = 0LHL - f(0)

$$\Rightarrow \frac{5}{2} = k +$$

$$\Rightarrow k = 2$$

35. Required area = area of curve PSMNROP



= 2 area of curve PSRQP
=
$$2 \int_{a}^{4a} \sqrt{4ax} dx$$

$$= 4\sqrt{a} \left[\frac{x^{3/2}}{3/2} \right]_a^{44} = \frac{8}{3}\sqrt{a} \left[(4a)^{3/2} - a^{3/2} \right]$$
$$= \frac{8}{3}\sqrt{a} \left(8a^{3/2} - a^{3/2} \right) = \frac{56}{3} a^2$$

36.
$$p(t) = 1000 + \frac{1000t}{100 + t^2}$$

On differentiating both side w.r.t. t. $p'(t) = 0 + \frac{(100 + t^2)(1000) - 1000t(2t)}{t^2}$

$$=1000\frac{(100-t^2)^2}{(100-t^2)^2}$$

Put p'(t) = 0 for maxima or minima $\Rightarrow 100 - t^2 = 0$

Now, again differentiating Eq. (ii), w.r.t. x

 $\begin{array}{c}
p^{**}(t) = 1000 \\
\times \left[\frac{(100 + t^2)^2 (-2t) - (100 - t^2)^2 (100 + t^2)}{(100 + t^2)^4} \right] \\
\end{array}$

$$= 1000 t \frac{(100 + t^2)^n}{(100 + t^2)(-2) - (100 - t^2)(4)}$$

$$= (100 + t^2)^3$$

 $=-1000t \frac{[600-2t^2]}{(100+t^2)^3}$

At

At p''(t) < 0The maximum value is

 $p(10) = 1000 + \frac{10000}{100 + 100}$

$$= 1000 + \frac{10000}{200} = 1000 + 50$$

= 1050

Since, the circle touches the y-axis, therefore
the centre lies on the x-axis. Let the centre be
(h, 0).

⇒ Radius of circle = h.



The equation of circle is given by $(x-h)^2 + (y-0)^2 = h^2$ $\Rightarrow x^2 + y^2 - 2hx = 0$

On differentiating both sides w.r.t. x, we get $2x + 2y \frac{dy}{dx} - 2h = 0$

 $\Rightarrow h = x + y \frac{dy}{dx}$

Putting the value of h in Eq. (i)

$$x^2 + y^2 - 2x\left(x + y\frac{dy}{dx}\right) = 0$$

 $\Rightarrow -x^2 + y^2 - 2xy \frac{dy}{dx} = 0$ $\Rightarrow x^2 - y^2 + 2xy \frac{dy}{dx} = 0$

$$\Rightarrow x^2 - y^2 + 2xy \frac{dy}{dx} = 0$$
This is the required differential equation.

38. Given differential equation is

(2x - y + 1) dx + (2y - x + 1) dy = 0⇒ 2x dx + 2y dy - (y dx + x dy) + dx + dy = 0⇒ (2x dx + 2y dy) - d(xy) + dx + dy = 0On integrating both sides, we get $x^2 + y^2 - xy + x + y = r$

39. $y = \tan^{-1} \frac{\sqrt{1 + x^2} - \sqrt{1 - x^2}}{\sqrt{1 + x^2} + \sqrt{1 - x^2}}$

Put $x^2 = \cos 2\theta$

$$y = \tan^{-1} \frac{\sqrt{1 + \cos 2\theta} - \sqrt{1 - \cos 2\theta}}{\sqrt{1 + \cos 2\theta} + \sqrt{1 - \cos 2\theta}}$$

$$= \tan^{-1} \frac{\cos \theta - \sin \theta}{\cos \theta + \sin \theta}$$

 $= \tan^{-1} \tan \left(\frac{\pi}{4} - \theta \right)$ $y = \frac{\pi}{4} - \theta = \frac{\pi}{4} - \frac{1}{2} \cos^{-1} x^{2}$

 $\Rightarrow y = \frac{\pi}{4} - \theta = \frac{\pi}{4} - \frac{1}{2} \cos^{-1} x^{2}$ On differentiating both sides, we get

$$\frac{dy}{dx} = 0 - \frac{1}{2} \left(-\frac{(2x)}{\sqrt{1 - x^4}} \right)$$

$$= \frac{x}{\sqrt{1 - x^4}}$$

40. Given that

en that

$$x = \sin t$$
, $y = \cos pt$
 $\frac{dx}{dt} = \cot t$, $\frac{dy}{dt} = -p \sin pt$
 $\frac{dy}{dx} = -\frac{p \sin pt}{\cos t}$

$$\Rightarrow y_1 = \frac{-p\sqrt{1-y^2}}{\sqrt{1-x^2}}$$

$$\Rightarrow y_1 \sqrt{1-x^2} = -p\sqrt{1-y^2}$$

On squaring both sides, we get $v_1^2 (1 - x^2) = p^2 (1 - y^2)$

$$y_1^+ (1 - x^-) = p^- (1 - y^-)$$
Again differentiating

 $2y_1y_2(1-x^2) - 2xy_1^2 = -2yy_1p^2$ or $(1-x^2)y_2 - xy_1 + p^2y = 0$

41. Given that

 $x = a(\theta + \sin \theta)$ and $y = a(1 - \cos \theta)$ $\Rightarrow \frac{dx}{d\theta} = a(1 + \cos \theta)$ and $\frac{dy}{d\theta} = a \sin \theta$

$$\frac{dy}{dx} = \frac{a \sin \theta}{a(1 + \cos \theta)}$$

$$=\frac{2\sin\frac{\theta}{2}\cos\frac{\theta}{2}}{2\cos^{\frac{\theta}{2}}}$$

$$=\tan\frac{\theta}{2}$$
Now, length of subtangent
$$=\frac{y}{|dy/dx|}$$

$$sT = \frac{a(1-\cos\theta)}{a(2\cos\theta)}$$

$$= a\frac{(1-\cos\theta)}{a(2\cos\theta)} = a\sin\theta$$

$$\sin\frac{\pi}{2}$$

$$= Length of subtangent at $\theta = \frac{\pi}{2}$,$$

⇒ Length of subtangent at
$$\theta = \frac{\pi}{2}$$
,
 $ST = a \sin \frac{\pi}{2} = a$

And length of subnormal =
$$y \frac{dy}{dx}$$

$$SN = a(1 - \cos \theta) \tan \frac{\theta}{2}$$

= $a2 \sin^2 \frac{\theta}{2} \tan \frac{\theta}{2}$

⇒ Length of subnormal at
$$\theta = \frac{\pi}{2}$$
, $SN = \alpha \cdot 2 \cdot \frac{1}{2} = \alpha$

Hence, SN = ST

$$x^2 + y^2 = 5$$
 ...(i)
and $y^2 = 4x$...(ii)

On solving Eqs. (i) and (ii), we get x = -5.1

at
$$x = -5$$
, $y^2 = -20$ (imaginary value)

$$at x = 1$$
, $y^2 = 4$

$$\Rightarrow y = \pm 2$$
Hence, point of intersection are (1, 2) and

On differentiating Eq. (i) w.r.t. x, we get $2x + 2y \frac{dy}{dx} = 0$

46. Angle turned by the body
$$\theta = \theta_0 + \theta_1 t + \theta_2 t^2$$
Angular velocity

$$\omega = \frac{d\theta}{dt}$$

$$= \frac{d}{dt} (\theta_0 + \theta_1 t + \theta_2 t^2)$$

 $= \theta_1 + 2\theta_2 t$

$$m_1 = \begin{pmatrix} dy \\ dx \end{pmatrix}_{(1,2)} = -\frac{1}{2}$$
And on differentiating Eq. (ii) w.r.t. x, we get
$$2y \frac{dy}{dx} = 4$$

$$\Rightarrow \frac{dy}{dx} = \frac{2}{y}, m_2 = \left(\frac{dy}{dx}\right)_{(1,2)} = \frac{2}{2} = 1$$

 $\frac{dy}{dx} = -\frac{x}{y}$

Now,
$$\tan \theta = \frac{m_1 - m_2}{1 + m_1 m_2}$$

$$= \frac{-\frac{1}{2} - 1}{1 - \frac{3}{2} - \frac{3}{2}} = \frac{3}{2} - \frac{3}{2}$$

$$= \begin{vmatrix} -\frac{1}{2} - 1 \\ 1 - \frac{1}{2} \end{vmatrix} = \begin{vmatrix} -\frac{3}{2} \\ \frac{1}{2} \end{vmatrix} = 3$$
43.
$$U = \{x : x^3 - 6x^4 + 11x^3 - 6x^2 = 0\}$$

$$= \{0, 1, 2, 3\}$$

$$0 = (x : x^{2} - 6x^{6} + 11x^{3} - 6x^{2})$$

$$= (0, 1, 2, 3)$$

$$A = (x : x^{2} - 5x + 6 = 0)$$

=
$$\{2, 3\}$$

and $B = \{x : x^2 - 3x + 2 = 0\}$
= $\{2, 1\}$

=
$$\{2, 1\}$$

 $A \cap B = \{2\}$
 $\therefore (A \cap B)' = U - (A \cap B)$
= $\{0, 1, 2, 3\} - \{2\} = \{0, 1, 3\}$

$$(11)_2 = 2^1 + 2^0 = 2 + 1 = 3$$

 $(101)_2 = 2^2 + 2^0 = 4 + 1 = 5$
 $(10)_2 = 2^1 = 2$

$$\begin{array}{c} (10)_2 = 2^t = 2\\ \text{and} \qquad (01)_2 = 1\\ (1001)_2^{1/12} - (101)_2^{1/12}\\ \\ \therefore \frac{(1001)_2^{1/12} - (101)_2^{1/12}}{(1001)_2^{1/12} + (101)_2^{1/12}} + (101)_2^{1/12}\\ \\ 0^1 = 8^1 \\ \end{array}$$

$$= \frac{9 - 3}{9^2 + 9 \times 5 + 5^2}$$

$$= \frac{(9 - 5)(9^2 + 9 \times 5 + 5^2)}{(9^2 + 9 \times 5 + 5^2)}$$

$$= 9 - 5 = 4 = (100)_2$$

Angular acceleration
$$\alpha = \frac{d\omega}{dt}$$

$$= \frac{d}{dt} (\theta_1 + 2\theta_2 t)$$

48. Acceleration of the body down the rough inclined plane = $g \sin \theta$

=
$$mg \sin \theta$$

= $5 \times 10 \times \sin 30^{\circ}$
= $5 \times 10 \times \frac{1}{2} = 25 \text{ N}$

49. Work done
$$W = \int_0^x F \cdot dx$$

$$= \int_0^x Cx \, dx = C \left(\frac{x^2}{2}\right)_0^x$$
$$= \frac{1}{2} Cx^2$$

50. A.B - A × B

$$AB \cos \theta = A B \sin \theta$$

 $\tan \theta = 1$
 $\tan \theta = \tan 45^{\circ}$

Given circuit is a balanced Wheatstone bridge.
 So, diagonal resistance of 2Ω will be ineffective.



Equivalent resistance of upper arms = $2 + 2 - 4 \Omega$

Equivalent resistance of lower arms $= 2 + 2 = 4 \Omega$

Maximum % error in X

= $a\alpha + b\beta + c\gamma$ 53. Induced emf e = 2V

$$\Delta t = 2 \times 10^{-3} \text{ s}$$
Coefficient of self induction
$$L = \frac{e}{\delta i} = \frac{-2}{(6-8)/2 \times 10^{-3}}$$

$$= \frac{-2 \times 2 \times 10^{-3}}{-2}$$

$$= 2 \times 10^{-3} \text{ ft}$$

54. Potential at the centre of a hollow metal sphere

$$V = \frac{1}{4\pi\varepsilon_0} \frac{Q}{R}$$

56. Refractive index of prism

$$\mu = \frac{\sin \frac{A + \delta_m}{2}}{\sin \frac{A}{2}}$$

$$= \frac{\sin \frac{60^\circ + 30^\circ}{2}}{\sin \frac{60^\circ}{2}}$$

$$= \frac{\sin 45^\circ}{\sin 30^\circ} = \frac{1/\sqrt{3}}{1/2}$$

$$= \frac{1}{6} \times \frac{2}{3} = \sqrt{2}$$

58. Current given by cell

$$I = \frac{E}{R}$$

Power delivered in first case

$$P_1 = I^2 R_1$$

$$= \left(\frac{E}{R_1 + r}\right)^2 R_1$$

 $= \left(\frac{1}{R_1 + r}\right)^{-\frac{r}{2}}$ Power delivered in second case

$$P_2 = I^2 R_2$$

$$= \left(\frac{E}{R_2 + r}\right)^2 R_2$$

Power delivered is same in the both the case $\begin{pmatrix} E \end{pmatrix}^2 = \begin{pmatrix} E \end{pmatrix}^2 =$

$$\left(\frac{E}{R_1 + r}\right)^2 R_1 = \left(\frac{E}{R_2 + r}\right)^2 R_2$$

$$\frac{R_1}{(R_1 + r)^2} = \frac{R_2}{(R_2 + r)^2}$$

$$\begin{split} R_1 \left(R_2^2 + r^2 + 2R_2 r \right) &= R_2 (R_1^2 + r^2 + 2R_1 t) \\ R_1 R_2^2 + R_2 r^2 + 2R_1 R_2 r &= R_2 R_1^2 + R_2 r^2 + 2R_1 R_2 t \end{split}$$

$$R_1 R_2^2 - R_2 R_1^2 = R_2 r^2 - R_1 r^2$$

 $R_1 R_2 (R_2 - R_1) = r^2 (R_2 - R_1)$

 $r = \sqrt{R_1 R_2}$

- on. At the top most point of the projectile there is anly horizontal component of velocity and acceleration due to gravity is vertically downward, so velocity and acceleration are nemendicular to each other.
- 41 u = 20 cm. f = 20 cm From mirror formula.

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

$$\frac{1}{20} = \frac{1}{v} + \frac{1}{-20}$$

$$\frac{1}{v} = \frac{1}{20} + \frac{1}{20}$$

$$\frac{1}{v} = \frac{2}{20} \implies v = 10 \text{ cm}$$

- 62. According to law of conseration of angular momentum, if there is no torque on the system. then the angular momentum remains constant.
- 63. Equivalent focal length

$$F = \frac{1}{f_1} + \frac{1}{f_2}$$

$$= \frac{1}{20} + \frac{1}{30}$$

$$F = \frac{20 \times 30}{20 + 30}$$

$$= \frac{600}{50} = 12 \text{ cm}$$

64. For isothermal process

$$PV = K$$
 (constant)
 $P = \frac{K}{V}$...(1)

For adiabatic process

atic process
$$PV' = K \qquad \text{(constant)}$$

$$P = K \qquad \text{(constant)}$$

$$= \frac{K}{V'}$$

$$= \frac{K}{K} = K(2^{Y})$$

From Eqs. (1) and (2), we have

 $P_2 > P_1$

- 68. According to Newton's law of cooling, $t_1 < t_2$. 66. The lift is moving with constant velocity so, there will be no change in the acceleration hence time period will remain same.
- 67. $x_1 = 2 \sin \omega t$ $x_2 = 4 \sin (\omega t + 90^\circ)$ The phase difference between the two waves is

So, resultant amplitude

$$a = \sqrt{(3)^2 + (4)^2}$$

$$= \sqrt{9 + 16} = \sqrt{25}$$

$$= 5 \text{ unit}$$

68. B = 0.5 T A. = 101 cm2 = 101 × 10-4 m2

 $A_2 = 100 \text{ cm}^2 = 100 \times 10^{-4} \text{ m}^2$

R = 20 Amount of charge q = BAA

 $= \frac{0.50 \times (101 \times 10^{-4} - 100 \times 10^{-4})}{2}$ $= \frac{0.05 \times 1 \times 10^{-4}}{2}$

= 2.5 × 10-6 C 70. Amplification factor µ = 20

Plate resistance $R_a = 10 k \Omega$ = 10 × 103 O

.: Mutual conductance

= 2 milli mho

75. For wavelength

Here, transition is s

 $\frac{\lambda_H}{\lambda_{11}} = \frac{(Z_{1j})^2}{(Z_2)^2} = \frac{(3)^1}{(3)^2} = 9$

76. m = 1000 kg $\frac{\Delta m}{\Delta t} = 4 \text{ kg/s}, v = 3000 \text{ m/s}$

Thrust on the rocket $F = -v \frac{\Delta m}{\Delta t}$

-- 12000 N

(Negative sign indicates that thrust applied in a direction opposite to the direction of escaping 79. The direction of magnetic field is alone the direction of motion of the charge particles, so angle will be 0°.

(sin 0 = 0)

Force $F = qvB \sin \theta$ - meR sin O

So, there will be no change in the velocity. 81. Mass defect

Am = Total mass of α-particles - mass of 12C nucleus

= 3 × 4.002603 - 12 = 12.007809 - 12 - 0.007809 unit

82. $\frac{N_p}{N_r} = \frac{1}{10}$

$$V_p = 230 \text{ V}, I_s = 2 \text{ A},$$

$$\frac{I_p}{I_s} = \frac{N_s}{N_p}$$

$$\frac{I_p}{2} = \frac{10}{1}$$

83. Equation of wave

 $v = 2 \sin (kx - 2r)$ Comparing with standard equation v = A sin (k v = 0.0) A = 2 m = 2 .. Maximum particle velocity

 $v_{max} = A\omega = 2 \times 2$ = 4 unit

85. $N = N_0 \left(\frac{1}{2}\right)^7$

$$\frac{N_0}{16} = N_0 \left(\frac{1}{2}\right)^2$$
$$\left(\frac{1}{2}\right)^4 = \left(\frac{1}{2}\right)^n$$

 $T_{1/2} = \frac{1}{4} h = 15 min$

Reasoning

the conclusion

- 141. Second is a bigger unit than the first, though both are used to measure the same quantity.
- 142. Except (d) all other groups contain only small letter.
- 143. Clearly, Fig. (d) will complete the pattern when placed in the blank space of fig. (x) as shown below. In the following question, a statement group statements is given followed

by same conclusion choose logically follows from the

given statement. 145. In fig. X, the upper triangular half of the paper has been folded over the lower half. In fig. Y, the paper is refolded to a quarter

In fig. Z, a square has been punched in the folded paper.

Clearly, the square will appear in each of the trianglular quarters of the paper.

Thus, when the paper is unfolded, four source will appear symmetrically over it and it will resemble fig. (C).

148, Clearly. (3 + 2)2 = 25

 $(15+6)^2 = (21)^2 = 441$ $(10 + 7)^2 = (17)^2 = 289$

So, missing number = $(12 + 13)^2 = (25)^2 = 625$

- 149. The first letter of each term is moved the steps forward and the last letter is moved two sleps backward to obtain the corresponding letters of the next term. The numbers follow the sequence, ×2 + 1, *2 + 2, ×2+3×2+4 So 10 is wrong and must be replaced by
- (4 x 2+ 1)i.e. 9. 150. Clearly, in the first and second rows, the secon figure is the inner part of the first figure and the third figure is the inner part of the secon figure.

Thus, the missing figure should be the into part of the second figure in third row, i. 6.4 small circle.